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1404

ANALYSIS OF THE EFFECT OF WIND ON A HIGH REINFORCED
CONCRETE BUILDING

COMPARISON OF APPROXIMATE AND EXACT METHODS

BY

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SUBMITTED TO THE SCHOOL OF ENGINEERING, AMERICAN
UNIVERSITY OF BEIRUT, IN PARTIAL FULFILMENT OF
REQUIREMENTS FOR THE DEGREE OF MASTER OF ENGINEERING
WITH MAJOR IN CIVIL ENGINEERING.

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BEIRUT, LEBANON

DECEMBER, 1964

A C K N O W L E D G E M E N T

The subject matter and title were suggested by Dr. Jack Nasser, Professor of Civil Engineering, A.U.B. His help, devotion and constructive criticism were indispensable guiding lines all through; from the choice of the subject till the present appearance of my work.

I am also indebted to Dr. Nasser's endeavor during his special visit last September to the I.B.M. Center in Paris from where he brought some important programs among which was the Frame Analysis one.

I also wish to express my thanks to:

Dr. Robert Sloane, Prof. Munir El-Khatib and Dr. Zuheir Alami for serving on my supervisory committee.

Prof. A. Vogt, School of Engineering, A.U.B., for his revision of my work and helpful suggestions.

Mr. Arch Johnston, General Director of the Computer Center, A.U.B., for his help in acquiring programs from different I.B.M. Centers.

Mrs. Susan Magnuson, Consultant of the Computer Center, A.U.B. for her help in handling the program for the solution of simultaneous equation.

Riad M. Shahin

Beirut, Lebanon

December, 1964

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CHAPTER ONE

SCOPE AND OBJECTIVES

This thesis serves a dual goal. The first deals with the study of the influence of wind on high reinforced concrete buildings, and the comparison of two methods of analysis. The first one, the Hardy Cross Method, is considered as an ingenious and convenient method of handling the stress analysis of all types of rigid joint structures subjected to any sort of loading. The other being the Factor Method, is used only for analyzing building frames acted upon by lateral loads.

The Hardy Cross Method gives exact values because it consists in solving the simultaneous equation in the slope-deflection method by successive approximations.

"The Factor Method is the most accurate among the approximate methods. Whereas the Portal and Cantilever Methods depend upon certain stress assumptions that make possible a stress analysis based on the equations of statics, the Factor Method depends on certain assumptions regarding the elastic action of the structure, which makes possible an approximate slope-deflection analysis of the frame. While based upon the slope-deflection method of analysis, it is possible to formulate a relatively simple set of rules by which the method can be applied without knowledge of the elastic principles upon which it is based."⁽¹⁾

The statements made so far convey that the comparison is one based on competitive exactness of the two different methods. Such as

(1) J.B. Wilbur and C.H. Norris, "Elementary Structural Analysis", p. 280, McGraw-Hill Book Company, New York, 1948.

evaluation in the author's point of view is unfair, because the Founder of the Factor Method does not claim, in any respect, the exactness of his method as compared with the Hardy Cross Method.

The basic concept of this comparison is one regarding the fundamentals of the methods, which could be misleading in the case of the Factor Method while it is not the case with the Hardy Cross Method.

The author ran three sets of calculations by the two methods for the cases mentioned below:

1. A frame with very stiff columns versus concealed beams with an extremely small stiffness.
2. A frame with the same column stiffness in "1", versus drop beam of better stiffness than in "1", but yet with relatively small stiffness as compared to the columns.
3. A frame with columns and beams whose stiffness is of the same order.

In all the three sets of analyses the Factor Method gave values of moments for both the columns and beams which indicated no signs of erroneous results even for the first two critical cases, but failed to do so when checked by the Hardy Cross Method.

I shall go no further regarding the first objective which constitutes the backbone of this thesis, and which was encouraged by Dean John B. Wilbur, former Dean of the School of Engineering, A.U.B., and the founder of the Factor Method.

The second objective of this thesis is a numerical illustration of the analysis carried out in the first part. In order to be practical in this thesis the author ran his analysis on the frames of a twenty story reinforced concrete building with assumed site conditions which were maintained constant throughout the whole thesis.

Finally, it was not my intention to go into meteorological or physical description of wind. The only variables being the sections of the members.

CHAPTER TWO
S T U D Y O F W I N D

Wind Loads, General Discussion:

Wind load is one of the most important loads that an engineer has to deal with and is also one that is most difficult to evaluate properly. The magnitude of wind pressure is intimately connected with wind velocity, and (as has been determined by tests of model structures in wind tunnels) with the shape of the structure. The magnitude of wind velocity varies with the geographical location of the structure and the height of the structure. These involved relationships have resulted in a very chaotic situation which is being clarified at the present time. Two solutions to the problem of evaluating wind loads are usually considered: the present solution, as reflected in buildings codes and specifications; and the future solution, as is anticipated in current periodical literature. The fundamental approach, however, is the same, namely, the relationship between velocity and pressure.

Relationship Between Velocity and Pressure:

The derivation of this relationship is, like so much of engineering, due to Sir Issac Newton and is therefore quite frequently referred to as the Newtonian Theory. If a stream of air flows around an object, as shown in Fig. 1 , a pressure is created on the "nose" of the object. The pressure may be found from a consideration of the energy involved.



Fig. 1

Energy exists in three forms: Kinetic energy, potential energy, and pressure energy. They are defined as follows:

1. Kinetic Energy: This is the energy which a mass possesses because of its motion; that is,

$$KE = \frac{1}{2} Mv^2 = \frac{Wv^2}{2g}$$

where M = mass

W = weight

g = gravitational constant

v = velocity

2. Potential Energy: This is the energy a mass possesses because of its position above some horizontal datum plane. Therefore

$$\text{Pot. E} = WZ$$

where Z = the distance above the datum plane.

3. Pressure Energy: This is the energy that a fluid has because it is under pressure, for example, water in a pipe under pressure has

pressure energy. Hence,

$$\text{Press. E.} = \frac{W \times p}{w}$$

where p = pressure

W = weight the pressure could lift

w = weight per unit volume of the fluid.

Fig. 2 shows fluid in a pipe which has energy of the three types.

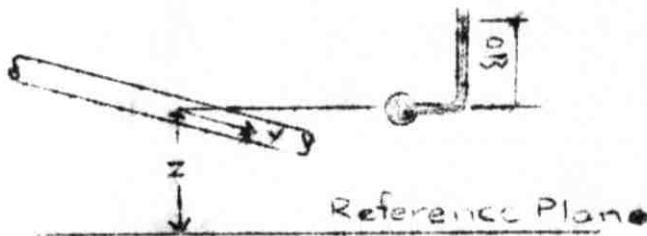


Fig. 2

In any fluid flow the sum of the energies at all points must be constant, as has been stated by Bernoulli, that is

$$\frac{Wv^2}{2g} + WZ + \frac{WP}{w} = \text{constant.}$$

If each term is divided by W , the sum of the resulting three terms is called total head and is designated H . Therefore,

$$H = \frac{v^2}{2g} + Z + \frac{p}{w}$$

The three terms are called velocity head, gravity head, and pressure head respectively. If each term is multiplied by w , then the total energy, E , per unit volume is obtained as

$$E = \frac{wv^2}{2g} + wZ + P$$

The energy per unit volume as given above must remain constant for all points in the fluid.

In any object such as that shown in Fig. 1 there is a point, S, where the air has no velocity. This point is called the stagnation point. Since the energy at points O and S must be the same, then

$$p_o + \frac{wv_o^2}{2g} = p_s$$

The potential energy term does not appear since both points are being considered at the same elevation. It follows that

$$p_s - p_o = \frac{wv_o^2}{2g}$$

The rise in pressure, $p_s - p_o$, caused by bringing the air to rest, is the impact pressure of the air on the object and will be called q . Therefore,

$$q = \frac{wv_o^2}{2g} = \frac{wv^2}{2g}$$

The weight per unit volume of air varies with the temperature and the barometric pressure, and increases with a decrease in temperature.

However, for a specific condition both w and g are constants.

$$\text{Therefore, } q = C_1 V^2$$

Tests by Hillman of the action of wind pressure on vertical rigid obstacles resulted in

$$q_d = \frac{V^2}{16}$$

where q_d = dynamic pressure in Kg/m^2

V = velocity in m/sec .

Early experiments tried to verify the value of q by tests, that is, they tried to prove that

$$p = q$$

where p is the pressure on an object, but they were unsuccessful, until wind tunnels for research into aeronautical problems were devised. Here it was quickly learned, where controlled air flow as possible, that the proper relationship is

$$p = C_2 \cdot q$$

in which C_2 is a coefficient that varies with the size, shape, and position of the object in the air stream. The early experiments did not realize that the object itself had an effect, outside the projected area, on the pressure to which it was subjected.

Tests made by Hillman resulted in

$$p = C_3 \text{ Kr. } K_s \text{ } qd$$

where K_s = factor of site

K_r = factor of resonance

C_3 = factor due to taking into account the suction behind the building.

The values of the factors cited above are determined from experiments.

1. K_s

a - protected site = 0.60 - 0.80

b - ordinary site = 1.00

c - exposed site = 1.20 - 1.40

2. K_r

Determined from Fig. 4b, where

$$\lambda = \frac{2s}{H}$$

H being the height of the structure above ground, and s is the surface area up to mid-height.

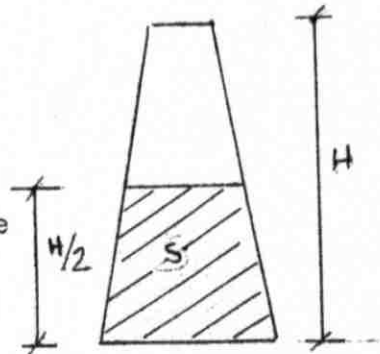


Fig 3

3. C_2 is usually taken as 1.20

Variation of Velocity and Dynamic Pressure with Height:

Wind velocity increases with height because the friction of the air and the earth reduces velocity near the ground. During 1889 extended observations were made from the top of the Eiffel Tower and simultaneously from the meteorological station near the base. The average velocity of the observations at the top (elevation 994 ft) was 15.80 miles per hour and at the base of the station (elevation 69 ft) was 5 miles per hour. On account of the low velocities these figures are

of little use to the structural engineer. (For higher velocities the differences were less).

The Stevenson formula so often quoted in textbooks is

$$V = v \left(\frac{H + 72}{h + 72} \right) \text{ (English Units)}$$

in which V is the velocity at a height H and v is the velocity at a lesser height h. The observations of Stevenson were made on heights not exceeding 50 ft. and on winds varying from 2 to 44 miles per hour. This is too limited a range for the structural engineer, although Stevenson later wrote that the formula "should be applicable to lofty engineering structures such as lighthouse towers, chimneys, and high-level bridges".

Another formula often quoted is the Archibald formula. Professor Archibald endeavored to determine values for the exponent X in the equation $\frac{V}{v} = \left(\frac{H}{h} \right)^X$

The Archibald formula is often given:

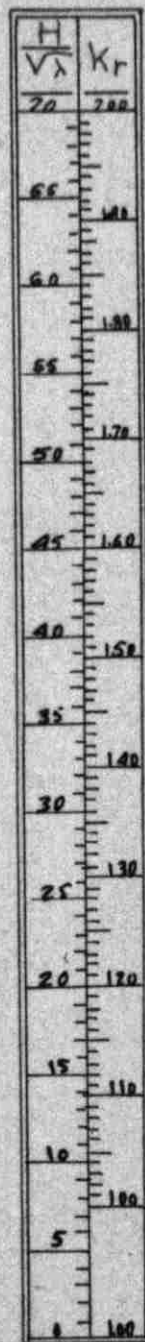
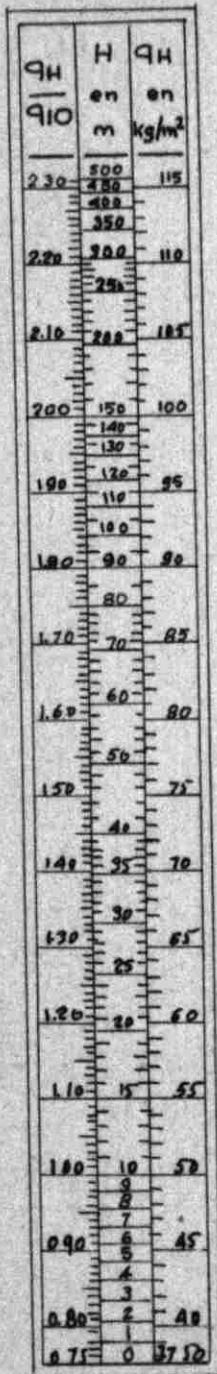
$$\frac{V}{v} = \left(\frac{H}{h} \right)^{\frac{1}{4}}$$

From the standpoint of this thesis the equation presented below is adopted.

$$\frac{q_H}{q_{10}} = 2.50 \frac{H + 10}{H + 60} \quad (1)$$

where q_H represents the dynamic pressure at a height H, where q_{10} is the pressure at a height of 10 meters.

(1) "Regles Definissant Les Effets De La Neige Et Du Vent Sur Les Constructions Applicables Aux Travaux Dependants Du Ministere De La Reconstruction Et De L'Urbanisme," p. 8, Paris, 1947.

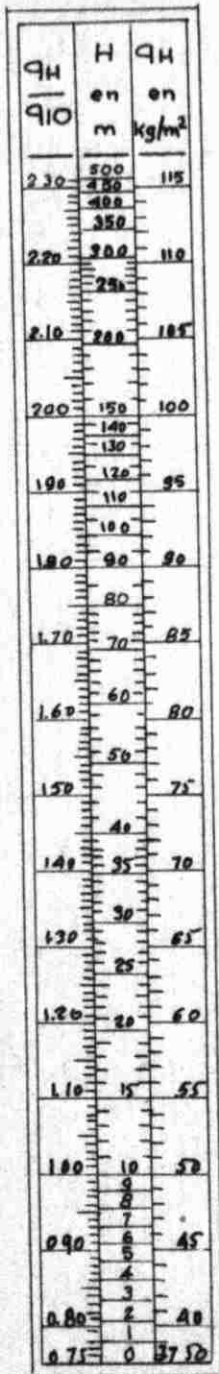


EFFECT OF HEIGHT ⁽¹⁾

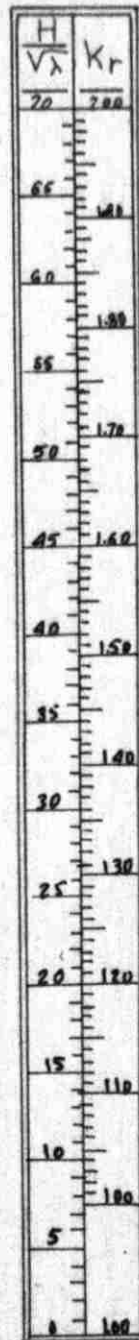
EFFECT OF RESONANCE ⁽¹⁾

Fig.4a, and b.

(1) Ibid, p.10.



EFFECT OF HEIGHT ⁽¹⁾



EFFECT OF RESONANCE ⁽¹⁾

Fig.4a, and b.

(1) Ibid, p.10.

CHAPTER THREE

FACTOR METHOD (1)

This method may be applied by carrying out the following six steps:

1. Compute the girder factor g for each joint. Record at the girder ends at the joint.

$$g = \frac{\sum K_c}{\sum K}$$

where $\sum K_c$ = sum of K values for columns at the joint.

$\sum K$ = sum of K values of all members at the joint.

2. Compute the column factor c for each joint.

$$c = 1 - g$$

Record at the column ends at the joint.

At a fixed base, $c = 1.00$

3. Every member of the frame has a number appearing at each end. To each number add half the number at the far end of the member.

4. Multiply the sums obtained in step 3 by the K value of the member. Call this number the column moment factor C and the girder moment factor G . The column moment factors C are the approximate relative column-end moment values. Similarly, the girder moment factors G are the

(1) J.B. Wilbur and C.H. Norris, "Elementary Structural Analysis", p. 280, McGraw-Hill Book Company, New York, 1948.

approximate relative girder-end moment values.

5. The sum of the C values divided by the column height is the relative column shear, and the sum of all the column shears is the story shear. Thus adding the C values for each column gives the relative column shear taken by each column, and the actual shear taken by any column is equal to the story shear multiplied by the sum of the column C values divided by the sum of all of the C values for the story. The column-end moments then follow by simple proportions.

$$M_{C1} = \frac{C_1}{\sum C \text{ for story}} \times Hh$$

All column moments are obtained in a similar fashion.

6. The girder moments are now obtained by statics and simple proportion where necessary.

CHAPTER FOUR
HARDY CROSS METHOD

(1) The Use of Auxiliary Force Systems to Control Translation of the Joints.

The method consists in applying a system of auxiliary forces F_b , F_c , and F_d to prevent any horizontal displacements. This allows the analysis of the structure by the regular moment distribution method. Replace these forces by three different auxiliary force systems, as shown by Figures 1b, c, and d, each of which permits one horizontal displacement. The algebraic relation existing between any single displacement and the force system producing it will be known if it is determined for any assumed value of Δ . Hence, express each auxiliary force system, the shears and the moments which it produces in terms of one displacement Δ .

The equilibrium conditions will result in three equations in terms of the three unknown sideways, expressed as:

$$F_{b_1} + F_{b_2} + F_{b_3} + F_b = 0$$

$$F_{c_1} + F_{c_2} + F_{c_3} + F_c = 0$$

$$F_{d_1} + F_{d_2} + F_{d_3} + F_d = 0$$

The final moments will be the summation of the corrected values due to the individual action of each displacement.

Analysis of Multistory Frames:

The above method is a powerful and relatively simple tool for determining moments in frames up to three or four floors. This method results in as many simultaneous equations as there are unknown joint translations, i.e.

(1) L.C. Maugh, "Statically Indeterminate Structures", p. 90, John Wiley & Sons, Inc., New York, 1956.

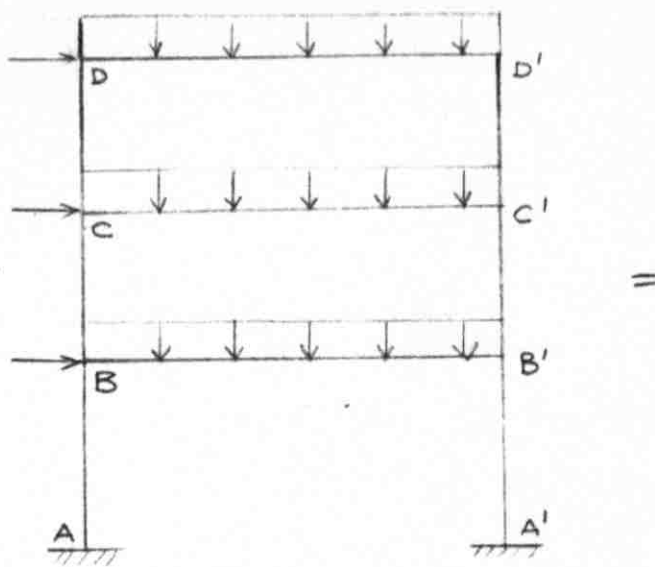


Fig. 1

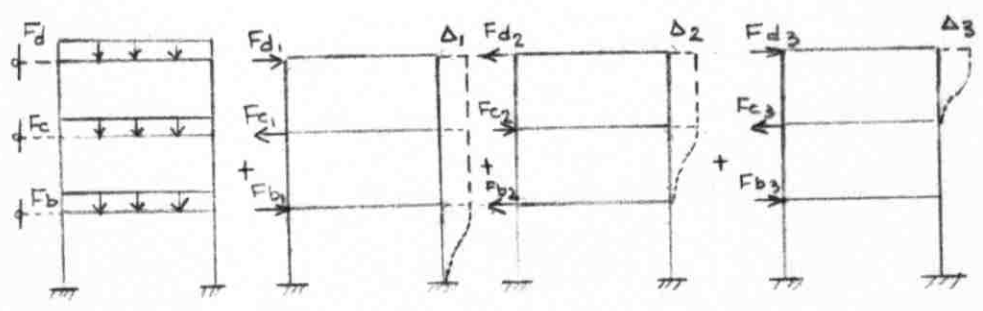


Fig 1a, b, c and d.

twenty equations with twenty unknowns for the case under consideration. Such a set of equations cannot be solved except by the computer. The work and time involved in preparing the equations are subject to many sources of errors. To overcome this difficulty the following method was suggested by Dr. Jack Nasser.

Assume the presence of hinges at mid-height of columns; and analyze the top most three floors. The assumption of hinges influence the lower floors more. So it is suggested to consider the moments of the top floor and the moments in the superior members of the lower floor as correct.

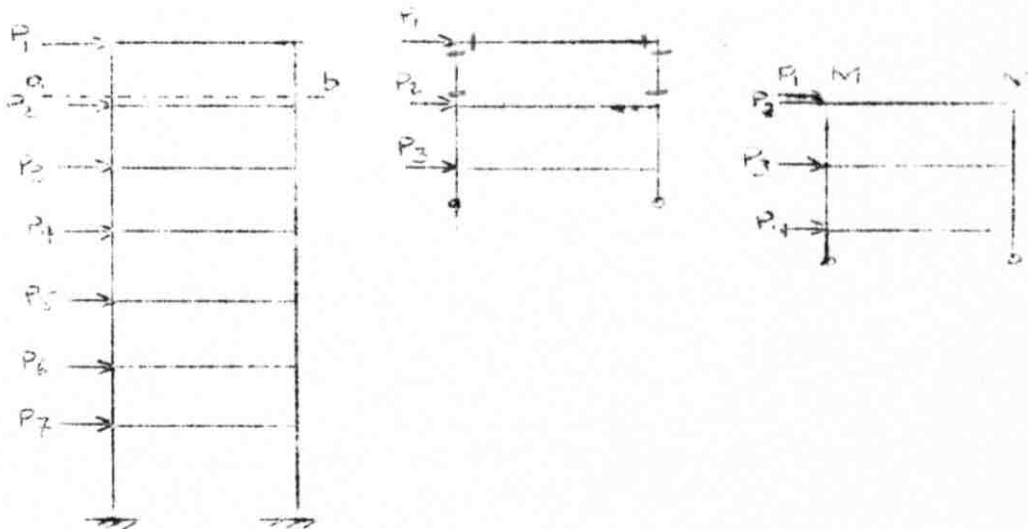


Fig 2a, b, and c

Cut the structure along the line ab, and go one floor lower. This implies the addition of the shear of the cut off floor and the moments of the cut off columns to the joints. This results in a frame subjected to the dual action of lateral forces and moments. The analysis due to

the action of moments boils to the same routine as the lateral forces. Much of the computational labor is saved if the total shear is taken when solving the simultaneous equations.

This method was adopted to Case C, while Case A was handled by analyzing the whole structure as a unity. The simultaneous equations were solved on a 1620, I.B.M. Computer.

Signs for Bending Moments:

Signs are one of the most prolific sources of error in analysis.

The convention of signs used in this thesis is as follows:

The internal moments or bending moments calls a moment positive when it produces tension on a designated side of the member. In ordinary design of beams, a bending moment is taken as positive if it produces tension on the bottom of the beam. In columns there is no standard sign for bending moments, we have used below the same convention as for beams when the column is looked at from the right-hand side of the sheet or if the tension is on the inward side of the column if the column is part of a frame.

However, when drawing the moment diagrams the upper side of the beam is considered positive, while the right side of the column is considered positive.

The above statements are interpreted below with the help of the deformation diagrams for a one story frame.

1. Wind From Left

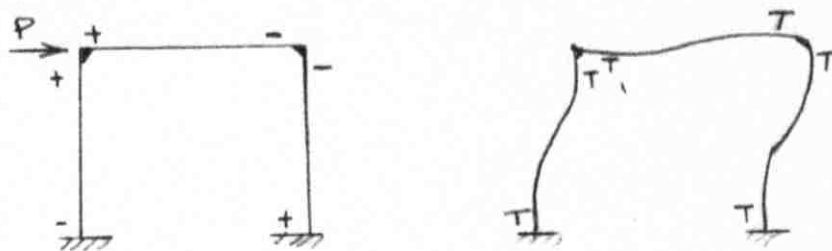


Fig 3a, and b.

2. Wind From Right.

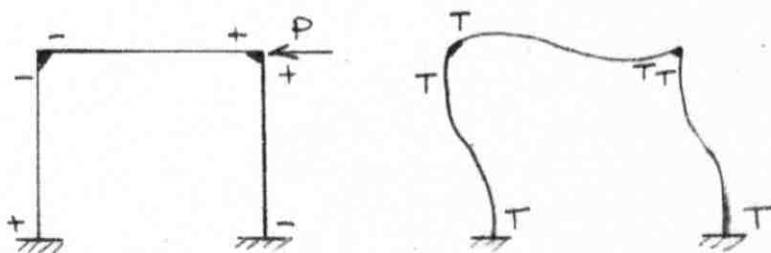


Fig 4a, and b

3. Vertical Loading.

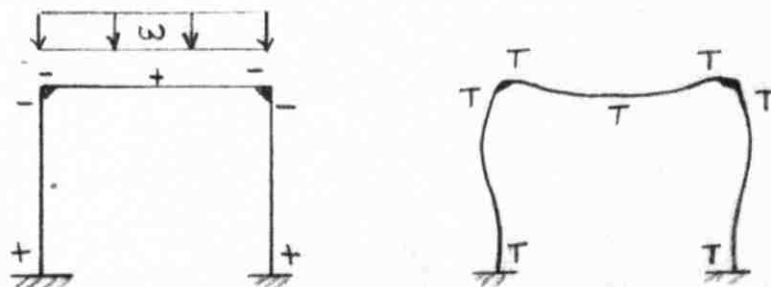


Fig 5a, and b

CHAPTER FIVE

ALLOWANCE FOR SYMMETRY

General:

In most methods of structural analysis it is possible to take advantage of any symmetry in a structure and its loading. Occasionally, however, symmetry is ignored, and much needless effort usually results. Sometimes, after a completely general approach to the analysis of a structure its symmetry is finally used to provide a check on the computations, such a check may, however, be found to apply mostly against the complications arising through neglect of the symmetry. The most evident course is to reduce the computational labour by allowing directly for symmetry, wherever possible.

A structure may be symmetrical, both in its geometry about a point or a "line" support (as, for example, in a continuous beam or a multi-story building frame with an even number of spans or bays). Then, with symmetrical loading there will be no joint rotation one way or the other in the beams passing over or through the central support. In such a case only half of the structure needs to be considered, with the ends of members at the center-line being taken as fixed in position and direction.

Another type of symmetry occurs when a symmetrical structure has its center-line equally between supports (as, for example, in a continuous beam or a multi-story frame with an odd number of spans). Then, with symmetrical loading, the adjacent joints on either side of the

center-line, and at the same level, must undergo equal and opposite regular displacements. Clearly only half of the structure need be analyzed if a stiffness modifications can be deduced for the central member. If the stiffness and restraint factors are known for these members when they are considered fixed-ended, the modified stiffness in this case can easily be deduced.

The various cases of symmetrical frames are discussed below:

Hardy Cross Method⁽¹⁾

1. Symmetrical Structures Symmetrically Loaded

a. Even Number of Span

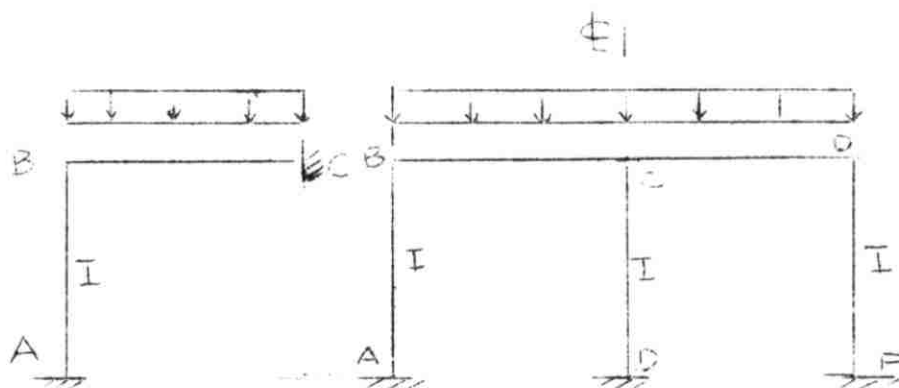


Fig. 1

CD will not move, therefore study ABC without any modifications of the factors.

b. Odd Number of Spans

(1) The contents of this section have been selected from material developed by Dr. Jack Nasser for the course of Advanced Structural Analysis for graduate students at the American University of Beirut.

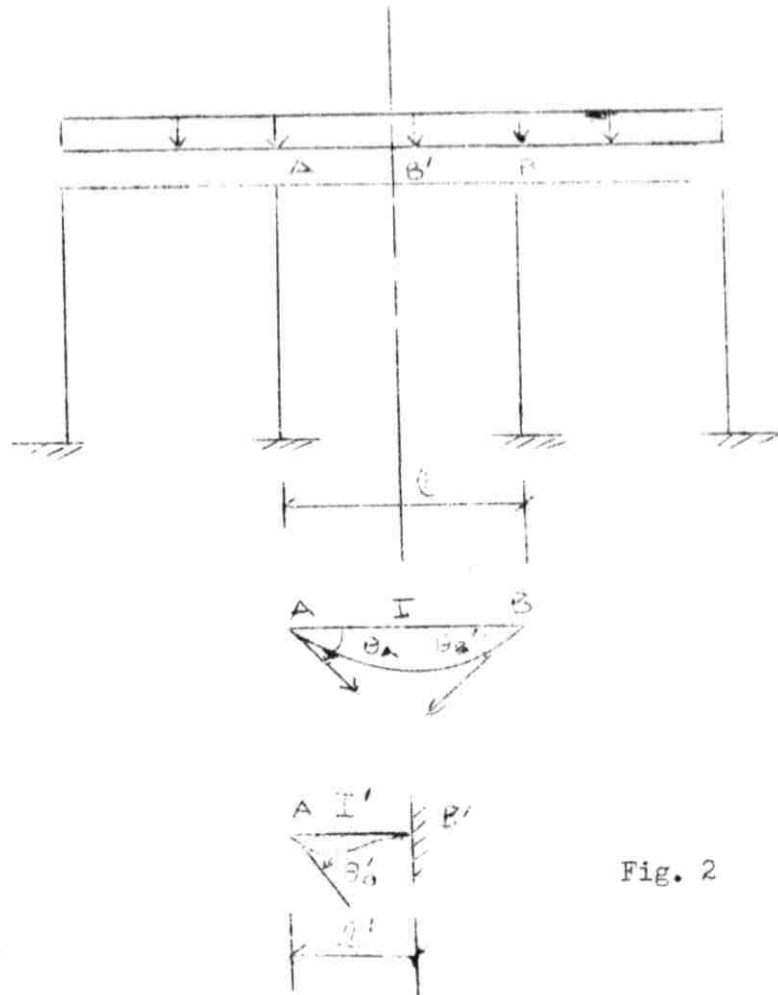


Fig. 2

$$\theta_a = \theta_b$$

$$\theta' a = \theta_a$$

$$M_{AB} = 2EK_{AB} (2\theta_A + \theta_B) = 2EK_{AB}\theta_A = 2E \frac{I}{l} \theta_A$$

$$M_{A'B'} = 2EK_{A'B'} \times 2\theta_{A'} = 4E \frac{I'}{l'} \theta_{A'}$$

$$2E \frac{I}{l} \theta_A = 4E \frac{I'}{l'} \theta_{A'}$$

$$\frac{I}{l} = 2 \frac{I'}{l'}$$

$$\frac{I'}{l'} = \frac{1}{2} \times \frac{I}{l}$$

$$\therefore K_{A'B'} = \frac{1}{2} K_{AB}$$

Hence in symmetrical structures symmetrically loaded with an odd number of spans it is allowable to analyze half of the structure provided the central span fixed end moment corresponds to its real stiffness and

a factor of stiffness equal to one half of the real stiffness.

2. Symmetrical Structures Non-Symmetrically Loaded

a. Even Number of Spans

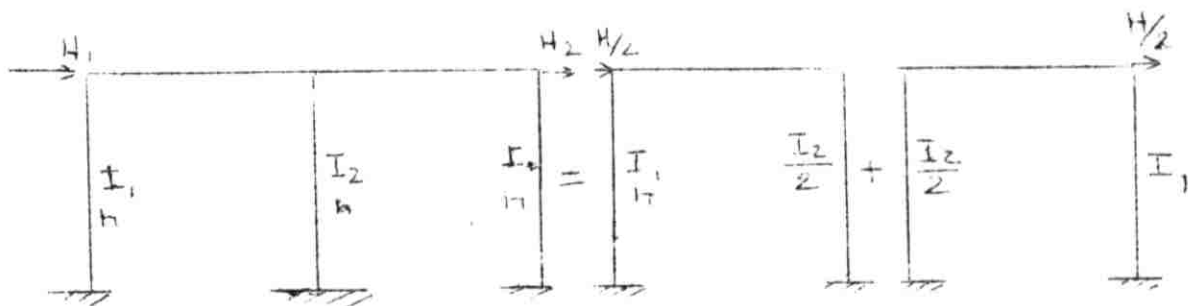


Fig. 3

where $H = H_1 + H_2$

b. Odd Numbers of Spans



Fig. 4

Because a point of inflection exists at B', $M_{B'} = 0$

Hence B' acts like a hinge from a deformation point of view.

$$K_{AB} = \frac{I}{L}$$

$$(K_{.B'})^R = \frac{3}{4} \cdot \frac{I}{\ell/2} = 1.50 \frac{I}{\ell}$$

Whence analyze half of the structure, supposing a hinge at midpoint by taking a stiffness for .B' equal to three half times .B.

Factor Method:

Because the Factor Method is a relatively short method, no attempts were made in textbooks about the utilization of the factors of symmetry. However, starting from the basic fact that the Factor Method combines both statics and the elastic behavior of members, the author was able to arrive at definite short cuts, which are in one way or another similar to the previous simplifications utilized by the Cross Method.

Symmetrical Structures Non-Symmetrically Loaded

a. Odd Number of Spans

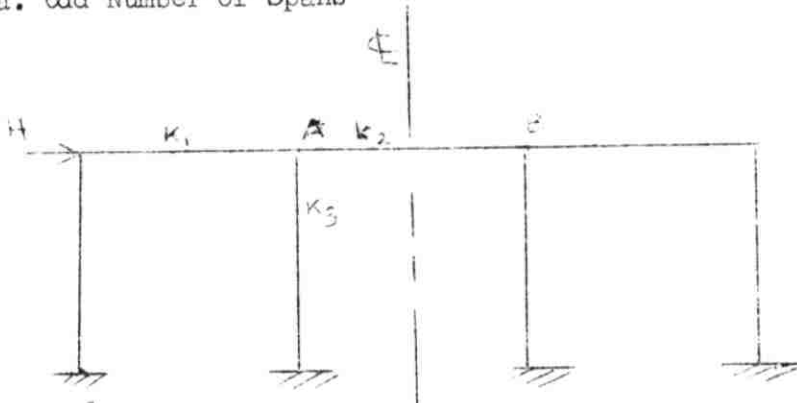


Fig. 5

The g-Factor at joint A is always equal to $\frac{K_3}{K_1 + K_2 + K_3}$

irrespective of whether we are analyzing the whole structure or half of

it provided that the stiffness of AB is kept the same in both analysis. Hence the c-Factor is kept constant at joint A.

However, when analyzing half the structure we are discarding half the value of the g-Factor coming to A from B and vice versa. Since the g-Factors at A and B are the same, after the c-Factors are calculated take 1.50 times the g-Factor at joint A. The fact that we are analyzing half the structure implies taking half the value of the shear.

Rule:

Analyze half the structure maintaining the same stiffness factor for the central span, provided that the c-Factor is calculated on the basis of the true g-Factor, then a modified g-Factor of three half times the true value is maintained throughout the rest of the calculations.

b. Even Number of Spans

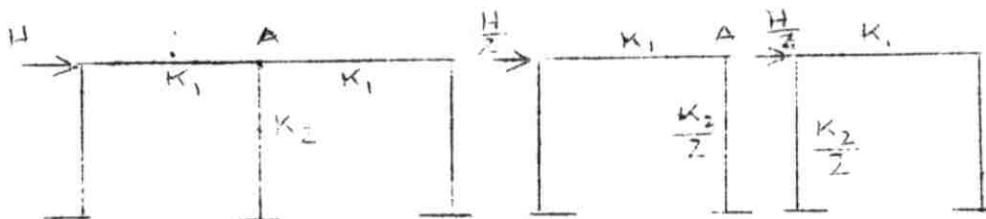


Fig. 6

g-Factor for A when analyzing the whole structure is equal to

$$\frac{K_2}{K_1 + K_1 + K_2} = \frac{K_2}{2K_1 + K_2}$$

g-Factor for A when analyzing half the structure is equal to

$$\frac{K_2/2}{K_1 + \frac{K_2}{2}} = \frac{K_2}{2\left(\frac{2K_1 + K_2}{2}\right)} = \frac{K_2}{2K_1 + K_2}$$

Hence the same rule for the Hardy Cross Method applies in this case.

CHAPTER SIX
SIMULTANEOUS EQUATION SOLUTION BY COMPUTER⁽¹⁾

Description:

This program generates solutions to a linear system of maximum matrix 39 x 39 with from 1 to 99 vectors. Division feature and indirect addressing are not necessary. The solution is accomplished without matrix inversion by the product matrix method. This method requires only $n^3/2$ multiplications and divisions as opposed to inversion which requires n^3 multiplications and divisions. The typed output of this program is the constant vectors and associated solution vectors.

All input and output is in excess 50 floating point notation.

Card Preparation:

Data input consists of 1 header card, 1 or more matrix cards and 1 or more constant vector cards per constant vector set.

Header Card:

Cols. 1 - 2: \bar{xx} = number of rows = number of columns in the matrix of coefficients.

Cols. 3 - 4: \bar{xx} = number of constant vectors.

Matrix Cards:

The matrix of coefficients by rows in floating point form with high order digits flagged. Utilize as many columns and as many cards as

(1) I.B.M. - 1620 Manuals.

needed with eight elements per card. A matrix of 6 x 6 will use 4 full cards and 40 columns of a 5th. A matrix of 2 x 2 uses only $\frac{1}{2}$ of one cards. A maximum matrix uses 190 full cards and 10 columns of 191st (39 x 39).

Constant Vector Card(s):

The constant vector in floating point form with high order digits flagged. Utilize as many columns and as many cards as needed with eight elements per card. A matrix of 16 x 16 with 1 constant vector of 6 elements requires 2 cards for constant vector description.

If more than 1 constant vector exists begin a new set of constant vector card(s) for each constant vector.

Example:

$$2x + 3y = 7$$

$$9x - 2y = 4$$

Card: 1 $\bar{0}\bar{2}\bar{0}\bar{1}$
 2 $\bar{5}\bar{1}\bar{2}\bar{0}\bar{0}\bar{0}\bar{0}\bar{0}\bar{0}\bar{0}\bar{0}$ $\bar{5}\bar{1}\bar{3}\bar{0}\bar{0}\bar{0}\bar{0}\bar{0}\bar{0}\bar{0}\bar{0}$ $\bar{5}\bar{1}\bar{9}\bar{0}\bar{0}\bar{0}\bar{0}\bar{0}\bar{0}\bar{0}\bar{0}$ $\bar{5}\bar{1}\bar{2}\bar{0}\bar{0}\bar{0}\bar{0}\bar{0}\bar{0}\bar{0}\bar{0}$
 3 $\bar{5}\bar{1}\bar{7}\bar{0}\bar{0}\bar{0}\bar{0}\bar{0}\bar{0}\bar{0}\bar{0}$ $\bar{5}\bar{1}\bar{4}\bar{0}\bar{0}\bar{0}\bar{0}\bar{0}\bar{0}\bar{0}$

Operation:

1. Clear memory
2. Load program deck
3. Program halts after loading

4. Ready data in card-read hopper.

5. Press start.

6. Program solves for all constant vector and halts.

If further systems are to be solved, ready reader with data
and press start.

Result:

Constant Vector

$\bar{5}170000000$

$\bar{5}140000000$

Solution of system for above listed vector

$\bar{5}084500000$

$\bar{5}117700000$

CHAPTER SEVEN
DISCUSSION OF RESULTS

The problem of the stresses produced in high buildings by wind has long occupied the attention of engineers in the case of buildings of steel; and the increase in height of buildings built of reinforced concrete has in recent years extended the problem to this field. Anyone who has given any thought to the subject knows that these structures are highly indeterminate. The problem involved in indeterminate structures has been approached by two methods: The Factor which is approximate, and the Hardy Cross which is exact. The problems of what wind pressure should be provided for and of how they would best be provided for are as important and were discussed in Chapter 4 (Appendix) no attempt is made here to comment on this part.

The laws of statics tell us a good deal in these problems, usually they tell us all that we really need to know in order to design the structure safely. In any given story the total shear is the total wind pressure above that story, which is assumed to be known. The sum of all bending moments at the top and at the bottom of all columns is, then, this shear multiplied by the height of the story. We may say, then, that the total moment in the story Hh is distributed in some way to the ends of the columns. The question of distribution of moments to columns calculated by the above method in the case of the Factor Method, and the fixed end moments to all member meeting at a joint of a frame

structures in the case of the Hardy Cross Method constitutes the first point to be discussed. Undoubtedly, the Hardy Cross Method is more correct because it distributes the moments at any joint in direct proportion to the stiffness of the members, which is a perfectly true assumption; whereas the Factor Method distributes the moments in a given story according to the column factors which again are functions of the stiffness of the columns of a given story. But the way these factors are computed does not, in my opinion, convey much confidence. However, the Factor Method distributes again the column moments at a joint to the beams according to g-Factors calculated as $\frac{\sum K_c}{\sum K}$ at a joint. This point needs a severe criticism, because it assumes that at any joint of a frame structure subject to wind the sum of column moments is equal to the beam moments. This is a completely valid statement in a perfectly rigid joint. The question here arises about the definition of a rigid joint, which could be stated as that joint whereby the members are connected to each other in a perfect manner through welding or bolts.

What about the definition in reinforced concrete terminology? Such definitions are not usually available in textbooks. From my point of view, a good definition should be based on the relative stiffness of the members meeting at a joint - e.g. "A rigid joint is a joint where the relative ratio of the stiffness of columns to that of beams meeting falls within certain limits". What are these limits? These limits are a function of many factors such as the number of member meeting at a joint, the overall height of the structure, the material used, the cross-sectional area, length of members and may be other factors. However,

the establishment of these limits are beyond the scope of this thesis. From the experience of the author throughout this analysis, it is conceived that if the stiffness of the members at a joint fall within the same order, it is quite safe to consider the joint rigid.

Hence a value of unity to the limits explained above permits the use of the Factor Method without leading to erroneous results as explained in the first case considered in this thesis, whereas the Hardy Cross Method is a perfectly true method for any kind of structure irrespective of the values of the limits explained above. This marks the second advantage of the Hardy Cross Method and which I believe, is the most important due to the absence of any restrictions regarding its application.

With this background one will be able to understand the results better. In the first two cases the Factor Method gave erroneous values of moments because the stiffness of the beams was very low as compared to the columns, a case whereby the Factor Method cannot be applied as explained before. Whereas the Hardy Cross Method gave correct answers for the first case with very small values of moments for the beams, which is an indication that the joints are not rigid; a case whereby the application of the Factor Method is prohibitive.

The writer was not encouraged to carry out an exact analysis for the second case on the light of the distribution factors calculated which ranged between 0.02 and 0.05 for the first ten floors, indicating no proper transfer of moments from columns (which are the donors) to the beams. The beams in this case being the recipient will acquire moments in proportion to their distribution factors, thus creating a partial problem which resolves itself in one way or another as an integral part of the first case. In the last case, when abiding by the restriction referred to on page 31, both methods lead to nearly the same results. This indicates that the Factor Method could be considered dependable for similar cases.

One more point should be discussed in order to be objective in this discussion. The time required to carry out an exact analysis is about ten times as much. In some cases, the need of meeting time schedules may be controlling factor. In other instances, economic considerations may make it desirable to use an approximate method of analysis. It may be less expensive to use more material, as a result of basing design on approximate stresses and on a higher apparent factor of safety with respect to the computed stresses, than to save material by basing design on exact stresses and a lower apparent factor of safety. This attitude may sometimes be properly taken in designing relatively unimportant structures or secondary portions of important structures. The analyst will also be influenced in this connection by his judgment as to magnitude of the errors likely to be introduced by the approximate method he proposes to use. Again, when the design of a statically indeterminate structure is first begun, the areas and moments of inertia of its members are not known. It is therefore necessary to carry out an approximate analysis for stresses in the structure, so as to obtain some idea as to the required sizes of these members. Once these tentative sizes have been assigned, an exact analysis may be carried out.

CHAPTER EIGHT
C O N C L U S I O N S

This investigation was limited to the study of one building. Therefore, only some conclusions can be stipulated about buildings of the same nature. Details may be subject to some revision should more extensive cases be considered. The following conclusions seem to be indicated:

1. The problem of wind stresses in high buildings differ from that of low buildings in the relative stiffness of the beams and columns. In low buildings, the beams are normally stiff and the columns light and flexible, whereas in high buildings for office or resident use, the relative stiffness of the beams is smaller than that of the columns especially in the lower stories.

2. The Hardy Cross Method is an exact method of analysis. Its only disadvantage is the time required for the analysis.

3. The Factor Method applies mainly to low buildings, or else in the preliminary design of high buildings, and could be used for final design purposes, provided the analyst is sure that it will not mislead him as explained in the previous chapter. This method has the advantage of giving quick results.

4. The question of the establishment of the limits regarding the ratio of stiffness of members meeting at a joint is an important problem, because it serves as a guide to the application of the Factor Method which in my line of thinking, is quite a good method provided one knows when and where to apply it.

5. The question of symmetry of structures should be given further attention on the part of engineers because less computational labour is required. The author has the pleasure of being able to introduce some short-cuts regarding the use of symmetry in as far as the Factor Method is concerned.

6. As a result of the stimulus provided by the development of automatic digital computers, spectacular advances have been made during the last ten years in the field of structural analysis, both in theory of structural behavior and the techniques of numerical analysis. Analysis of complex structures, that could have been obtained only approximately and at the cost of tremendous computational effort a few years ago, may now be conducted exactly by routine application of standard computer programs.

7. The question of stiffness should be given further consideration on the part of engineers, because the calculation of the inertia of members on the basis of concrete section only is rather a poor assumption.

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pt. 2

ANALYSIS OF THE EFFECT OF WIND ON A HIGH REINFORCED
CONCRETE BUILDING

COMPARISON OF APPROXIMATE AND EXACT METHODS

BY

RIAD M. SHAHIN, B.ENG.

SUBMITTED TO THE SCHOOL OF ENGINEERING, AMERICAN
UNIVERSITY OF BEIRUT, IN PARTIAL FULFILMENT OF
REQUIREMENTS FOR THE DEGREE OF MASTER OF ENGINEERING
WITH MAJOR IN CIVIL ENGINEERING.

ADVISOR: DR. JACK NASSER

BEIRUT, LEBANON

DECEMBER, 1964

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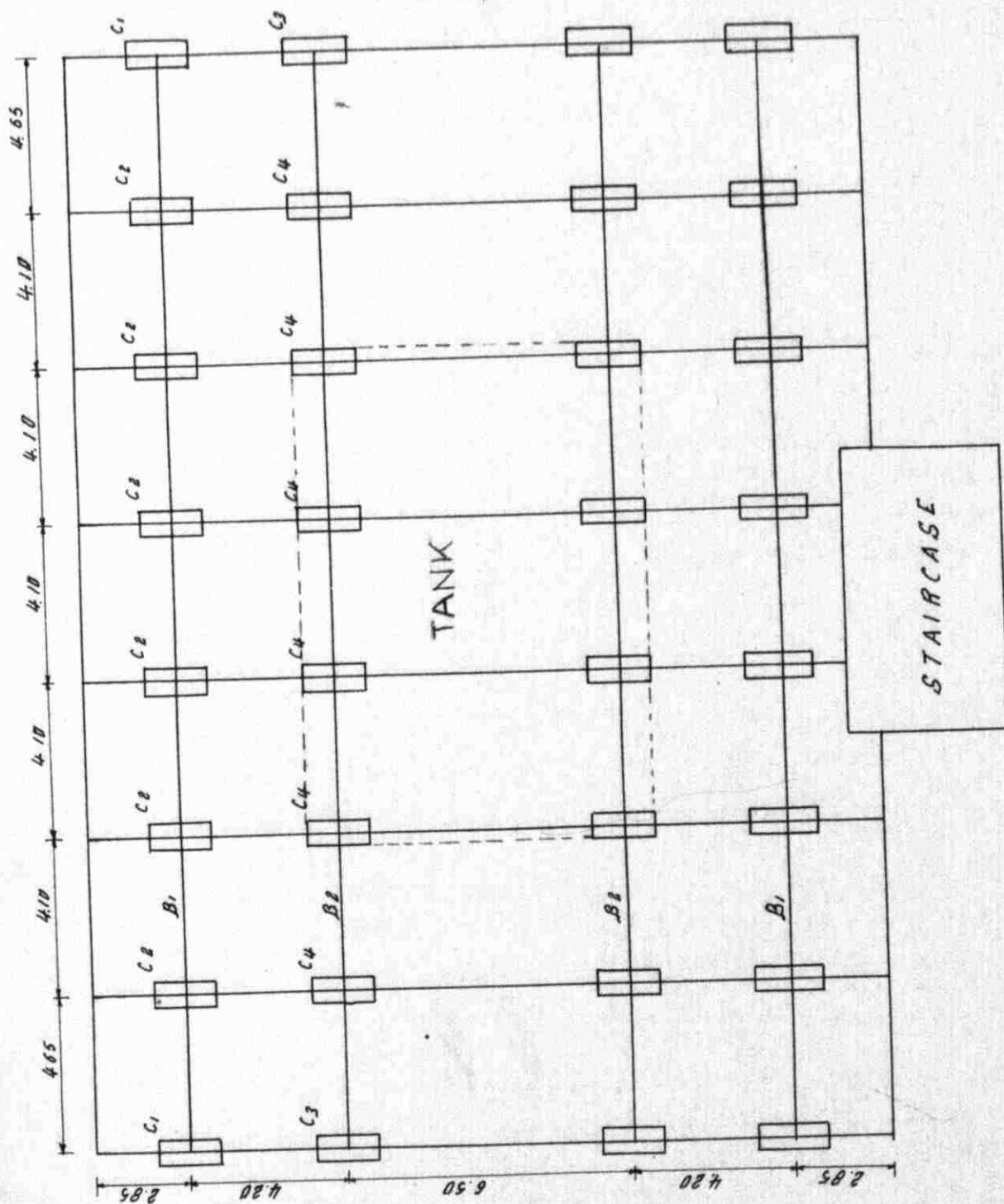
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NOTATIONS

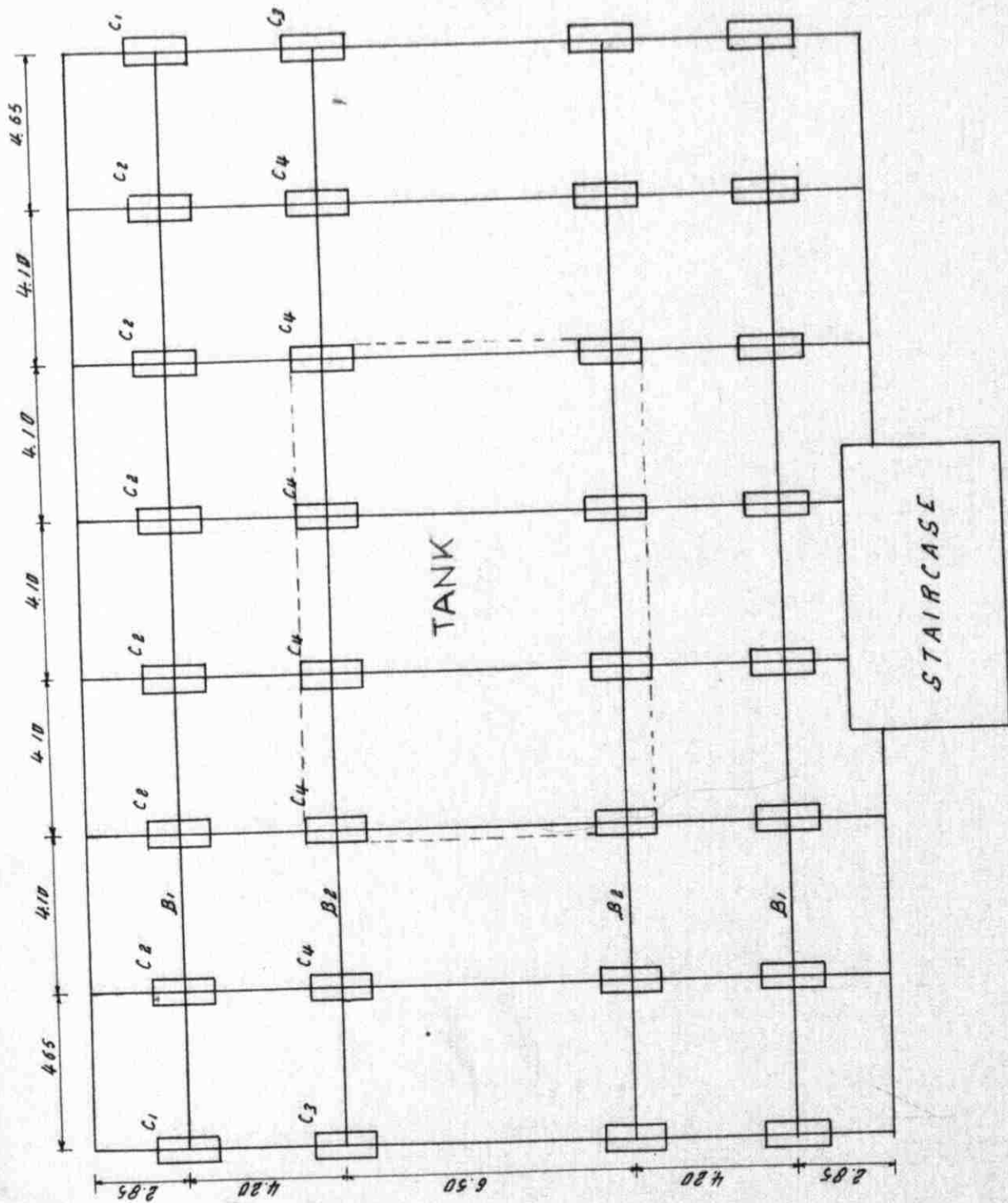
Unless otherwise specified, notations are as follows:

- A_s = Area of tensile reinforcement.
- A_s^c = Area of compression reinforcement.
- b = Width of rectangular beam and width of T-section beam.
- b' = Width of the T-section beam.
- d = Depth from centroid of tensile reinforcement to the compression face of the beam.
- D = Bar diameter.
- E = Modulus of elasticity.
- f'_c = Ultimate compression strength of concrete.
- f_s = Stress in tensile reinforcement.
- I = Moment of Inertia.
- kd = Depth from neutral axis to the compression face of the beam.
- M_c = Resisting Moment of Concrete
- n = Modular ratio.
- u = Unit bond stress.
- v = Unit shear stress
- w = Weight per unit length of the member.
- $\sum o$ = Perimeter of the bars.
- Δ = Deflection.
- I = Inferior Member at a joint.
- S = Superior Member at a joint.
- R = Right Member at a joint.
- L = Left Member at a joint.

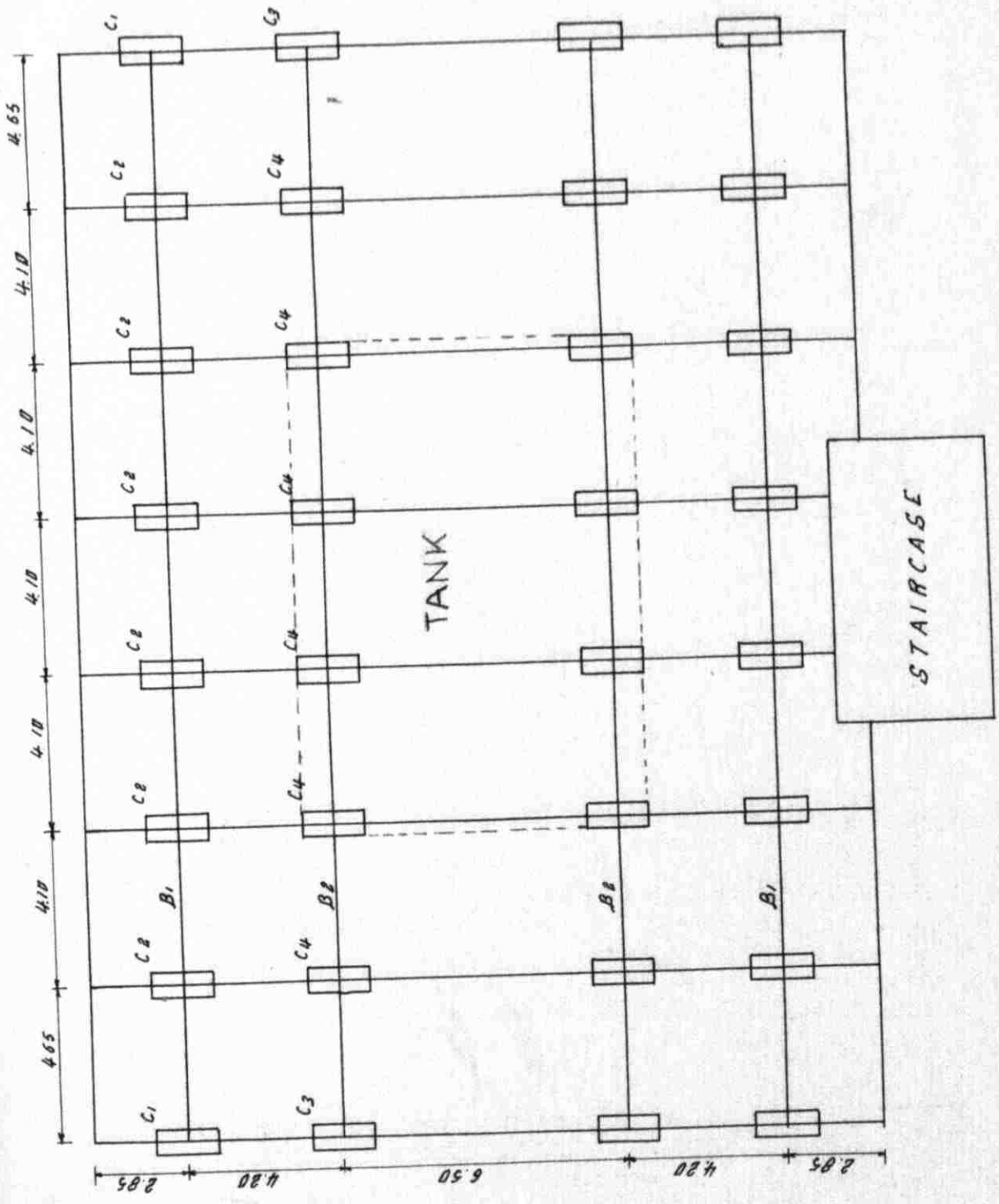
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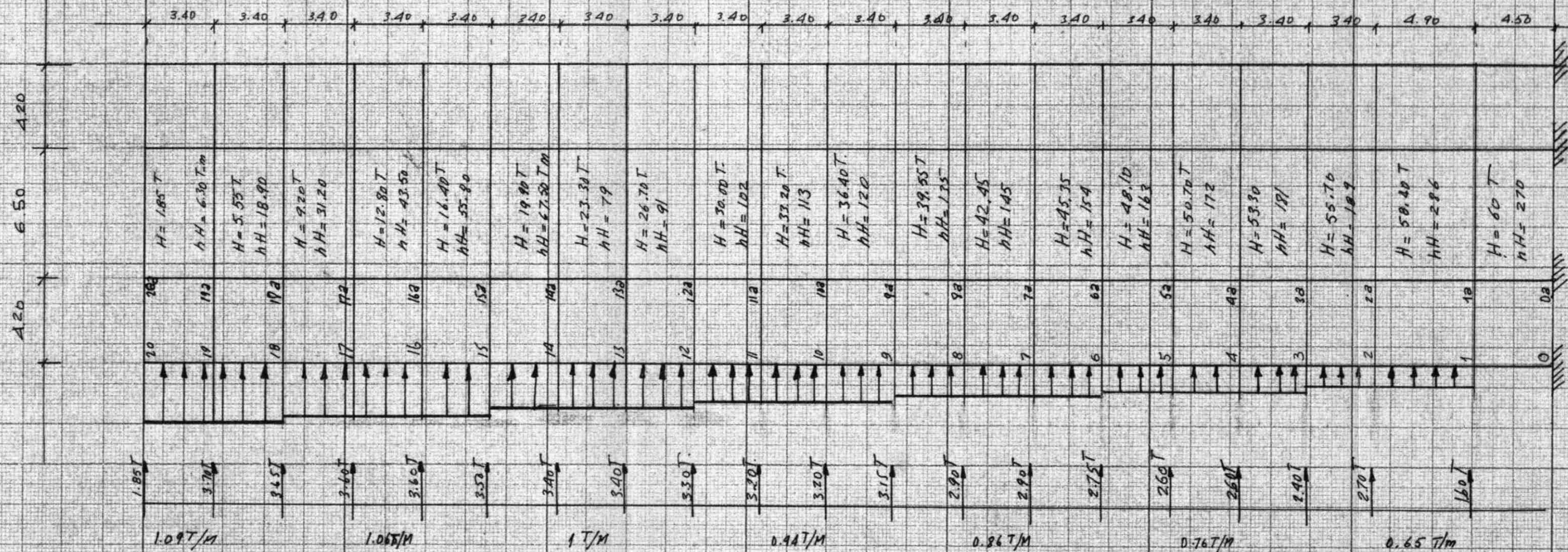
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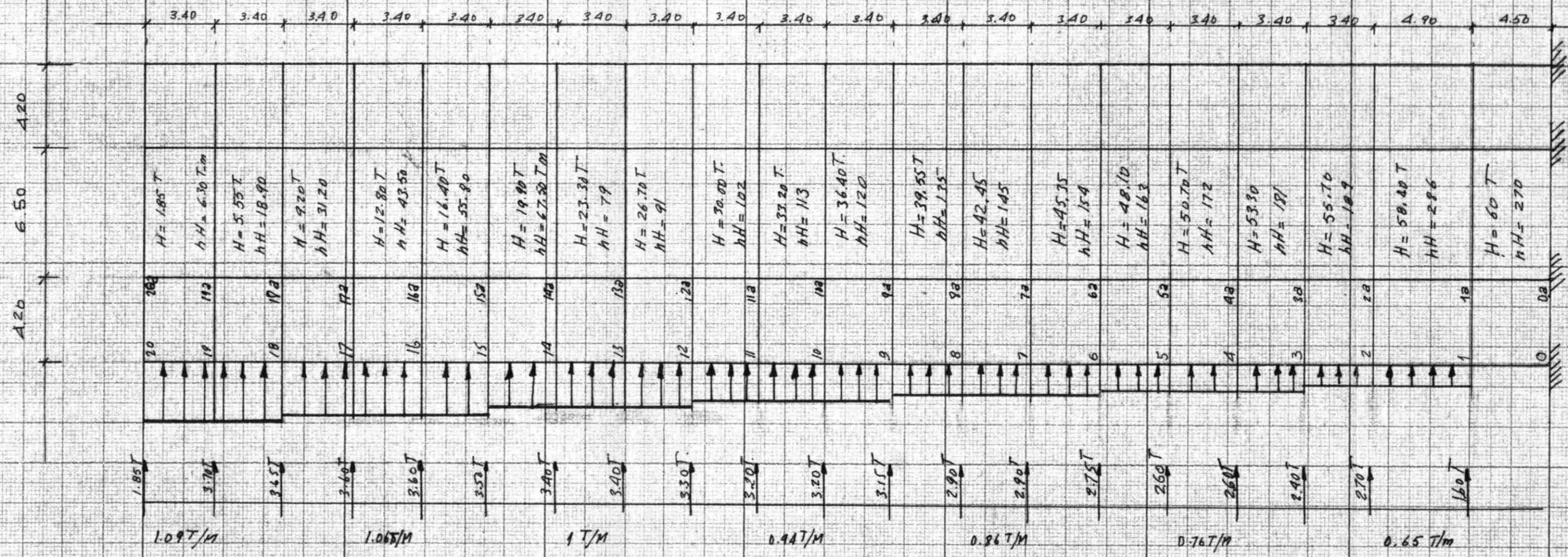
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N.B.: Total height = 70.60 meters

| | |
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| ANALYSIS OF THE EFFECT OF WIND ON A HIGH REINFORCED CONCRETE BUILDING | |
| Comparison of Approximate and Exact Methods | |
| COMPUTER : RIAD SHAHIN | WIND ANALYSIS |
| CHK'D BY : RIAD SHAHIN | PRESSURE DIAGRAM |
| APP'D BY : DR JACK NASSER | DATE : DECEMBER 1964 |
| | SHEET NO 2 / |

ET-1404



N.B.: Total height = 70.60 meters

ANALYSIS OF THE EFFECT OF WIND ON A HIGH REINFORCED CONCRETE BUILDING

Comparison of Approximate and Exact Methods

| | |
|---------------------------|----------------------|
| COMPUTER BY : RIAD SHAHIN | WIND ANALYSIS |
| CHK'D BY : RIAD SHAHIN | PRESSURE DIAGRAM |
| APP'D BY : DR JACK NASSER | DATE : DECEMBER 1964 |
| | SHEET NO 2 / |

CHAPTER ONE
WIND CALCULATIONS

Assume on exposed site conditions:

$$q = C_2 \cdot K_r \cdot K_s \cdot q_d$$

$$C_2 = 1.25$$

$$K_s = 1.20$$

$$\lambda = \frac{2S}{H} = \frac{2(h/2 \times b)}{H} = b$$

where b is the distance c-c of frames

$$\frac{H}{\sqrt{\lambda}} = \frac{66.10}{\sqrt{\frac{4.65+4.30}{2}}} = 30 \text{ m}$$

$$\therefore K_r = 1.36$$

$$q = 1.25 \times 1.36 \times 1.20 \cdot q_d = 2.00 \cdot q_d$$

Assume a wind velocity of 125 Km/hr.

$$\therefore V = \frac{125 \times 100}{3600} = 34.70 \text{ m/sec.}$$

$$q_d = \frac{34.70^2}{16} = 75 \text{ Kg/m}^2$$

$$q = 2.00 \times 75 = 150 \text{ Kg/m}^2$$

$$q = 150 \left(\frac{4.65+4.10}{2} \right) = 650 \text{ Kg/m}$$

$$\text{Height of structure above ground} = 3.40 \times 18 + 4.90 = 66.10 \text{ m}$$

Assume that the second and third floors to have $q_1 = 0.65 \text{ T/m}$, and change the intensity every third floor.

$$q_2 = \left(\frac{H+18}{H+60} \right) 2.50 w_1 = \left(\frac{H+18}{H+60} \right) 1.63$$

$$= 1.63 \left(\frac{18.50 + 18.00}{18.50 + 60} \right) = 1.63 \times \frac{36.50}{78.50} = 0.76 \text{ T/m}$$

$$q_3 = 1.63 \left(\frac{28.70 + 18.00}{28.70 + 60.00} \right) = 1.63 \times \frac{46.70}{88.70} = 0.86 \text{ T/m}$$

$$q_4 = 1.63 \left(\frac{38.90 + 18.00}{38.90 + 60.00} \right) = 1.63 \times \frac{56.90}{98.90} = 0.94 \text{ T/m}$$

$$q_5 = 1.63 \left(\frac{49.10 + 18.00}{49.10 + 60.00} \right) = 1.63 \times \frac{67.10}{109.10} = 1.00 \text{ T/m}$$

$$q_6 = 1.63 \left(\frac{59.30 + 18.00}{59.30 + 60.00} \right) = 1.63 \times \frac{77.30}{119.30} = 1.06 \text{ T/m}$$

$$q_7 = 1.63 \left(\frac{66.10 + 18.00}{66.10 + 60.00} \right) = 1.63 \times \frac{84.10}{126.10} = 1.09 \text{ T/m}$$

| | | | | | | | |
|------------|------|-------|-------|-------|-------|-------|------|
| w (T/m) | 0.65 | 0.76 | 0.86 | 0.94 | 1.00 | 1.06 | 1.09 |
| h (m) | 8.30 | 10.20 | 10.20 | 10.20 | 10.20 | 10.20 | 6.80 |
| P (T) | 5.40 | 7.80 | 8.80 | 9.60 | 10.20 | 10.80 | 7.40 |

$$\Sigma P = 60.00 \text{ T}$$

The above uniform loads should be changed to a system of concentrated loads acting on the joints

$$P_1 = 0.65 \times \frac{4.90}{2} = 1.60 \text{ T}$$

$$P_2 = 0.65 \times \frac{(4.90 + 3.40)}{2} = 2.70 \text{ T}$$

$$P_3 = (5.40 - 4.30) + 0.76 \times 1.70 = 2.40 \text{ T}$$

$$P_4 = P_5 = 0.76 \times 3.40 = 2.60 \text{ T}$$

$$P_6 = (7.80 - 6.50) + 0.86 \times 1.70 = 2.75 \text{ T}$$

$$P_7 = P_8 = 0.86 \times 3.40 = 2.90 \text{ T}$$

$$P_9 = (8.80 - 7.25) + 0.94 \times 1.70 = 3.15 \text{ T}$$

$$P_{10} = P_{11} = 1.60 \times 2 = 3.20 \text{ T}$$

$$P_{12} = (9.60 - 8.00) + 1 \times 1.70 = 3.30 \text{ T}$$

$$P_{13} = P_{14} = 3.40 \text{ T}$$

$$P_{15} = (10.20 - 8.50) + 1.06 \times 1.70 = 3.50 \text{ T}$$

$$P_{16} = P_{17} = 3.60 \text{ T}$$

$$P_{18} = (10.90 - 9.00) + 1.09 \times 1.70 = 3.65 \text{ T}$$

$$P_{19} = 1.85 \times 2 = 3.70 \text{ T}$$

$$P_{20} = 1.85 \text{ T}$$

CHAPTER TWO
FACTOR METHOD
CASE A

Introduction:

The analysis consists of:

1. Concealed beams of widths which vary every floor from 50 cms. up to 210 cms. Since the stiffness factor is a direct function of d^3 , all the beams have very small stiffness factors.

2. Bulky columns of dimensions varying every floor up to 50 x 200 cms., and hence of relatively very high stiffness factors.

This arrangement implies the use of economical percentages of intermediate grade steel for columns.

K Values For Beams

| Joint | Dimensions b x d (m x m) | $d^3/12$ | I (m ⁴) | K _{g1} (Absolute) | K _{g1} (Relative) | K _{g2} (Absolute) | K _{g2} (Relative) |
|-------|--------------------------------|----------|------------------------|-------------------------------|-------------------------------|-------------------------------|-------------------------------|
| 20 | 0.50 x 0.30 | 0.00225 | 0.00113 | 0.000270 | 2.70 | 0.000174 | 1.74 |
| 19 | " . " | " | " | " | " | " | " |
| 18 | " . " | " | " | " | " | " | " |
| 17 | " . " | " | " | " | " | " | " |
| 16 | 0.80 x 0.30 | " | 0.00135 | 0.000330 | 3.30 | 0.002000 | 2.00 |
| 15 | 0.70 x 0.30 | " | 0.00157 | 0.000372 | 3.72 | 0.002442 | 2.42 |
| 14 | 0.80 x 0.30 | " | 0.00180 | 0.000430 | 4.30 | 0.00278 | 2.78 |
| 13 | 0.90 x 0.30 | " | 0.00202 | 0.000480 | 4.80 | 0.00310 | 3.10 |
| 12 | 1.00 x 0.30 | " | 0.00225 | 0.000535 | 5.35 | 0.00346 | 3.46 |
| 11 | 1.20 x 0.30 | " | 0.00270 | 0.000642 | 6.42 | 0.00415 | 4.15 |
| 10 | 1.30 x 0.30 | " | 0.00293 | 0.000700 | 7.00 | 0.00450 | 4.50 |
| 9 | 1.40 x 0.30 | " | 0.00315 | 0.000750 | 7.50 | 0.00486 | 4.86 |
| 8 | 1.60 x 0.30 | " | 0.00360 | 0.000856 | 8.56 | 0.00550 | 5.50 |
| 7 | 1.70 x 0.30 | " | 0.00372 | 0.000890 | 8.90 | 0.00570 | 5.70 |
| 6 | 1.70 x 0.30 | " | 0.00372 | 0.000890 | 8.90 | 0.00570 | 5.70 |
| 5 | 1.80 x 0.30 | " | 0.00402 | 0.000970 | 9.70 | 0.00625 | 6.25 |
| 4 | 1.90 x 0.30 | " | 0.00430 | 0.001030 | 10.30 | 0.00662 | 6.62 |
| 3 | 2.00 x 0.30 | " | 0.00450 | 0.001070 | 10.70 | 0.00692 | 6.92 |
| 2 | 2.10 x 0.30 | " | 0.00472 | 0.001130 | 11.30 | 0.0073 | 7.30 |
| 1 | 2.10 x 0.30 | " | 0.00472 | 0.001130 | 11.30 | 0.00750 | 5.70 |

K Values For Columns

| Joint | Dimensions $b \times d$ (m x m) | d^3 (m^3) | I (m^4) | K (Absolute) | K Relative |
|-------|------------------------------------|--------------------|------------------|-------------------|-----------------|
| 20 | 0.50 x 0.20 | 0.008 | 0.00033 | 0.000097 | 0.97 |
| 19 | 0.50 x 0.20 | 0.008 | 0.00033 | 0.000097 | 0.97 |
| 18 | 0.50 x 0.30 | 0.027 | 0.00113 | 0.000333 | 3.33 |
| 17 | 0.50 x 0.45 | 0.092 | 0.00383 | 0.001130 | 11.30 |
| 16 | 0.50 x 0.55 | 0.166 | 0.00690 | 0.002030 | 20.30 |
| 15 | 0.50 x 0.65 | 0.275 | 0.01160 | 0.003380 | 33.80 |
| 14 | 0.50 x 0.75 | 0.420 | 0.01750 | 0.005150 | 51.50 |
| 13 | 0.50 x 0.85 | 0.620 | 0.02580 | 0.007600 | 76.00 |
| 12 | 0.50 x 0.95 | 0.860 | 0.03580 | 0.010500 | 105.00 |
| 11 | 0.50 x 1.10 | 1.330 | 0.05520 | 0.016200 | 162.00 |
| 10 | 0.50 x 1.20 | 1.720 | 0.07150 | 0.021000 | 210.00 |
| 9 | 0.50 x 1.30 | 2.200 | 0.09150 | 0.027000 | 270.00 |
| 8 | 0.50 x 1.45 | 3.050 | 0.1270 | 0.037300 | 373.00 |
| 7 | 0.50 x 1.55 | 3.720 | 0.15500 | 0.046000 | 460.00 |
| 6 | 0.50 x 1.65 | 4.500 | 0.18700 | 0.055000 | 550.00 |
| 5 | 0.50 x 1.80 | 5.800 | 0.24200 | 0.071000 | 710.00 |
| 4 | 0.50 x 2.00 | 8.000 | 0.33300 | 0.098000 | 980.00 |
| 3 | 0.50 x 2.00 | 8.000 | 0.33300 | 0.098000 | 980.00 |
| 2 | 0.50 x 2.00 | 8.000 | 0.33300 | 0.068000 | 680.00 |
| 1 | 0.50 x 2.00 | 8.000 | 0.33300 | 0.074000 | 740.00 |

Beam And Column Factors

| Joint | Kc | | ΣKc | ΣKg _i | ΣK | g-factor $\frac{\Sigma K_c}{\Sigma K}$ | c factor (1-g) |
|-------|--------|--------|---------|------------------|---------|---|-------------------|
| | I | S | | | | | |
| 20 | 0.97 | 0 | 0.97 | 2.70 | 3.67 | 0.265 | 0.735 |
| 19 | 0.97 | 0.97 | 3.67 | 2.70 | 4.64 | 0.418 | 0.582 |
| 18 | 3.33 | 0.97 | 4.30 | 2.70 | 7.00 | 0.615 | 0.385 |
| 17 | 11.30 | 3.33 | 14.63 | 2.70 | 17.33 | 0.855 | 0.145 |
| 16 | 20.30 | 11.30 | 31.60 | 3.20 | 34.80 | 0.905 | 0.095 |
| 15 | 33.80 | 20.30 | 54.10 | 3.72 | 57.82 | 0.935 | 0.065 |
| 14 | 51.50 | 33.80 | 85.30 | 4.30 | 89.60 | 0.950 | 0.050 |
| 13 | 76.00 | 51.50 | 127.50 | 4.80 | 132.30 | 0.960 | 0.040 |
| 12 | 105.00 | 76.00 | 181.00 | 5.35 | 186.35 | 0.970 | 0.030 |
| 11 | 162.00 | 105.00 | 267.00 | 6.42 | 273.42 | 0.972 | 0.028 |
| 10 | 210.00 | 162.00 | 372.00 | 7.00 | 379.00 | 0.980 | 0.020 |
| 9 | 270.00 | 210.00 | 480.00 | 7.50 | 489.50 | 0.984 | 0.016 |
| 8 | 373.00 | 270.00 | 643.00 | 8.56 | 651.56 | 0.986 | 0.014 |
| 7 | 460.00 | 373.00 | 833.00 | 8.90 | 841.90 | 0.988 | 0.012 |
| 6 | 550.00 | 460.00 | 1010.00 | 8.90 | 1018.90 | 0.990 | 0.010 |
| 5 | 710.00 | 550.00 | 1260.00 | 9.70 | 1269.70 | 0.992 | 0.008 |
| 4 | 980.00 | 710.00 | 1690.00 | 10.30 | 1700.30 | 0.992 | 0.008 |
| 3 | 980.00 | 980.00 | 1960.00 | 10.70 | 1970.70 | 0.992 | 0.008 |
| 2 | 680.00 | 980.00 | 1660.00 | 11.30 | 1671.30 | 0.992 | 0.008 |
| 1 | 740.00 | 680.00 | 1420.00 | 11.30 | 1431.30 | 0.992 | 0.008 |

| Joint (#) | Dimensions $b \times d$ (m x m) | d^3 (m ³) | I (m ⁴) | K Absolute | K Relative |
|--------------|------------------------------------|-------------------------|-----------------------|-----------------|-----------------|
| 20 | 0.50 x 0.20 | 0.0080 | 0.00033 | 0.000097 | 0.97 |
| 19 | 0.50 x 0.25 | 0.0157 | 0.00065 | 0.000192 | 1.92 |
| 18 | 0.50 x 0.35 | 0.0430 | 0.00179 | 0.005250 | 5.25 |
| 17 | 0.50 x 0.45 | 0.0920 | 0.00383 | 0.001130 | 11.30 |
| 16 | 0.50 x 0.55 | 0.1560 | 0.00690 | 0.002030 | 20.30 |
| 15 | 0.50 x 0.65 | 0.2750 | 0.0115 | 0.0033800 | 33.80 |
| 14 | 0.50 x 0.80 | 0.5100 | 0.02130 | 0.006300 | 63.00 |
| 13 | 0.50 x 0.90 | 0.7300 | 0.03030 | 0.008900 | 89.00 |
| 12 | 0.50 x 1.00 | 1.0000 | 0.04200 | 0.012300 | 123.00 |
| 11 | 0.50 x 1.10 | 1.3300 | 0.05500 | 0.016200 | 162.00 |
| 10 | 0.50 x 1.25 | 1.9500 | 0.08100 | 0.023800 | 238.00 |
| 9 | 0.50 x 1.35 | 2.4300 | 0.10100 | 0.029800 | 298.00 |
| 8 | 0.50 x 1.50 | 3.3500 | 0.14000 | 0.041200 | 412.00 |
| 7 | 0.50 x 1.60 | 4.1000 | 0.17000 | 0.050000 | 500.00 |
| 6 | 0.50 x 1.70 | 4.9000 | 0.20300 | 0.060000 | 600.00 |
| 5 | 0.50 x 1.85 | 6.3000 | 0.26200 | 0.077000 | 770.00 |
| 4 | 0.50 x 2.00 | 8.0000 | 0.33300 | 0.098000 | 980.00 |
| 3 | 0.50 x 2.00 | 8.0000 | 0.33300 | 0.098000 | 980.00 |
| 2 | 0.50 x 2.00 | 8.0000 | 0.33300 | 0.068000 | 680.00 |
| 1 | 0.50 x 2.00 | 8.0000 | 0.33300 | 0.07400 | 074.00 |

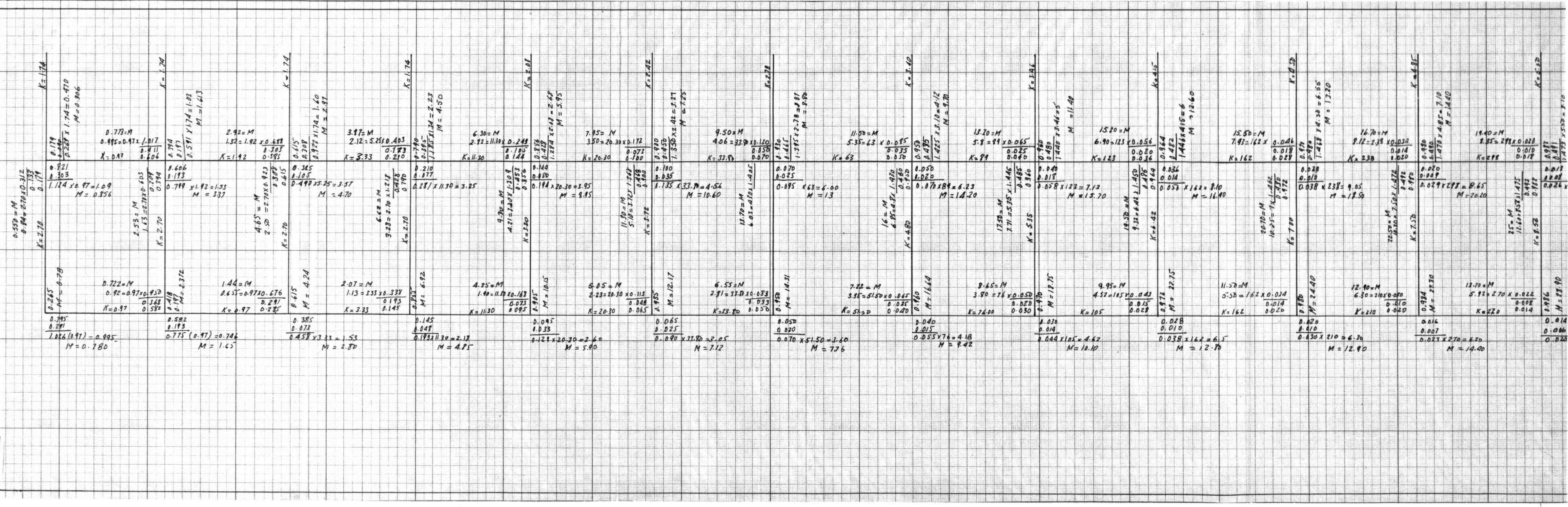
| Joint # | Kg | | ΣK_g | ΣK_c | ΣK | g-Factor $\frac{\Sigma K_c}{\Sigma K}$ | c-Factor (1-g) |
|---------|-------|------|--------------|--------------|------------|---|-------------------|
| | Kg1 | Kg2 | | | | | |
| 20 | 2.70 | 1.74 | 4.44 | 0.97 | 5.41 | 0.179 | 0.821 |
| 19 | " | " | " | 2.89 | 7.33 | 0.394 | 0.606 |
| 18 | " | " | " | 7.17 | 11.61 | 0.615 | 0.385 |
| 17 | " | " | " | 16.55 | 20.90 | 0.790 | 0.210 |
| 16 | 3.20 | 2.08 | 5.28 | 31.60 | 36.88 | 0.856 | 0.144 |
| 15 | 3.72 | 2.42 | 6.14 | 54.10 | 60.24 | 0.900 | 0.100 |
| 14 | 4.30 | 2.78 | 7.08 | 96.80 | 103.88 | 0.930 | 0.070 |
| 13 | 4.80 | 3.10 | 7.90 | 152.00 | 159.90 | 0.950 | 0.050 |
| 12 | 5.35 | 3.46 | 8.81 | 212.00 | 220.81 | 0.960 | 0.040 |
| 11 | 6.42 | 4.15 | 10.57 | 285.00 | 295.57 | 0.964 | 0.036 |
| 10 | 7.00 | 4.50 | 11.50 | 400.00 | 411.50 | 0.972 | 0.028 |
| 9 | 7.50 | 4.85 | 12.35 | 536.00 | 548.35 | 0.980 | 0.020 |
| 8 | 8.56 | 5.50 | 14.06 | 710.00 | 724.06 | 0.982 | 0.018 |
| 7 | 8.90 | 5.70 | 14.60 | 912.00 | 926.60 | 0.984 | 0.016 |
| 6 | 8.90 | 5.70 | 14.60 | 1100.00 | 1124.60 | 0.988 | 0.012 |
| 5 | 9.70 | 5.70 | 15.40 | 1370.00 | 1385.95 | 0.990 | 0.010 |
| 4 | 10.30 | 6.62 | 16.92 | 1750.00 | 1766.92 | 0.990 | 0.010 |
| 3 | 10.70 | 6.92 | 17.62 | 1960.00 | 1977.62 | " " | " " |
| 2 | 11.30 | 7.30 | 18.60 | 1660.00 | 1678.60 | " " | " " |
| 1 | 11.30 | 7.30 | 18.60 | 1420.00 | 1438.60 | " " | " " |

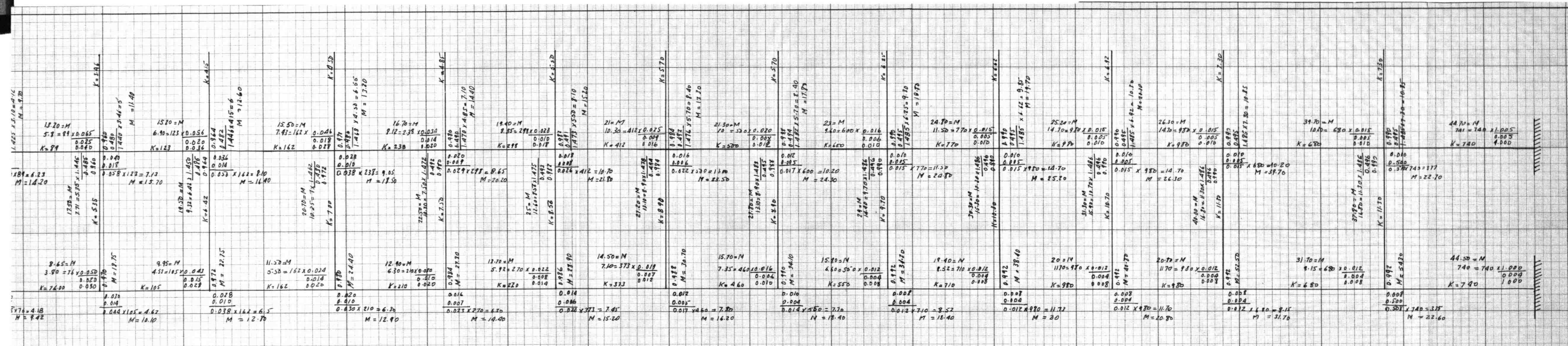
A Factors

| | | | |
|----------|---|--------------------------|------------|
| A_{20} | $= \frac{6.30}{2(1.090 + 0.985 + 0.995 + 0.920)}$ | $= \frac{3.15}{3.99}$ | $= 0.786$ |
| A_{19} | $= \frac{18.90}{2(1.530 + 0.746 + 1.320 + 0.655)}$ | $= \frac{9.45}{4.251}$ | $= 2.22$ |
| A_{18} | $= \frac{31.20}{2(2.570 + 1.53 + 2.12 + 2.210)}$ | $= \frac{15.60}{8.43}$ | $= 1.83$ |
| A_{17} | $= \frac{43.50}{2(2.82 + 3.25 + 1.90 + 2.18)}$ | $= \frac{21.75}{10.15}$ | $= 2.23$ |
| A_{16} | $= \frac{55.80}{2(3.50 + 3.95 + 2.23 + 2.60)}$ | $= \frac{27.90}{12.28}$ | $= 2.27$ |
| A_{15} | $= \frac{67.50}{2(4.06 + 4.56 + 2.81 + 3.05)}$ | $= \frac{33.75}{14.48}$ | $= 2.33$ |
| A_{14} | $= \frac{79}{2(5.35 + 6.00 + 3.35 + 3.60)}$ | $= \frac{39.50}{18.30}$ | $= 2.17$ |
| A_{13} | $= \frac{91}{2(5.80 + 6.23 + 3.80 + 4.18)}$ | $= \frac{45.50}{20.01}$ | $= 22.75$ |
| A_{12} | $= \frac{102}{2(6.90 + 7.13 + 4.52 + 4.62)}$ | $= \frac{51}{23.17}$ | $= 2.20$ |
| A_{11} | $= \frac{113}{2(7.43 + 8.10 + 5.50 + 6.15)}$ | $= \frac{56.50}{27.18}$ | $= 2.08$ |
| A_{10} | $= \frac{120}{2(8.12 + 9.05 + 6.30 + 6.30)}$ | $= \frac{60}{29.23}$ | $= 2.05$ |
| A_9 | $= \frac{135}{2(8.35 + 8.65 + 5.92 + 6.20)}$ | $= \frac{67.50}{29.12}$ | $= 2.32$ |
| A_8 | $= \frac{145}{2(10.30 + 10.70 + 7.10 + 7.45)}$ | $= \frac{72.50}{33.55}$ | $= 2.04$ |
| A_7 | $= \frac{154}{2(10 + 10.70 + 7.10 + 7.45)}$ | $= \frac{77}{36.15}$ | $= 2.13$ |
| A_6 | $= \frac{163}{2(9.60 + 10.20 + 6.60 + 7.70)}$ | $= \frac{81.50}{34.10}$ | $= 2.39$ |
| A_5 | $= \frac{172.00}{2(11.50 + 11.50 + 8.52 + 8.52)}$ | $= \frac{86}{40.04}$ | $= 2.15$ |
| A_4 | $= \frac{181.00}{2(14.70 + 14.70 + 11.70 + 11.70)}$ | $= \frac{90.50}{52.80}$ | $= 1.72$ |
| A_3 | $= \frac{189.00}{2(14.70 + 14.70 + 11.70 + 11.70)}$ | $= \frac{94.50}{52.80}$ | $= 1.79$ |
| A_2 | $= \frac{286.00}{2(10.20 + 8.15 + 8.15 + 8.15)}$ | $= \frac{143.00}{36.70}$ | $= 3.90$ |
| A_1 | $= \frac{270.00}{2(741 + 377 + 740 + 375)}$ | $= \frac{135.00}{2233}$ | $= 0.0603$ |

B Factors

| | | |
|-----------|---|---------------------------------|
| B_{20a} | $= \frac{0.856}{0.84 + 0.47}$ | $= \frac{0.856}{0.131} = 0.653$ |
| B_{19a} | $= \frac{0.773 + 3.370}{1.63 + 1.03}$ | $= \frac{4.143}{2.66} = 1.56$ |
| B_{18a} | $= \frac{2.92 + 4.70}{2.50 + 1.60}$ | $= \frac{7.62}{4.10} = 1.86$ |
| B_{17a} | $= \frac{7.25 + 3.87}{3.28 + 2.23}$ | $= \frac{11.12}{5.51} = 2.02$ |
| B_{16a} | $= \frac{6.30 + 8.95}{4.21 + 2.68}$ | $= \frac{15.25}{6.89} = 2.22$ |
| B_{15a} | $= \frac{10.60 + 7.95}{5.10 + 3.27}$ | $= \frac{18.55}{8.37} = 2.22$ |
| B_{14a} | $= \frac{13.00 + 9.50}{6.03 + 3.87}$ | $= \frac{22.50}{9.90} = 2.27$ |
| B_{13a} | $= \frac{14.20 + 11.50}{6.85 + 4.12}$ | $= \frac{25.70}{10.97} = 2.33$ |
| B_{12a} | $= \frac{15.70 + 13.80}{7.71 + 5.00}$ | $= \frac{29.50}{12.71} = 2.28$ |
| B_{11a} | $= \frac{16.90 + 15.20}{9.32 + 6.00}$ | $= \frac{32.10}{15.32} = 2.09$ |
| B_{10a} | $= \frac{18.50 + 15.50}{10.25 + 6.55}$ | $= \frac{34.00}{16.80} = 2.02$ |
| B_{9a} | $= \frac{16.70 + 20.20}{10.30 + 6.60}$ | $= \frac{36.90}{16.90} = 2.18$ |
| B_{8a} | $= \frac{19.40 + 21.80}{10.30 + 6.60}$ | $= \frac{41.20}{16.90} = 2.43$ |
| B_{7a} | $= \frac{21.00 + 23.50}{13.00 + 8.40}$ | $= \frac{44.50}{21.50} = 2.07$ |
| B_{6a} | $= \frac{21.30 + 24.30}{13.10 + 8.40}$ | $= \frac{47.60}{23.70} = 2.12$ |
| B_{5a} | $= \frac{23.00 + 24.80}{14.40 + 9.30}$ | $= \frac{47.80}{23.70} = 2.02$ |
| B_{4a} | $= \frac{24.80 + 25.20}{15.30 + 9.85}$ | $= \frac{50.00}{25.15} = 1.99$ |
| B_{3a} | $= \frac{25.20 + 26.30}{15.90 + 10.30}$ | $= \frac{51.50}{26.20} = 1.97$ |
| B_{2a} | $= \frac{26.30 + 39.70}{16.80 + 10.85}$ | $= \frac{66.00}{27.65} = 2.38$ |
| B_{1a} | $= \frac{39.70 + 22.70}{16.80 + 10.85}$ | $= \frac{62.40}{27.65} = 2.26$ |





| | | | |
|---|----------------------------|---------------------|--------------|
| ANALYSIS OF THE EFFECT OF WIND ON A HIGH REINFORCED CONCRETE BUILDING | | | |
| Comparison of Approximate and Exact Methods | | | |
| COMPUTER | RIAD SHAMIN | | |
| CHK'D BY | RIAD SHAMIN | FACTOR METHOD | |
| APP'D BY | D ^r JACK NASSER | DATE: DECEMBER 1964 | SHEET NO 14/ |

CASE B

Introduction:

The analysis consists of:

1. Same column dimensions as in previous case.
2. Drop beams of constant widths of 30 cms., and varying depths every fourth floor as such 50, 60, 70, 80, and 90 cms. ?

The stiffness^{of beams} is about four times as much as the previous case.

K Values For Beams

| Joint | Dimensions b x d (m x m) | d^3 (m^3) | $b/12$ (m) | I (m^4) | Kg_1 (Absolute) | Kg_2 (Absolute) | Kg_1 (Relative) | Kg_2 (Relative) |
|-------|--------------------------------|--------------------|---------------|------------------|----------------------|----------------------|----------------------|----------------------|
| 20-17 | 0.30 x 0.50 | 0.125 | 0.025 | 0.00312 | 0.00074 | 0.00048 | 7.40 | 4.80 |
| 16-13 | 0.30 x 0.60 | 0.216 | 0.025 | 0.00540 | 0.00128 | 0.00083 | 12.80 | 8.30 |
| 12-9 | 0.30 x 0.70 | 0.343 | 0.025 | 0.00855 | 0.00203 | 0.00131 | 20.30 | 13.10 |
| 8-5 | 0.30 x 0.80 | 0.512 | 0.025 | 0.01280 | 0.00305 | 0.00196 | 30.50 | 19.60 |
| 4-1 | 0.30 x 0.90 | 0.729 | 0.025 | 0.0182 | 0.00432 | 0.00280 | 43.20 | 28.00 |

Beam And Column Factors

| Joint | ΣK_c | K_{g1} | ΣK | g factor $\frac{\Sigma K_c}{\Sigma K}$ | c Factor (1-g) |
|-------|--------------|----------|------------|---|---------------------|
| 20 | 0.97 | 7.40 | 8.37 | 0.116 | 0.884 |
| 19 | 3.67 | " | 9.34 | 0.206 | 0.794 |
| 18 | 4.30 | " | 11.70 | 0.366 | 0.634 |
| 17 | 14.63 | " | 21.93 | 0.662 | 0.338 |
| 16 | 31.60 | 12.80 | 44.30 | 0.710 | 0.290 |
| 15 | 54.10 | " | 66.90 | 0.810 | 0.190 |
| 14 | 85.30 | " | 98.10 | 0.870 | 0.130 |
| 13 | 127.50 | " | 139.30 | 0.910 | 0.090 |
| 12 | 181.00 | 20.30 | 200.30 | 0.900 | 0.100 |
| 11 | 267.00 | " | 287.30 | 0.930 | 0.070 |
| 10 | 372.00 | " | 392.30 | 0.950 | 0.050 |
| 9 | 480.00 | " | 496.30 | 0.960 | 0.040 |
| 8 | 643.00 | 30.50 | 669.50 | 0.940 | 0.060 |
| 7 | 833.00 | " | 863.50 | 0.966 | 0.034 |
| 6 | 1010.00 | " | 1040.50 | 0.970 | 0.030 |
| 5 | 1260.00 | " | 1280.50 | 0.974 | 0.026 |
| 4 | 1690.00 | 43.20 | 1723.20 | 0.960 | 0.040 |
| 3 | 1860.00 | " | 2003.20 | 0.980 | 0.020 |
| 2 | 1660.00 | " | 1703.20 | 0.974 | 0.026 |
| 1 | 1420.00 | " | 1463.20 | 0.970 | 0.030 |

A Factors

| | | | | | | |
|-----------------|---|--|---|-------------------------|---|-------|
| A ₂₀ | = | $\frac{315}{1.23 + 1.29 + 1.19 + 1.24}$ | = | $\frac{3.15}{4.95}$ | = | 0.636 |
| A ₁₉ | = | $\frac{9.45}{1.98 + 2.15 + 1.00 + 1.07}$ | = | $\frac{9.45}{6.20}$ | = | 1.53 |
| A ₁₈ | = | $\frac{15.60}{3.85 + 4.40 + 2.18 + 2.67}$ | = | $\frac{15.60}{13.10}$ | = | 1.19 |
| A ₁₇ | = | $\frac{21.75}{6.88 + 6.92 + 5.13 + 5.40}$ | = | $\frac{21.75}{24.27}$ | = | 0.895 |
| A ₁₆ | = | $\frac{27.90}{9.75 + 11.00 + 6.80 + 7.80}$ | = | $\frac{27.90}{35.35}$ | = | 0.79 |
| A ₁₅ | = | $\frac{33.75}{10.80 + 12.50 + 7.60 + 8.60}$ | = | $\frac{33.75}{39.50}$ | = | 0.854 |
| A ₁₄ | = | $\frac{39.50}{13.20 + 15.10 + 8.00 + 9.00}$ | = | $\frac{39.50}{45.30}$ | = | 0.870 |
| A ₁₃ | = | $\frac{45.50}{17.60 + 16.70 + 10.90 + 10.50}$ | = | $\frac{45.50}{55.70}$ | = | 0.817 |
| A ₁₂ | = | $\frac{51}{21.80 + 23.80 + 12.60 + 14.80}$ | = | $\frac{51}{72.40}$ | = | 0.702 |
| A ₁₁ | = | $\frac{56.50}{21.80 + 24.80 + 18.70 + 15.90}$ | = | $\frac{56.50}{75.60}$ | = | 0.748 |
| A ₁₀ | = | $\frac{60}{23.80 + 26.20 + 13.60 + 14.70}$ | = | $\frac{60}{78.30}$ | = | 0.768 |
| A ₉ | = | $\frac{67.50}{28.70 + 27.60 + 21.20 + 18.50}$ | = | $\frac{67.50}{96.00}$ | = | 0.702 |
| A ₈ | = | $\frac{72.50}{36.20 + 39.00 + 23.80 + 28.70}$ | = | $\frac{72.50}{127.70}$ | = | 0.57 |
| A ₇ | = | $\frac{77}{36.50 + 38.00 + 21.70 + 22.60}$ | = | $\frac{77}{119.30}$ | = | 0.645 |
| A ₆ | = | $\frac{81.50}{37.80 + 39.60 + 22.50 + 23.70}$ | = | $\frac{81.50}{123.60}$ | = | 0.660 |
| A ₅ | = | $\frac{86}{45.30 + 45.30 + 37.00 + 32.30}$ | = | $\frac{86}{159.80}$ | = | 0.54 |
| A ₄ | = | $\frac{90.50}{57.50 + 57.80 + 39.20 + 49.00}$ | = | $\frac{90.50}{203.00}$ | = | 0.455 |
| A ₃ | = | $\frac{94.50}{57.80 + 57.00 + 37.20 + 38.30}$ | = | $\frac{94.50}{184.30}$ | = | 0.518 |
| A ₂ | = | $\frac{143.00}{47.50 + 44.00 + 29.20 + 27.80}$ | = | $\frac{143.00}{148.50}$ | = | 0.960 |
| A ₁ | = | $\frac{135.00}{75.8 + 40.6 + 75.0 + 39.2}$ | = | $\frac{135.00}{230.0}$ | = | 0.587 |

B Factors

| | | | | |
|---|---|------------------------|---|-------|
| $B_{20a} = \frac{0.88}{0.98 + 0.53}$ | = | $\frac{0.88}{1.51}$ | = | 0.542 |
| $B_{19a} = \frac{0.78 + 3.40}{2.18 + 1.48}$ | = | $\frac{4.18}{3.66}$ | = | 1.14 |
| $B_{18a} = \frac{3.03 + 5.52}{4.10 + 2.66}$ | = | $\frac{8.53}{6.76}$ | = | 1.26 |
| $B_{17a} = \frac{4.57 + 6.20}{6.72 + 4.17}$ | = | $\frac{10.77}{10.89}$ | = | 0.99 |
| $B_{16a} = \frac{6.10 + 8.65}{12.20 + 7.42}$ | = | $\frac{14.75}{19.62}$ | = | 0.75 |
| $B_{15a} = \frac{7.70 + 10.70}{14.40 + 8.95}$ | = | $\frac{18.40}{23.35}$ | = | 0.79 |
| $B_{14a} = \frac{9.25 + 13.10}{16.00 + 10.20}$ | = | $\frac{22.35}{26.20}$ | = | 0.855 |
| $B_{13a} = \frac{11.50 + 13.60}{17.00 + 12.90}$ | = | $\frac{25.10}{29.90}$ | = | 0.836 |
| $B_{12a} = \frac{14.30 + 16.70}{26.70 + 16.90}$ | = | $\frac{31.00}{43.60}$ | = | 0.710 |
| $B_{11a} = \frac{15.30 + 18.50}{27.50 + 17.50}$ | = | $\frac{33.80}{45.00}$ | = | 0.750 |
| $B_{10a} = \frac{16.30 + 20.00}{28.30 + 18.10}$ | = | $\frac{36.30}{46.40}$ | = | 0.785 |
| $B_{9a} = \frac{18.10 + 19.40}{28.80 + 18.50}$ | = | $\frac{37.50}{47.30}$ | = | 0.79 |
| $B_{8a} = \frac{20.20 + 22.20}{42.70 + 27.40}$ | = | $\frac{42.40}{70.10}$ | = | 0.602 |
| $B_{7a} = \frac{20.60 + 24.80}{43.50 + 27.70}$ | = | $\frac{45.40}{71.20}$ | = | 0.637 |
| $B_{6a} = \frac{23.50 + 26.20}{43.80 + 28.00}$ | = | $\frac{49.70}{71.80}$ | = | 0.692 |
| $B_{5a} = \frac{25 + 24.50}{44.20 + 28.20}$ | = | $\frac{49.50}{72.40}$ | = | 0.682 |
| $B_{4a} = \frac{24.50 + 26.20}{62.00 + 41.00}$ | = | $\frac{50.70}{103}$ | = | 0.49 |
| $B_{3a} = \frac{25.80 + 29.20}{62.50 + 41.00}$ | = | $\frac{55.00}{103.50}$ | = | 0.532 |
| $B_{2a} = \frac{29.60 + 42.20}{62.10 + 41}$ | = | $\frac{71.80}{103.10}$ | = | 0.700 |
| $B_{1a} = \frac{45.50 + 26.80}{61.80 + 40.60}$ | = | $\frac{72.30}{102.40}$ | = | 0.710 |

| | | | | | | | | | | | | | | | | | | | |
|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|
| $M = 10.70$ | $M = 13.60$ | $M = 17.50$ | $M = 18.50$ | $M = 19.60$ | $M = 22.20$ | $M = 24.80$ | $M = 26.20$ | $M = 27.60$ | $M = 28.80$ | $M = 30.50$ | $M = 32.80$ | $M = 34.40$ | $M = 37.00$ | $M = 40.60$ | $M = 42.20$ | $M = 44.00$ | $M = 46.00$ | $M = 49.70$ | $M = 50.00$ |
| $K = 88$ | $K = 123$ | $K = 162$ | $K = 203.0$ | $K = 238$ | $K = 293$ | $K = 373$ | $K = 412$ | $K = 466$ | $K = 520$ | $K = 570$ | $K = 602$ | $K = 756$ | $K = 980$ | $K = 980$ | $K = 670$ | $K = 4320$ | $K = 4320$ | $K = 740$ | $K = 740$ |
| $M = 14.30$ | $M = 15.30$ | $M = 16.30$ | $M = 17.30$ | $M = 18.30$ | $M = 19.30$ | $M = 20.30$ | $M = 21.30$ | $M = 22.30$ | $M = 23.30$ | $M = 24.30$ | $M = 25.30$ | $M = 26.30$ | $M = 27.30$ | $M = 28.30$ | $M = 29.30$ | $M = 30.30$ | $M = 31.30$ | $M = 32.30$ | $M = 33.30$ |
| $M = 17.60$ | $M = 21.80$ | $M = 21.80$ | $M = 22.80$ | $M = 23.80$ | $M = 24.80$ | $M = 25.80$ | $M = 26.80$ | $M = 27.80$ | $M = 28.80$ | $M = 29.80$ | $M = 30.80$ | $M = 31.80$ | $M = 32.80$ | $M = 33.80$ | $M = 34.80$ | $M = 35.80$ | $M = 36.80$ | $M = 37.80$ | $M = 38.80$ |
| $M = 19.00$ | $M = 20.60$ | $M = 22.10$ | $M = 23.30$ | $M = 24.70$ | $M = 25.90$ | $M = 27.10$ | $M = 28.30$ | $M = 29.50$ | $M = 30.70$ | $M = 31.90$ | $M = 33.10$ | $M = 34.30$ | $M = 35.50$ | $M = 36.70$ | $M = 37.90$ | $M = 39.10$ | $M = 40.30$ | $M = 41.50$ | $M = 42.70$ |
| $M = 8.90$ | $M = 8.90$ | $M = 10.20$ | $M = 13.70$ | $M = 14.30$ | $M = 14.90$ | $M = 15.60$ | $M = 16.30$ | $M = 17.00$ | $M = 17.70$ | $M = 18.40$ | $M = 19.10$ | $M = 19.80$ | $M = 20.50$ | $M = 21.20$ | $M = 21.90$ | $M = 22.60$ | $M = 23.30$ | $M = 24.00$ | $M = 24.70$ |
| $M = 10.50$ | $M = 14.20$ | $M = 15.80$ | $M = 19.70$ | $M = 21.00$ | $M = 22.60$ | $M = 24.70$ | $M = 26.60$ | $M = 28.70$ | $M = 30.50$ | $M = 32.80$ | $M = 35.00$ | $M = 37.50$ | $M = 40.00$ | $M = 42.50$ | $M = 45.00$ | $M = 47.50$ | $M = 50.00$ | $M = 52.50$ | $M = 55.00$ |
| $M = 8.55$ | $M = 9.95$ | $M = 11.40$ | $M = 14.70$ | $M = 18.30$ | $M = 21.20$ | $M = 24.70$ | $M = 28.60$ | $M = 32.70$ | $M = 37.00$ | $M = 41.60$ | $M = 46.50$ | $M = 51.60$ | $M = 57.00$ | $M = 62.60$ | $M = 68.30$ | $M = 74.10$ | $M = 80.00$ | $M = 86.00$ | $M = 92.00$ |

ANALYSIS OF THE EFFECT OF WIND ON A HIGH REINFORCED CONCRETE BUILDING
 Comparison of Approximate and Exact Methods

COMPUTER : RIAD SHAHIN
 CHK'D BY : RIAD SHAHIN
 APP'D BY : D JACK NASSER

FACTOR METHOD
 DATE : DECEMBER 1964 SHEET NO 21

CASE C (1)

Introduction:

The analysis consists of:

1. Artificial T-beams whereby the flanges are provided merely to furnish sufficient area in compression and hence to improve the stiffness of the beams. The effective overhanging width will be assumed constant for all beams and taken as 50 cms. The depths of the beams will be changed every four floors as such 60, 70, 80, 90 and 100 cms.

2. Column sizes which have been reduced almost to half, resulting in values for stiffness which fall in the same order of the beams.

This arrangement implies the:

1. Use of high strength steel with an $f_s = 2,100 \text{ Kg/cm}^2 = 21,000 \text{ T/m}^2$.
2. Use of maximum allowable percentage of steel for the columns.

(1) For dimensions of members refer to Chapter 3, Case C.

Beam And Column Factors

| Joint | K_c | | ΣK_c | K_{g_c} | ΣK | g factor $\frac{\Sigma K_c}{\Sigma K}$ | c. Factor (1-g) |
|----------|--------|--------|--------------|-----------|------------|---|--------------------|
| | I | S | | | | | |
| 20 | 7.70 | 0 | 7.70 | 24.00 | 31.70 | 0.242 | 0.758 |
| 19-18-17 | -7.70 | 7.70 | 15.40 | 24.00 | 39.40 | 0.390 | 0.610 |
| 16 | 26.40 | 7.70 | 34.10 | 37.30 | 71.40 | 0.476 | 0.524 |
| 15-14-13 | 26.40 | 26.40 | 52.80 | 37.30 | 90.10 | 0.586 | 0.414 |
| 12 | 62.50 | 26.40 | 88.90 | 55.80 | 144.70 | 0.612 | 0.388 |
| 11-10-9 | 62.50 | 62.50 | 125.00 | 55.80 | 180.80 | 0.690 | 0.310 |
| 8 | 122.00 | 62.50 | 184.50 | 79.00 | 263.50 | 0.700 | 0.300 |
| 7-6-5 | 122.00 | 122.00 | 244.50 | 79.00 | 323.00 | 0.756 | 0.244 |
| 4 | 211.00 | 122.00 | 333.00 | 108.00 | 441.00 | 0.756 | 0.244 |
| 3 | 211.00 | 211.00 | 422.00 | 108.00 | 530.00 | 0.796 | 0.204 |
| 2 | 147.00 | 211.00 | 358.00 | 108.00 | 466.00 | 0.766 | 0.234 |
| 1 | 160.00 | 147.00 | 307.00 | 108.00 | 415.00 | 0.740 | 0.260 |

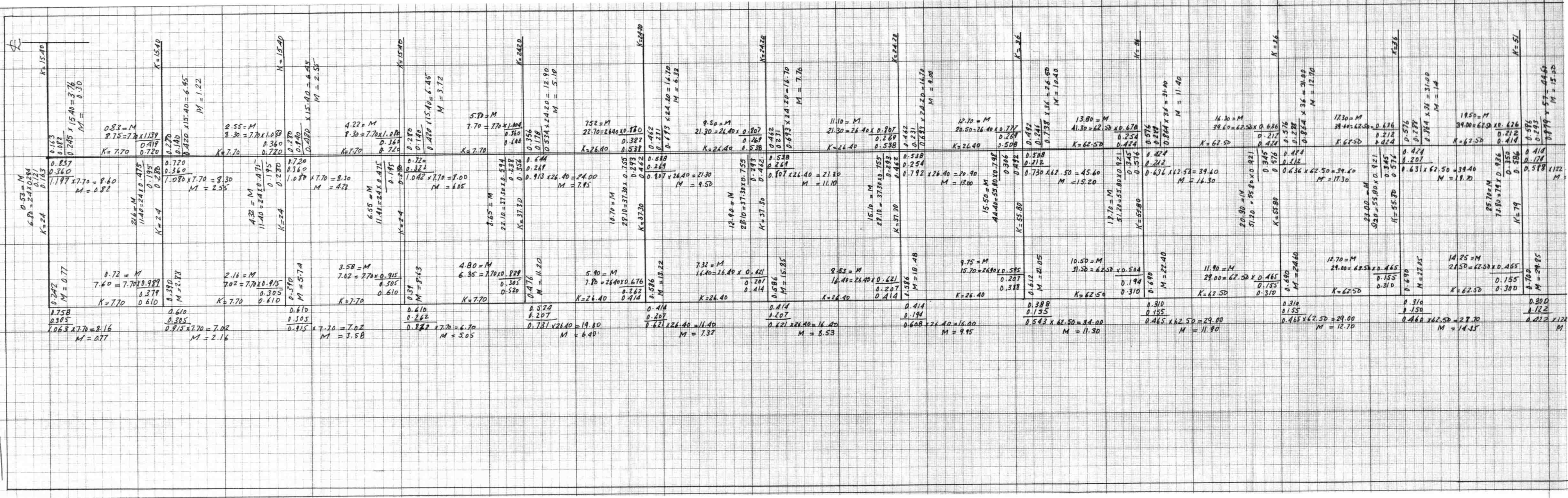
| Joint a | Kg | | ΣK_g | ΣK_c | ΣK | g. Factor $\frac{\Sigma K_c}{\Sigma K}$ | c. Factor (1-g) |
|------------|-----------------|-----------------|--------------|--------------|------------|--|--------------------|
| | Kg ₁ | Kg ₂ | | | | | |
| 20 | 24.00 | 15.40 | 39.40 | 7.70 | 47.10 | 0.163 | 0.837 |
| 19-18-17 | 24.00 | 15.40 | 39.40 | 15.40 | 54.80 | 0.280 | 0.720 |
| 16 | 37.30 | 24.20 | 61.50 | 34.10 | 95.60 | 0.356 | 0.644 |
| 15-14-13 | 37.30 | 24.20 | 61.50 | 52.80 | 114.30 | 0.462 | 0.538 |
| 12 | 55.80 | 36.00 | 91.80 | 88.90 | 180.70 | 0.492 | 0.508 |
| 11-10-9 | 55.80 | 36.00 | 91.80 | 125.00 | 216.80 | 0.576 | 0.424 |
| 8 | 79.00 | 51.00 | 130.00 | 184.50 | 314.00 | 0.586 | 0.414 |
| 7-6-5 | 79.00 | 51.00 | 130.00 | 244.00 | 374.00 | 0.652 | 0.348 |
| 4 | 108.00 | 70.00 | 178.00 | 333.00 | 511.00 | 0.650 | 0.350 |
| 3 | 108.00 | 70.00 | 178.00 | 422.00 | 600.00 | 0.702 | 0.292 |
| 2 | 108.00 | 70.00 | 178.00 | 358.00 | 536.00 | 0.670 | 0.330 |
| 1 | 108.00 | 70.00 | 178.00 | 307.00 | 485.00 | 0.632 | 0.368 |

A Factors

| | | | | |
|------------|---|-----|-------------------------|-----------|
| $A_{20} =$ | $\frac{630}{2(8.75 + 8.60 + 7.60 + 8.16)}$ | $=$ | $\frac{3.15}{39.11}$ | $= 0.095$ |
| $A_{19} =$ | $\frac{10.90}{2(8.30 + 8.30 + 7.02 + 7.02)}$ | $=$ | $\frac{9.45}{30.64}$ | $= 0.308$ |
| $A_{18} =$ | $\frac{31.20}{2(8.30 + 8.30 + 7.02 + 7.02)}$ | $=$ | $\frac{15.60}{30.64}$ | $= 0.510$ |
| $A_{17} =$ | $\frac{43.50}{2(7.70 + 8.00 + 5.35 + 6.70)}$ | $=$ | $\frac{21.75}{28.75}$ | $= 0.757$ |
| $A_{16} =$ | $\frac{55.80}{2(22.70 + 24.00 + 17.80 + 19.30)}$ | $=$ | $\frac{27.90}{83.80}$ | $= 0.332$ |
| $A_{15} =$ | $\frac{67.50}{2(21.30 + 21.30 + 16.40 + 16.40)}$ | $=$ | $\frac{33.75}{75.40}$ | $= 0.447$ |
| $A_{14} =$ | $\frac{79.00}{2(21.30 + 21.30 + 16.40 + 16.40)}$ | $=$ | $\frac{39.50}{75.40}$ | $= 0.521$ |
| $A_{13} =$ | $\frac{91.00}{2(20.50 + 20.90 + 15.70 + 16.00)}$ | $=$ | $\frac{45.50}{73.10}$ | $= 0.621$ |
| $A_{12} =$ | $\frac{102.00}{2(41.30 + 45.50 + 31.50 + 34.00)}$ | $=$ | $\frac{51.00}{152.40}$ | $= 0.334$ |
| $A_{11} =$ | $\frac{113.00}{2(39.60 + 39.60 + 29.00 + 29.00)}$ | $=$ | $\frac{56.50}{137.20}$ | $= 0.412$ |
| $A_{10} =$ | $\frac{120.00}{2(39.60 + 39.60 + 29.00 + 29.00)}$ | $=$ | $\frac{60.00}{137.20}$ | $= 0.436$ |
| $A_9 =$ | $\frac{135.00}{2(39.00 + 39.40 + 28.50 + 28.70)}$ | $=$ | $\frac{67.50}{135.60}$ | $= 0.500$ |
| $A_8 =$ | $\frac{145.00}{2(67.50 + 71.70 + 48.00 + 51.30)}$ | $=$ | $\frac{72.50}{238.50}$ | $= 0.304$ |
| $A_7 =$ | $\frac{154.00}{2(63.70 + 63.70 + 44.60 + 44.60)}$ | $=$ | $\frac{77.00}{216.60}$ | $= 0.355$ |
| $A_6 =$ | $\frac{163.00}{2(63.70 + 63.70 + 44.60 + 44.60)}$ | $=$ | $\frac{81.50}{216.60}$ | $= 0.375$ |
| $A_5 =$ | $\frac{172.00}{2(63.90 + 63.80 + 44.60 + 44.60)}$ | $=$ | $\frac{86.00}{216.90}$ | $= 0.396$ |
| $A_4 =$ | $\frac{181.00}{2(98.10 + 104.20 + 68.50 + 72.70)}$ | $=$ | $\frac{90.50}{343.50}$ | $= 0.263$ |
| $A_3 =$ | $\frac{189.00}{2(100.00 + 96.00 + 70.80 + 67.50)}$ | $=$ | $\frac{94.50}{334.30}$ | $= 0.283$ |
| $A_2 =$ | $\frac{286.00}{2(78.20 + 75.40 + 55.20 + 53.40)}$ | $=$ | $\frac{143.00}{262.20}$ | $= 0.545$ |
| $A_1 =$ | $\frac{270.00}{2(189.00 + 138.00 + 180.00 + 121.00)}$ | $=$ | $\frac{135.00}{628.00}$ | $= 0.215$ |

B Factors

| | | | |
|-----------|--|--------------------------|-----------|
| B_{20a} | $= \frac{0.82}{6.80 + 3.76}$ | $= \frac{0.82}{10.56}$ | $= 0.078$ |
| B_{19a} | $= \frac{0.83 + 2.65}{11.40 + 6.45}$ | $= \frac{3.38}{17.85}$ | $= 0.19$ |
| B_{18a} | $= \frac{2.55 + 4.22}{11.40 + 6.45}$ | $= \frac{6.77}{17.85}$ | $= 0.38$ |
| B_{17a} | $= \frac{4.22 + 6.05}{11.40 + 6.40}$ | $= \frac{10.27}{17.85}$ | $= 0.576$ |
| B_{16a} | $= \frac{5.80 + 7.95}{22.10 + 12.90}$ | $= \frac{13.75}{35.00}$ | $= 0.392$ |
| B_{15a} | $= \frac{7.52 + 9.50}{28.10 + 16.70}$ | $= \frac{17.02}{44.80}$ | $= 0.38$ |
| B_{14a} | $= \frac{9.50 + 11.10}{28.10 + 16.70}$ | $= \frac{20.60}{44.80}$ | $= 0.46$ |
| B_{13a} | $= \frac{11.10 + 13.00}{28.10 + 16.70}$ | $= \frac{24.10}{44.80}$ | $= 0.538$ |
| B_{12a} | $= \frac{12.70 + 15.20}{44.40 + 26.50}$ | $= \frac{27.90}{70.90}$ | $= 0.393$ |
| B_{11a} | $= \frac{13.80 + 16.30}{15.20 + 31.00}$ | $= \frac{30.10}{82.20}$ | $= 0.365$ |
| B_{10a} | $= \frac{16.30 + 17.30}{51.20 + 31.00}$ | $= \frac{33.60}{82.20}$ | $= 0.408$ |
| B_{9a} | $= \frac{17.30 + 19.70}{51.20 + 31.00}$ | $= \frac{37.00}{82.20}$ | $= 0.450$ |
| B_{8a} | $= \frac{19.50 + 21.70}{73.80 + 44.60}$ | $= \frac{41.20}{118.40}$ | $= 0.348$ |
| B_{7a} | $= \frac{20.50 + 22.60}{81.00 + 49.70}$ | $= \frac{43.10}{130.70}$ | $= 0.330$ |
| B_{6a} | $= \frac{22.60 + 23.80}{81.00 + 49.70}$ | $= \frac{46.40}{130.70}$ | $= 0.355$ |
| B_{5a} | $= \frac{23.80 + 25.10}{81.00 + 49.70}$ | $= \frac{48.90}{130.70}$ | $= 0.374$ |
| B_{4a} | $= \frac{25.20 + 27.40}{111.00 + 68.00}$ | $= \frac{52.60}{179.00}$ | $= 0.294$ |
| B_{3a} | $= \frac{25.70 + 27.10}{119.00 + 73.30}$ | $= \frac{52.80}{192.30}$ | $= 0.275$ |
| B_{2a} | $= \frac{28.30 + 41.00}{113.00 + 70.00}$ | $= \frac{69.30}{183.00}$ | $= 0.380$ |
| B_{1a} | $= \frac{42.60 + 29.60}{180.00 + 66.30}$ | $= \frac{72.20}{174.30}$ | $= 0.415$ |



| | | | | | | | | | | | | |
|--|---|---|---|---|---|---|---|---|---|---|---|---|
| $12.70 = M$ $20.50 = 26.40 \times 0.777$ $K = 26.40$ | $13.80 = M$ $41.30 = 62.50 \times 0.678$ $K = 62.50$ | $16.30 = M$ $39.60 = 62.50 \times 0.636$ $K = 62.50$ | $17.30 = M$ $39.40 = 62.50 \times 0.636$ $K = 62.50$ | $19.50 = M$ $39.00 = 62.50 \times 0.626$ $K = 62.50$ | $20.50 = M$ $67.50 = 122 \times 0.555$ $K = 122$ | $22.60 = M$ $63.70 = 122 \times 0.522$ $K = 122$ | $23.70 = M$ $63.70 = 122 \times 0.522$ $K = 122$ | $25.20 = M$ $63.40 = 122 \times 0.524$ $K = 122$ | $25.70 = M$ $98.10 = 211 \times 0.467$ $K = 211$ | $28.30 = M$ $100 = 211 \times 0.476$ $K = 211$ | $42.60 = M$ $78.20 = 147 \times 0.533$ $K = 147$ | $40.60 = M$ $189 = 160 \times 1.184$ $K = 160$ |
| $15.50 = M$ $44.40 = 52.80 \times 0.798$ $K = 52.80$ | $17.70 = M$ $51.20 = 55.80 \times 0.921$ $K = 55.80$ | $20.30 = M$ $51.20 = 55.80 \times 0.921$ $K = 55.80$ | $23.00 = M$ $52.00 = 55.80 \times 0.921$ $K = 55.80$ | $25.70 = M$ $75.80 = 79 \times 0.936$ $K = 79$ | $26.70 = M$ $81 = 79 \times 1.025$ $K = 79$ | $28.20 = M$ $81 = 79 \times 1.025$ $K = 79$ | $30.20 = M$ $81 = 79 \times 1.025$ $K = 79$ | $32.60 = M$ $111 = 108 \times 1.028$ $K = 108$ | $32.60 = M$ $119 = 108 \times 1.100$ $K = 108$ | $42.70 = M$ $113 = 108 \times 1.053$ $K = 108$ | $44.70 = M$ $108 = 108 \times 1.002$ $K = 108$ | $48.70 = M$ $108 = 108 \times 1.002$ $K = 108$ |
| $9.75 = M$ $15.70 = 26.40 \times 0.595$ $K = 26.40$ | $10.50 = M$ $31.50 = 62.50 \times 0.504$ $K = 62.50$ | $11.90 = M$ $29.00 = 62.50 \times 0.465$ $K = 62.50$ | $12.70 = M$ $29.00 = 62.50 \times 0.465$ $K = 62.50$ | $14.25 = M$ $28.50 = 62.50 \times 0.455$ $K = 62.50$ | $14.50 = M$ $48.00 = 122 \times 0.394$ $K = 122$ | $15.80 = M$ $44.60 = 122 \times 0.366$ $K = 122$ | $16.70 = M$ $44.60 = 122 \times 0.366$ $K = 122$ | $17.60 = M$ $44.60 = 122 \times 0.366$ $K = 122$ | $18.00 = M$ $68.50 = 211 \times 0.326$ $K = 211$ | $20.00 = M$ $70.00 = 211 \times 0.336$ $K = 211$ | $30.20 = M$ $55.20 = 147 \times 0.377$ $K = 147$ | $38.60 = M$ $180 = 160 \times 1.130$ $K = 160$ |
| $10 = 16.00$ $M = 9.95$ | 0.388 0.135 $0.543 \times 62.50 = 34.00$ $M = 11.30$ | 0.310 0.155 $0.465 \times 62.50 = 29.00$ $M = 11.90$ | 0.310 0.155 $0.465 \times 62.50 = 29.00$ $M = 12.70$ | 0.310 0.150 $0.460 \times 62.50 = 28.70$ $M = 14.35$ | 0.300 0.122 $0.422 \times 122 = 51.30$ $M = 15.60$ | 0.244 0.122 $0.366 \times 122 = 44.60$ $M = 15.80$ | 0.244 0.122 $0.366 \times 122 = 44.60$ $M = 16.70$ | 0.244 0.122 $0.366 \times 122 = 44.60$ $M = 17.60$ | 0.244 0.102 $0.346 \times 211 = 72.70$ $M = 19.10$ | 0.204 0.117 $0.321 \times 211 = 67.50$ $M = 19.10$ | 0.234 0.130 $0.364 \times 147 = 53.40$ $M = 23.20$ | 0.260 0.500 $0.760 \times 160 = 121$ $M = 26.20$ |

Checking Results of Factor Method

$$R_1 + R_2 = \frac{40.60 + 29.60 + 38.60 + 26.20}{4.50} = \frac{135.00}{4.50} = 30$$

$$\sum F_x = 60 - 2 \times 30 = 0$$

∴ O.K.

ANALYSIS OF THE EFFECT OF WIND ON A HIGH REINFORCED CONCRETE BUILDING

Comparison of Approximate and Exact Methods

| | | |
|------------|-----------------|---------------------|
| COMPUTER : | RIAD SHAHIN | FACTOR METHOD |
| CHK'D BY : | RIAD SHAHIN | |
| APP'D BY : | DR. JACK NASSER | DATE: DECEMBER 1964 |
| | | SHEET NO 27 |

CHAPTER THREE

HARDY CROSS METHOD

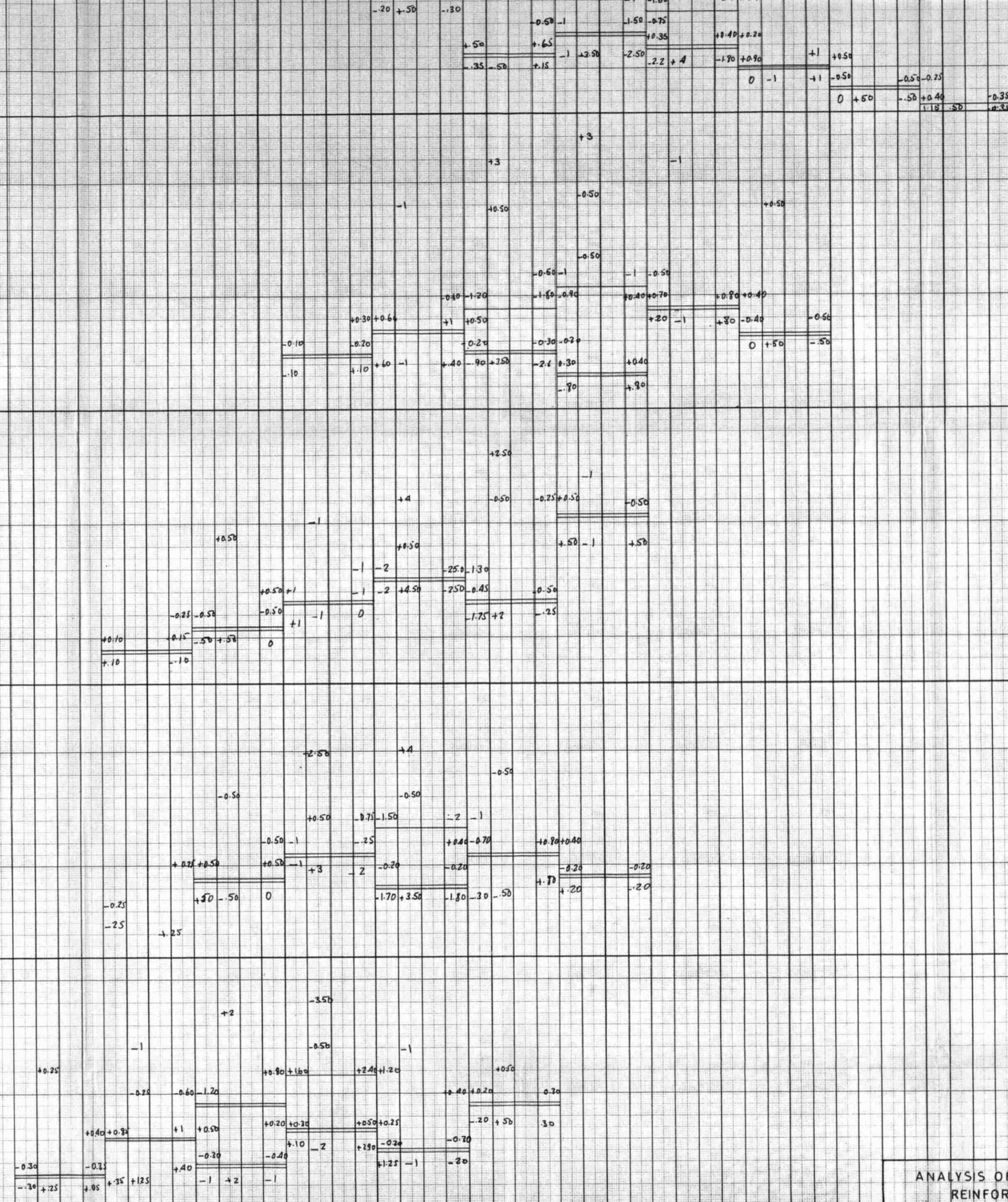
CASE A

Physical Constants

| Joint | Kg. R | K _c | | Σ K | Distribution factors | | | F E M (-6EKθ/r) T-m |
|-------|----------|----------------|--------|---------|----------------------|-------|-------|---------------------------|
| | | I | S | | I | R | S | |
| 20 | 2.70 | 0.97 | 0 | 3.67 | 0.26 | 0.74 | 00 | - 2.00 |
| 19 | 2.70 | 0.97 | 0.97 | 4.64 | 0.21 | 0.58 | 0.21 | - 2.00 |
| 18 | 2.70 | 3.33 | 0.97 | 7.00 | 0.48 | 0.48 | 0.14 | - 6.00 |
| 17 | 2.70 | 11.30 | 3.33 | 17.33 | 0.65 | 0.16 | 0.19 | - 20.00 |
| 16 | 3.20 | 20.30 | 11.30 | 34.80 | 0.58 | 0.09 | 0.33 | - 35.70 |
| 15 | 3.72 | 33.80 | 20.30 | 57.82 | 0.58 | 0.07 | 0.35 | - 60.00 |
| 14 | 4.30 | 51.50 | 33.80 | 89.60 | 0.57 | 0.05 | 0.38 | - 90.00 |
| 13 | 4.80 | 76.00 | 51.50 | 132.30 | 0.57 | 0.04 | 0.39 | - 134.00 |
| 12 | 5.35 | 105.00 | 76.00 | 186.35 | 0.56 | 0.04 | 0.40 | - 185.00 |
| 11 | 6.42 | 162.00 | 105.00 | 273.42 | 0.59 | 0.02 | 0.39 | - 285.00 |
| 10 | 7.00 | 210.00 | 162.00 | 379.00 | 0.56 | 0.02 | 0.43 | - 360.00 |
| 9 | 7.50 | 270.00 | 210.00 | 489.50 | 0.55 | 0.02 | 0.43 | - 475.00 |
| 8 | 8.56 | 373.00 | 270.00 | 651.56 | 0.57 | 0.01 | 0.42 | - 658.00 |
| 7 | 8.90 | 460.00 | 373.00 | 841.90 | 0.55 | 0.01 | 0.44 | - 810.00 |
| 6 | 8.90 | 550.00 | 460.00 | 1010.90 | 0.54 | 0.01 | 0.45 | - 970.00 |
| 5 | 9.70 | 710.00 | 550.00 | 1269.70 | 0.56 | 0.01 | 0.43 | - 1250.00 |
| 4 | 10.30 | 980.00 | 710.00 | 1700.30 | 0.57 | 0.01 | 0.42 | - 1730.00 |
| 3 | 10.70 | 980.00 | 980.00 | 1970.70 | 0.495 | 0.010 | 0.495 | -1730.00 |
| 2 | 11.30 | 680.00 | 980.00 | 1671.30 | 0.41 | 0.01 | 0.58 | - 830.00 |
| 1 | 11.30 | 740.00 | 680.00 | 1431.30 | 0 | 0.51 | 0.01 | - 985.00 |

| Joint a | K _{g2} | K _c | K _{g1} | K _{g1 Mod} | K _c | ΣK | Distribution factors | | | | F. E. M. K _{g1} / T. m |
|------------|-----------------|----------------|-----------------|---------------------|----------------|---------|----------------------|-------|-------|-------|------------------------------------|
| | | S | L | R | I | | S | L | R | I | |
| 20 | 1.74 | 0 | 2.70 | 2.60 | 0.97 | 6.17 | 0 | 0.42 | 0.42 | 0.16 | -2.00 |
| 19 | 1.74 | 0.97 | 2.70 | 2.60 | 1.92 | 8.19 | 0.12 | 0.33 | 0.92 | 0.23 | -3.40 |
| 18 | 1.74 | 1.92 | 2.70 | 2.60 | 5.25 | 12.47 | 0.15 | 0.22 | 0.21 | 0.42 | -9.30 |
| 17 | 1.74 | 5.25 | 2.70 | 2.60 | 11.30 | 21.85 | 0.24 | 0.12 | 0.12 | 0.52 | -20.00 |
| 16 | 2.08 | 11.30 | 3.20 | 3.12 | 20.30 | 37.92 | 0.30 | 0.09 | 0.08 | 0.53 | -36.00 |
| 15 | 2.42 | 20.30 | 3.72 | 3.62 | 33.80 | 61.44 | 0.33 | 0.06 | 0.06 | 0.55 | -60.00 |
| 14 | 2.78 | 33.80 | 4.30 | 4.16 | 63.00 | 105.26 | 0.32 | 0.04 | 0.04 | 0.60 | -111.00 |
| 13 | 3.10 | 63.00 | 4.80 | 4.65 | 89.00 | 161.45 | 0.39 | 0.03 | 0.03 | 0.55 | -157.00 |
| 12 | 3.46 | 89.00 | 5.35 | 5.20 | 123.00 | 222.55 | 0.40 | 0.026 | 0.024 | 0.55 | -217.00 |
| 11 | 4.15 | 123.00 | 6.42 | 6.22 | 162.00 | 297.64 | 0.41 | 0.02 | 0.02 | 0.55 | -285.00 |
| 10 | 4.50 | 162.00 | 7.00 | 6.75 | 238.00 | 414.00 | 0.39 | 0.018 | 0.017 | 0.575 | -420.00 |
| 9 | 4.85 | 238.00 | 7.50 | 7.25 | 298.00 | 550.75 | 0.435 | 0.013 | 0.012 | 0.54 | -525.00 |
| 8 | 5.50 | 298.00 | 8.66 | 8.25 | 412.00 | 726.81 | 0.41 | 0.01 | 0.01 | 0.57 | -725.00 |
| 7 | 5.70 | 412.00 | 8.90 | 8.52 | 500.00 | 929.42 | 0.44 | 0.01 | 0.01 | 0.54 | -880.00 |
| 6 | 5.70 | 500.00 | 8.90 | 8.52 | 600.00 | 1110.00 | 0.45 | 0.01 | 0.01 | 0.53 | -1050.00 |
| 5 | 6.25 | 600.00 | 9.70 | 9.35 | 770.00 | 1389.00 | 0.43 | 0.01 | 0.01 | 0.55 | -1430.00 |
| 4 | 6.62 | 770.00 | 10.30 | 9.90 | 980.00 | 1770.00 | 0.43 | 0.01 | 0.01 | 0.55 | -1730.00 |
| 3 | 6.92 | 980.00 | 10.70 | 10.40 | 980.00 | 1981.00 | 0.49 | 0.01 | 0.01 | 0.49 | -1730.00 |
| 2 | 7.30 | 980.00 | 11.30 | 10.90 | 680.00 | 1682.00 | 0.58 | 0.01 | 0.01 | 0.40 | -830.00 |
| 1 | 7.30 | 680.00 | 11.30 | 10.90 | 740.00 | 1442.00 | 0.47 | 0.01 | 0.01 | 0.51 | -985.00 |

| JOINT | 10 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 9a | 9a | 7a | 6a | 5a | 4a | 3a | 2a | 1a | 0 |
|-------------------------------------|---------|-------|-------|-------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|------|
| MEMBER | S | I | R | S | I | R | S | I | R | S | I | R | S | I | R | S | I | R | S | I | R | S | I | R | S |
| DIST. FACTOR | 0 | 0.5 | 0.0 | 0.47 | 0.47 | 0.01 | 0.58 | 0.43 | 0.01 | 0.47 | 0.58 | 0.01 | 0.47 | 0.58 | 0.01 | 0.47 | 0.58 | 0.01 | 0.47 | 0.58 | 0.01 | 0.47 | 0.58 | 0.01 | 0.47 |
| Influence of Δ 1 on Interior Column | | | | | | | | | | | | | | | | | | | | | | | | | |
| 9.81 | -9.81 | | | | | | | | | | | | | | | | | | | | | | | | |
| 251 | +251 | +11 | +472 | +236 | | | | | | | | | | | | | | | | | | | | | |
| 172.44 | +172.44 | +11 | +472 | +236 | | | | | | | | | | | | | | | | | | | | | |
| 13.00 | +13.00 | +15 | +2.33 | +1.40 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0.01 | +0.01 | | | | | | | | | | | | | | | | | | | | | |
| 0.01 | +0.01 | +0.01 | +0. | | | | | | | | | | | | | | | | | | | | | | |



| | |
|---|------------------------------------|
| ANALYSIS OF THE EFFECT OF WIND ON A HIGH REINFORCED CONCRETE BUILDING | |
| Comparison of Approximate and Exact Methods | |
| COMPUTER BY : RIAD SHAHIN | WIND ANALYSIS |
| CHK'D BY : RIAD SHAHIN | HARDY CROSS METHOD |
| APP'D BY : DR. JACK NASSER | DATE : DECEMBER 1964 SHEET N° 31 / |

| JOINT | Influence of $\Delta 12$ on Exterior Column | Influence of $\Delta 13$ on Exterior Column | Influence of $\Delta 14$ on Exterior Column | Influence of $\Delta 15$ on Exterior Column | Influence of $\Delta 16$ on Exterior Column | Influence of $\Delta 17$ on Exterior Column | Influence of $\Delta 18$ on Exterior Column | Influence of $\Delta 19$ on Exterior Column | Influence of $\Delta 20$ on Exterior Column |
|-------|---|---|---|---|---|---|---|---|---|
| 7 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 8 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 9 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 10 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 11 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 12 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 13 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 14 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 15 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 16 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 17 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 18 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 19 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 20 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 20a | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 19a | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 18a | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 17a | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 16a | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 15a | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 14a | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 13a | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 12a | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 11a | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 10a | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 9a | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 8a | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 7a | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |

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| | | |
|-----|---|-------|
| 1 | S | 0.21 |
| 15 | I | 0.28 |
| 16 | R | 0.07 |
| 17 | S | 0.35 |
| 18 | T | 0.58 |
| 19 | R | 0.07 |
| 20 | S | 0.407 |
| 20a | I | 0.33 |
| 19a | R | 0.65 |
| 18a | S | 0.16 |
| 17a | T | 0.19 |
| 16a | R | 0.48 |
| 15a | S | 0.31 |
| 14a | I | 0.14 |
| 13a | R | 0.21 |
| 12a | S | 0.58 |
| 11a | T | 0.21 |
| 10a | R | 0.26 |
| 9a | S | 0.74 |
| 8a | I | — |
| 7a | R | 0.42 |
| 6a | S | 0.42 |
| 5a | T | 0.16 |
| 4a | R | 0.12 |
| 3a | S | 0.33 |
| 2a | I | 0.32 |
| 1a | R | 0.25 |
| 19b | S | 0.15 |
| 18b | T | 0.22 |
| 17b | R | 0.21 |
| 16b | S | 0.47 |
| 15b | I | 0.24 |
| 14b | R | 0.12 |
| 13b | S | 0.12 |
| 12b | T | 0.52 |
| 11b | R | 0.20 |
| 10b | S | 0.09 |
| 9b | I | 0.68 |
| 8b | R | 0.53 |
| 7b | S | 0.33 |
| 6b | T | 0.06 |
| 5b | R | 0.06 |
| 4b | S | 0.55 |
| 3b | I | 0.32 |
| 2b | R | 0.04 |
| 1b | S | 0.60 |
| 19c | T | 0.34 |
| 18c | R | 0.02 |
| 17c | S | 0.03 |
| 16c | I | 0.65 |
| 15c | R | 1.40 |
| 14c | S | 0.26 |
| 13c | T | 0.64 |
| 12c | R | 0.55 |
| 11c | S | 0.01 |
| 10c | I | 0 |

Influence of $\Delta 11$ on Interior Column

Influence of $\Delta 10$ on Interior Column

Influence of $\Delta 9$ on Interior Column

Influence of $\Delta 8$ on Interior Column

Influence of $\Delta 7$ on Interior Column

Influence of $\Delta 6$ on Interior Column

JOINT NUMBER DIST FACTOR

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| JOINT NUMBER | DIST | FACTOR | Influence of $\Delta 6$ on Interior Column | Influence of $\Delta 7$ on Interior Column | Influence of $\Delta 8$ on Interior Column | Influence of $\Delta 9$ on Interior Column | Influence of $\Delta 10$ on Interior Column | Influence of $\Delta 11$ on Interior Column |
|--------------|------|--------|--|--|--|--|---|---|
| 1 | 0 | 0.51 | | | | | | |
| 2 | 0 | 0.48 | | | | | | |
| 3 | 0 | 0.41 | | | | | | |
| 4 | 0 | 0.58 | | | | | | |
| 5 | 0 | 0.48 | | | | | | |
| 6 | 0 | 0.41 | | | | | | |
| 7 | 0 | 0.58 | | | | | | |
| 8 | 0 | 0.48 | | | | | | |
| 9 | 0 | 0.41 | | | | | | |
| 10 | 0 | 0.58 | | | | | | |
| 11 | 0 | 0.48 | | | | | | |
| 12 | 0 | 0.41 | | | | | | |
| 13 | 0 | 0.58 | | | | | | |
| 14 | 0 | 0.48 | | | | | | |
| 15 | 0 | 0.41 | | | | | | |

-75
 $-75 + 1.58 - 2 + 2.5$
 $-75 + 1.58 - 2 + 2.5$

$+50$
 -50
 $-50 + 50$

$+50$
 -50
 $-50 + 50$

$+50$
 $+30 + 60$
 $+40$
 -50
 $-50 + 50$

$+2.5$
 $+2.5$
 -50
 $-50 + 2$
 -1.50
 $0.70 + 2$
 -1.30
 $-1.60 + 3$
 -1.40
 $+0.50$
 -1.60
 $-1.40 - 7.0$
 $+1$
 $+7.0$

$+2.5$
 $+2.5$
 -50
 $-50 + 2$
 -1.50
 $0.70 + 2$
 -1.30
 $-1.60 + 3$
 -1.40
 $+0.50$
 -1.60
 $-1.40 - 7.0$
 $+1$
 $+7.0$

-50
 -50
 $+1$
 $+1.58$
 $-50 + 1.58 - 50 - 1$
 $-1.00 + 2.28$
 -1
 $-1.50 + 2.5$
 -1
 $+50$
 $-50 + 50$

| DENOMI NATION | C FACTOR (z/n) | $\Delta 1$ | $\Delta 2$ | $\Delta 3$ | $\Delta 4$ | $\Delta 5$ | $\Delta 6$ | $\Delta 7$ | $\Delta 8$ |
|------------------|----------------------|-------------------------|------------------------|------------------------|-------------------------|-----------------------|------------------------|------------------------|----------------------|
| 1 | -0.588 | ZM=-2363.21 V=-639.0 | ZM=+1027.45 V=-6.10 | ZM=-452.30 V=-2.66 | ZM=+113.55 V=-66.50 | ZM=-27.25 V=-4.16 | ZM=+3 V=-1.77 | ZM=-1.50 V=+0.88 | 0.40 |
| 2 | 1/3 | ZM=+144.83 V=-6.70 | ZM=-148.15 V=-4.870 | ZM=+1321.58 V=-82.0 | ZM=-316.95 V=-19.0 | ZM=+70.50 V=-43.80 | ZM=-1.9 V=+11.20 | ZM=+5 V=-2.95 | ZM=-0.40 V=+6 |
| | | ZM=+144.83 V=-6.70 | ZM=-148.15 V=-4.870 | ZM=+1321.58 V=-82.0 | ZM=-316.95 V=-19.0 | ZM=+70.50 V=-43.80 | ZM=-1.9 V=+11.20 | ZM=+5 V=-2.95 | ZM=-0.40 V=+6 |
| 3 | 1/3 | ZM=+354.12 V=+197 | ZM=-492.10 V=-545 | ZM=-229.8 V=+16.90 | ZM=+454.90 V=-855 | ZM=-333.75 V=-198 | ZM=-12.60 V=+7.40 | ZM=-18.90 V=+11.0 | ZM=+4.00 V=-2 |
| | | ZM=+354.12 V=+197 | ZM=-492.10 V=-545 | ZM=-229.8 V=+16.90 | ZM=+454.90 V=-855 | ZM=-333.75 V=-198 | ZM=-12.60 V=+7.40 | ZM=-18.90 V=+11.0 | ZM=+4.00 V=-2 |
| 4 | 1/3 | ZM=+35.18 V=-4.9 | ZM=-229.55 V=+35 | ZM=-2.25 V=+4.6 | ZM=-2157.90 V=+133.0 | ZM=+124.75 V=-18.0 | ZM=+2.9215 V=+17.2 | ZM=+192.40 V=-42.60 | ZM=-1.9 V=+11 |
| | | ZM=+35.18 V=-4.9 | ZM=-229.55 V=+35 | ZM=-2.25 V=+4.6 | ZM=-2157.90 V=+133.0 | ZM=+124.75 V=-18.0 | ZM=+2.9215 V=+17.2 | ZM=+192.40 V=-42.60 | ZM=-1.9 V=+11 |
| 5 | 1/3 | ZM=-18.60 V=-110.90 | ZM=+52.90 V=-31 | ZM=-330.15 V=+1.95 | ZM=-152.2 V=+7.0 | ZM=-202.50 V=+11.0 | ZM=-152.310 V=+12.0 | ZM=-25.0 V=+14.7 | ZM=+6.0 V=-35 |
| | | ZM=-18.60 V=-110.90 | ZM=+52.90 V=-31 | ZM=-330.15 V=+1.95 | ZM=-152.2 V=+7.0 | ZM=-202.50 V=+11.0 | ZM=-152.310 V=+12.0 | ZM=-25.0 V=+14.7 | ZM=+6.0 V=-35 |
| 6 | 1/3 | ZM=+4.26 V=-2.52 | ZM=-12.40 V=-46.70 | ZM=+75.90 V=-44.60 | ZM=-302.75 V=+11.7 | ZM=+4.90 V=-6.40 | ZM=-152.310 V=+12.0 | ZM=+82.20 V=+12.0 | ZM=+82.20 V=+12.0 |
| | | ZM=+4.26 V=-2.52 | ZM=-12.40 V=-46.70 | ZM=+75.90 V=-44.60 | ZM=-302.75 V=+11.7 | ZM=+4.90 V=-6.40 | ZM=-152.310 V=+12.0 | ZM=+82.20 V=+12.0 | ZM=+82.20 V=+12.0 |
| 7 | 1/3 | ZM=0.52 V=+0.31 | ZM=+2.0 V=-1.10 | ZM=-1.25 V=+11.30 | ZM=+22.85 V=-24.25 | ZM=-257.50 V=+1.57 | ZM=+82.20 V=+12.0 | ZM=+82.20 V=+12.0 | ZM=+82.20 V=+12.0 |
| | | ZM=0.52 V=+0.31 | ZM=+2.0 V=-1.10 | ZM=-1.25 V=+11.30 | ZM=+22.85 V=-24.25 | ZM=-257.50 V=+1.57 | ZM=+82.20 V=+12.0 | ZM=+82.20 V=+12.0 | ZM=+82.20 V=+12.0 |
| 8 | 1/3 | ZM=-0.10 V=+0.6 | ZM=+2.75 V=-2.20 | ZM=-1.8 V=+10.60 | ZM=+61 V=+3.6 | ZM=-1.92 V=+11.6 | ZM=+82.20 V=+12.0 | ZM=+82.20 V=+12.0 | ZM=+82.20 V=+12.0 |
| | | ZM=-0.10 V=+0.6 | ZM=+2.75 V=-2.20 | ZM=-1.8 V=+10.60 | ZM=+61 V=+3.6 | ZM=-1.92 V=+11.6 | ZM=+82.20 V=+12.0 | ZM=+82.20 V=+12.0 | ZM=+82.20 V=+12.0 |
| 9 | 1/3 | ZM=0.43 V=+0.10 | ZM=1.20 V=+0.80 | ZM=7.50 V=+1.75 | ZM=2.3 V=+1.50 | ZM=1.92 V=+11.6 | ZM=+82.20 V=+12.0 | ZM=+82.20 V=+12.0 | ZM=+82.20 V=+12.0 |
| | | ZM=0.43 V=+0.10 | ZM=1.20 V=+0.80 | ZM=7.50 V=+1.75 | ZM=2.3 V=+1.50 | ZM=1.92 V=+11.6 | ZM=+82.20 V=+12.0 | ZM=+82.20 V=+12.0 | ZM=+82.20 V=+12.0 |
| 10 | 1/3 | ZM=0.44 V=2.00 | ZM=1.20 V=6.00 | ZM=7.50 V=38.00 | ZM=2.3 V=38.00 | ZM=1.92 V=11.7 | ZM=+82.20 V=+12.0 | ZM=+82.20 V=+12.0 | ZM=+82.20 V=+12.0 |
| | | ZM=0.44 V=2.00 | ZM=1.20 V=6.00 | ZM=7.50 V=38.00 | ZM=2.3 V=38.00 | ZM=1.92 V=11.7 | ZM=+82.20 V=+12.0 | ZM=+82.20 V=+12.0 | ZM=+82.20 V=+12.0 |
| 11 | 1/3 | ZM=0.52 V=+0.31 | ZM=+2.0 V=-1.10 | ZM=-1.25 V=+11.30 | ZM=+22.85 V=-24.25 | ZM=-257.50 V=+1.57 | ZM=+82.20 V=+12.0 | ZM=+82.20 V=+12.0 | ZM=+82.20 V=+12.0 |
| | | ZM=0.52 V=+0.31 | ZM=+2.0 V=-1.10 | ZM=-1.25 V=+11.30 | ZM=+22.85 V=-24.25 | ZM=-257.50 V=+1.57 | ZM=+82.20 V=+12.0 | ZM=+82.20 V=+12.0 | ZM=+82.20 V=+12.0 |
| 12 | 1/3 | ZM=0.52 V=+0.31 | ZM=+2.0 V=-1.10 | ZM=-1.25 V=+11.30 | ZM=+22.85 V=-24.25 | ZM=-257.50 V=+1.57 | ZM=+82.20 V=+12.0 | ZM=+82.20 V=+12.0 | ZM=+82.20 V=+12.0 |
| | | ZM=0.52 V=+0.31 | ZM=+2.0 V=-1.10 | ZM=-1.25 V=+11.30 | ZM=+22.85 V=-24.25 | ZM=-257.50 V=+1.57 | ZM=+82.20 V=+12.0 | ZM=+82.20 V=+12.0 | ZM=+82.20 V=+12.0 |
| 13 | 1/3 | ZM=0.52 V=+0.31 | ZM=+2.0 V=-1.10 | ZM=-1.25 V=+11.30 | ZM=+22.85 V=-24.25 | ZM=-257.50 V=+1.57 | ZM=+82.20 V=+12.0 | ZM=+82.20 V=+12.0 | ZM=+82.20 V=+12.0 |
| | | ZM=0.52 V=+0.31 | ZM=+2.0 V=-1.10 | ZM=-1.25 V=+11.30 | ZM=+22.85 V=-24.25 | ZM=-257.50 V=+1.57 | ZM=+82.20 V=+12.0 | ZM=+82.20 V=+12.0 | ZM=+82.20 V=+12.0 |
| 14 | 1/3 | ZM=0.52 V=+0.31 | ZM=+2.0 V=-1.10 | ZM=-1.25 V=+11.30 | ZM=+22.85 V=-24.25 | ZM=-257.50 V=+1.57 | ZM=+82.20 V=+12.0 | ZM=+82.20 V=+12.0 | ZM=+82.20 V=+12.0 |
| | | ZM=0.52 V=+0.31 | ZM=+2.0 V=-1.10 | ZM=-1.25 V=+11.30 | ZM=+22.85 V=-24.25 | ZM=-257.50 V=+1.57 | ZM=+82.20 V=+12.0 | ZM=+82.20 V=+12.0 | ZM=+82.20 V=+12.0 |
| 15 | 1/3 | ZM=0.52 V=+0.31 | ZM=+2.0 V=-1.10 | ZM=-1.25 V=+11.30 | ZM=+22.85 V=-24.25 | ZM=-257.50 V=+1.57 | ZM=+82.20 V=+12.0 | ZM=+82.20 V=+12.0 | ZM=+82.20 V=+12.0 |
| | | ZM=0.52 V=+0.31 | ZM=+2.0 V=-1.10 | ZM=-1.25 V=+11.30 | ZM=+22.85 V=-24.25 | ZM=-257.50 V=+1.57 | ZM=+82.20 V=+12.0 | ZM=+82.20 V=+12.0 | ZM=+82.20 V=+12.0 |
| 16 | 1/3 | ZM=0.52 V=+0.31 | ZM=+2.0 V=-1.10 | ZM=-1.25 V=+11.30 | ZM=+22.85 V=-24.25 | ZM=-257.50 V=+1.57 | ZM=+82.20 V=+12.0 | ZM=+82.20 V=+12.0 | ZM=+82.20 V=+12.0 |
| | | ZM=0.52 V=+0.31 | ZM=+2.0 V=-1.10 | ZM=-1.25 V=+11.30 | ZM=+22.85 V=-24.25 | ZM=-257.50 V=+1.57 | ZM=+82.20 V=+12.0 | ZM=+82.20 V=+12.0 | ZM=+82.20 V=+12.0 |
| 17 | 1/3 | ZM=0.52 V=+0.31 | ZM=+2.0 V=-1.10 | ZM=-1.25 V=+11.30 | ZM=+22.85 V=-24.25 | ZM=-257.50 V=+1.57 | ZM=+82.20 V=+12.0 | ZM=+82.20 V=+12.0 | ZM=+82.20 V=+12.0 |
| | | ZM=0.52 V=+0.31 | ZM=+2.0 V=-1.10 | ZM=-1.25 V=+11.30 | ZM=+22.85 V=-24.25 | ZM=-257.50 V=+1.57 | ZM=+82.20 V=+12.0 | ZM=+82.20 V=+12.0 | ZM=+82.20 V=+12.0 |
| 18 | 1/3 | ZM=0.52 V=+0.31 | ZM=+2.0 V=-1.10 | ZM=-1.25 V=+11.30 | ZM=+22.85 V=-24.25 | ZM=-257.50 V=+1.57 | ZM=+82.20 V=+12.0 | ZM=+82.20 V=+12.0 | ZM=+82.20 V=+12.0 |
| | | ZM=0.52 V=+0.31 | ZM=+2.0 V=-1.10 | ZM=-1.25 V=+11.30 | ZM=+22.85 V=-24.25 | ZM=-257.50 V=+1.57 | ZM=+82.20 V=+12.0 | ZM=+82.20 V=+12.0 | ZM=+82.20 V=+12.0 |
| 19 | 1/3 | ZM=0.52 V=+0.31 | ZM=+2.0 V=-1.10 | ZM=-1.25 V=+11.30 | ZM=+22.85 V=-24.25 | ZM=-257.50 V=+1.57 | ZM=+82.20 V=+12.0 | ZM=+82.20 V=+12.0 | ZM=+82.20 V=+12.0 |
| | | ZM=0.52 V=+0.31 | ZM=+2.0 V=-1.10 | ZM=-1.25 V=+11.30 | ZM=+22.85 V=-24.25 | ZM=-257.50 V=+1.57 | ZM=+82.20 V=+12.0 | ZM=+82.20 V=+12.0 | ZM=+82.20 V=+12.0 |
| 20 | 1/3 | ZM=0.52 V=+0.31 | ZM=+2.0 V=-1.10 | ZM=-1.25 V=+11.30 | ZM=+22.85 V=-24.25 | ZM=-257.50 V=+1.57 | ZM=+82.20 V=+12.0 | ZM=+82.20 V=+12.0 | ZM=+82.20 V=+12.0 |
| | | ZM=0.52 V=+0.31 | ZM=+2.0 V=-1.10 | ZM=-1.25 V=+11.30 | ZM=+22.85 V=-24.25 | ZM=-257.50 V=+1.57 | ZM=+82.20 V=+12.0 | ZM=+82.20 V=+12.0 | ZM=+82.20 V=+12.0 |

Coefficients of Δ 's

| Δ_1 | Δ_2 | Δ_3 | Δ_4 | Δ_5 | Δ_6 | Δ_7 | Δ_8 | Δ_9 | Δ_{10} | Δ_{11} | Δ_{12} | Δ_{13} | Δ_{14} | Δ_{15} | Δ_{16} | Δ_{17} | Δ_{18} | Δ_{19} | Δ_{20} | Constant vector 10^4 |
|------------|------------|------------|------------|------------|------------|------------|------------|------------|---------------|---------------|---------------|---------------|---------------|---------------|---------------|---------------|---------------|---------------|---------------|---------------------------|
| +1390 | -610 | +266 | -66.50 | +16 | -1.77 | +0.88 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 60 |
| -6.70 | -870 | -820 | +190 | -4380 | +11.20 | -2.95 | +0.24 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 58.40 |
| +197 | -545 | +1640 | -853 | +198 | +7.40 | +11.10 | -2.60 | +0.30 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 55.70 |
| -49 | +1.35 | +426 | +1330 | -790 | +172 | -42.60 | +11.20 | -2.65 | +0.30 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 53.30 |
| +10.97 | -31 | +195 | +1780 | +1180 | -625 | +147 | -35.30 | +8.52 | -2.65 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 50.70 |
| -2.50 | +6.70 | -44.60 | +177 | -640 | +920 | -4.95 | +117 | -24.20 | +8.35 | -1.18 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 48.10 |
| +0.31 | -1.30 | +11.90 | -48.75 | +151 | -528 | +735 | -406 | +90.50 | -22.20 | +530 | -0.35 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 45.35 |
| +0.06 | | -2.20 | +10.60 | -36 | +115 | -407 | +590 | -386 | +68.50 | -12.90 | +3.20 | -0.35 | +0.12 | 0 | 0 | 0 | 0 | 0 | 0 | 42.45 |
| | | | -17.60 | +7.92 | -25 | +98 | -318 | +468 | -232 | +50.20 | -11.30 | +1.53 | -0.27 | 0 | 0 | 0 | 0 | 0 | 0 | 39.55 |
| | | | | -147 | +5.90 | -21 | +70.80 | -266 | +343 | -174 | +37 | -8.35 | +2.70 | -0.18 | 0 | 0 | 0 | 0 | 0 | 36.40 |
| | | | | | -1.18 | +4.70 | -17 | +51.20 | -17.0 | +253 | -12.5 | +27 | -8.35 | +1.35 | 0 | 0 | 0 | 0 | 0 | 33.20 |
| | | | | | | -0.80 | +4.12 | -18 | +36.70 | -127 | +189 | -89 | +20 | -4.70 | 0 | 0 | 0 | 0 | 0 | 30.00 |
| | | | | | | | -0.60 | +2.30 | -7.50 | +27.50 | -92 | +124 | -58 | +12.70 | -2.35 | 0 | 0 | 0 | 0 | 26.70 |
| | | | | | | | | | +1.18 | -6.30 | +19.40 | -58.50 | +106 | -39.70 | +7.08 | -1.35 | +0.12 | 0 | 0 | 23.90 |
| | | | | | | | | | +1.18 | -4.06 | +12.70 | -39.50 | +60 | -22.50 | +4.12 | -0.53 | 0 | 0 | 0 | 19.90 |
| | | | | | | | | | | +0.60 | -2.18 | +9.52 | -21.70 | +36 | -13.20 | +1.41 | 0 | 0 | 0 | 16.40 |
| | | | | | | | | | | | +0.18 | -1.77 | +4.50 | -13.50 | +22 | +5.75 | -0.35 | 0 | 0 | 12.80 |
| | | | | | | | | | | | | | | -0.83 | +1.97 | -4.36 | +10.30 | -1.59 | +0.18 | 9.20 |
| | | | | | | | | | | | | | | | +0.12 | -0.98 | +3.35 | -0.57 | 0 | 5.55 |
| | | | | | | | | | | | | | | | | +0.09 | -0.47 | +2.75 | 0 | 1.85 |

| Card No | Col. 1 | Col. 2 | Col. 3 | Col. 4 | Col. 5 | Col. 6 | Col. 7 | Col. 8 |
|---------|----------|----------|----------|----------|----------|----------|----------|----------|
| 1 | 2001 | | | | | | | |
| 2 | 54390000 | 53610000 | 53266000 | 52665000 | 52160000 | 51770000 | 50880000 | 0 |
| 3 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 4 | 0 | 0 | 0 | 0 | 53670000 | 53870000 | 53820000 | 53190000 |
| 5 | 52428000 | 52112000 | 51295000 | 50240000 | 0 | 0 | 0 | 0 |
| 6 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 7 | 53197000 | 53545000 | 54164000 | 53853000 | 53198000 | 51740000 | 52110000 | 51260000 |
| 8 | 50500000 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 9 | 0 | 0 | 0 | 0 | 52490000 | 53350000 | 51420000 | 54120000 |
| 10 | 53790000 | 53172000 | 52420000 | 52112000 | 51265000 | 50300000 | 0 | 0 |
| 11 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 12 | 52109000 | 52310000 | 53195000 | 53780000 | 54118000 | 53625000 | 53147000 | 52353000 |
| 13 | 51852000 | 51265000 | 0 | 0 | 0 | 0 | 0 | 0 |
| 14 | 0 | 0 | 0 | 0 | 51250000 | 51470000 | 52446000 | 53177000 |
| 15 | 53440000 | 53220000 | 53495000 | 53170000 | 52242000 | 51855000 | 51180000 | 0 |
| 16 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 17 | 50310000 | 51130000 | 52113000 | 52427000 | 53151000 | 53502000 | 53735000 | 53460000 |
| 18 | 52905000 | 52205000 | 51530000 | 50350000 | 0 | 0 | 0 | 0 |
| 19 | 0 | 0 | 0 | 0 | 49600000 | 0 | 0 | 0 |
| 20 | 53360000 | 53115000 | 53407000 | 53590000 | 53326000 | 52625000 | 52129000 | 51320000 |
| 21 | 50350000 | 50120000 | 0 | 0 | 0 | 0 | 0 | 0 |
| 22 | 0 | 0 | 0 | 52176000 | 51792000 | 52350000 | 52980000 | 53312000 |
| 23 | 53468000 | 53232000 | 52250200 | 52113000 | 51153000 | 50470000 | 0 | 0 |
| 24 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 25 | 51147000 | 51590000 | 52210000 | 52708000 | 53266000 | 53343000 | 53174000 | 52370000 |
| 26 | 51805000 | 51270000 | 50180000 | 0 | 0 | 0 | 0 | 0 |
| 27 | 0 | 0 | 0 | 0 | 0 | 51180000 | 51470000 | 52170000 |
| 28 | 52512000 | 53172000 | 53253000 | 53125000 | 52270000 | 51835000 | 51135000 | 0 |
| 29 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 30 | 0 | 0 | 50600000 | 51412000 | 52120000 | 52367000 | 53127000 | 53890000 |
| 31 | 52890000 | 52203000 | 51470000 | 0 | 0 | 0 | 0 | 0 |
| 32 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 50600000 |
| 33 | 51230000 | 51750000 | 52275000 | 52910000 | 53134000 | 52528000 | 52127000 | 52350000 |
| 34 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 35 | 0 | 0 | 0 | 0 | 0 | 51118000 | 51630000 | 52184000 |
| 36 | 52585000 | 53104000 | 52397000 | 51708000 | 51135000 | 50120000 | 0 | 0 |
| 37 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 38 | 0 | 0 | 51180000 | 51404000 | 52127000 | 52395000 | 52600000 | 52225000 |
| 39 | 51412000 | 50530000 | 0 | 0 | 0 | 0 | 0 | 0 |
| 40 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 50400000 |
| 41 | 51218000 | 51982000 | 52217000 | 52360000 | 52132000 | 51141000 | 0 | 0 |
| 42 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 43 | 0 | 0 | 0 | 0 | 50180000 | 51177000 | 51450000 | 52135000 |
| 44 | 52200000 | 51575000 | 50350000 | 0 | 0 | 0 | 0 | 0 |
| 45 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 46 | 0 | 0 | 50930000 | 51197000 | 51436000 | 52163000 | 51159000 | 50180000 |
| 47 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 48 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 49 | 50120000 | 50980000 | 51335000 | 50570000 | 0 | 0 | 0 | 0 |
| 50 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 51 | 0 | 0 | 0 | 0 | 0 | 49900000 | 50470000 | 51275000 |
| 52 | 56600000 | 56584000 | 56557000 | 56553000 | 56507000 | 56481000 | 56453500 | 56424500 |
| 53 | 56395000 | 56364000 | 56332000 | 56300000 | 56267000 | 56233000 | 56199000 | 56164000 |
| 54 | 56228000 | 55820000 | 55555000 | 55185000 | 0 | 0 | 0 | 0 |

Coefficient of Δ

DATA

Constant Vectors.

CONSTANT VECTOR

5660000000
5658400000
5655700000
5655300000
5650700000
5648100000
5645350000
5642450000
5639550000
5636400000
5633200000
5630000000
5626700000
5623300000
5619900000
5616400000
5612800000
5592000000
5555500000
5518500000

SOLUTION OF SYSTEM FOR ABOVE LISTED VECTOR

5414460775
5427975187
5412043157
5379877684
5418982066
5458285045
5510403778
5513978150
5516450226
5520029694
5520251165
5518738491
5516450883
5513794960
5514996205
5517002073
5519346969
5518450215
5522981723
5510051232

| | 180 | 120 | 110 | 100 | 90 | 80 | 70 | 60 | 50 | 40 | 30 | 20 | 10 | 0 |
|-----|-----|-----|-----|-----|----|----|----|----|----|----|----|----|----|---|
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4/4

ANALYSIS OF THE EFFECT OF WIND ON A HIGH REINFORCED CONCRETE BUILDING

Comparison of Approximate and Exact Methods

COMPUTER BY R. J. D. SHAHIN

WIND ANALYSIS

CH'D BY K. I. A. D. SHAHIN

HARDY CROSS METHOD

AP'D BY DR. J. A. C. K. N. S. S. S. R.

FINAL MOMENTS

DATE: DECEMBER 1964

SHEET NO. 41

CASE B

Physical Constants

| Joint | K_c | | K_g R | ΣK | Distribution factors | | |
|-------|--------|--------|------------|------------|----------------------|------|------|
| | I | S | | | I | R | S |
| 20 | 0.97 | 0 | 7.40 | 8.37 | 0.12 | 0.88 | 0 |
| 19 | 0.97 | 0.97 | 7.40 | 9.34 | 0.11 | 0.78 | 0.11 |
| 18 | 3.33 | 0.97 | 7.40 | 11.70 | 0.28 | 0.63 | 0.09 |
| 17 | 11.30 | 3.33 | 7.40 | 21.93 | 0.51 | 0.34 | 0.15 |
| 16 | 20.30 | 11.30 | 12.80 | 44.30 | 0.46 | 0.29 | 0.25 |
| 15 | 33.80 | 20.30 | 12.80 | 66.90 | 0.51 | 0.19 | 0.30 |
| 14 | 51.50 | 33.80 | 12.80 | 98.10 | 0.53 | 0.13 | 0.34 |
| 13 | 76.00 | 51.50 | 12.80 | 139.30 | 0.54 | 0.09 | 0.37 |
| 12 | 105.00 | 76.00 | 20.30 | 200.30 | 0.53 | 0.10 | 0.37 |
| 11 | 162.50 | 105.00 | 20.30 | 287.30 | 0.56 | 0.08 | 0.36 |
| 10 | 210.00 | 162.00 | 20.30 | 392.30 | 0.54 | 0.05 | 0.41 |
| 9 | 270.00 | 210.00 | 20.30 | 496.30 | 0.54 | 0.04 | 0.42 |
| 8 | 373.00 | 270.00 | 30.50 | 669.50 | 0.55 | 0.05 | 0.40 |
| 7 | 460.00 | 373.00 | 30.50 | 863.50 | 0.53 | 0.04 | 0.43 |
| 6 | 550.00 | 460.00 | 30.50 | 1040.50 | 0.53 | 0.03 | 0.44 |
| 5 | 710.00 | 550.00 | 30.50 | 1280.50 | 0.53 | 0.03 | 0.43 |
| 4 | 980.00 | 710.00 | 43.20 | 1723.20 | 0.57 | 0.03 | 0.40 |
| 3 | 980.00 | 980.00 | 43.20 | 2003.20 | 0.49 | 0.02 | 0.49 |
| 2 | 680.00 | 980.00 | 43.20 | 1703.20 | 0.40 | 0.03 | 0.57 |
| 1 | 740.00 | 680.00 | 43.20 | 1463.20 | 0.51 | 0.03 | 0.46 |

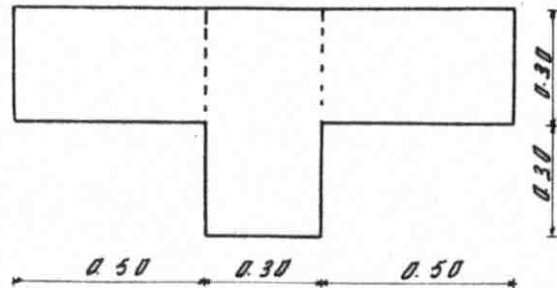
| Joint a | K _{g1} | K _c | K _{g1} | K _{g2} | K _c | ΣK | Distribution factors | | | |
|------------|-----------------|----------------|-----------------|-----------------|----------------|---------|----------------------|------|------|------|
| | | S | L | R | I | | S | L | R | I |
| 20 | 4.80 | 0 | 7.40 | 7.20 | 0.97 | 15.57 | 0 | 0.47 | 0.46 | 0.07 |
| 19 | 4.80 | 0.97 | 7.40 | 7.20 | 1.92 | 21.49 | 0.04 | 0.34 | 0.33 | 0.09 |
| 18 | 4.80 | 1.92 | 7.40 | 7.20 | 5.25 | 21.77 | 0.09 | 0.34 | 0.33 | 0.24 |
| 17 | 4.80 | 5.25 | 7.40 | 7.20 | 11.30 | 31.15 | 0.17 | 0.24 | 0.23 | 0.36 |
| 16 | 8.30 | 11.30 | 12.80 | 12.45 | 20.30 | 56.85 | 0.20 | 0.22 | 0.22 | 0.36 |
| 15 | 8.30 | 20.30 | 12.80 | 12.45 | 33.80 | 79.25 | 0.35 | 0.16 | 0.16 | 0.49 |
| 14 | 8.30 | 33.80 | 12.80 | 12.45 | 63.00 | 122.05 | 0.28 | 0.11 | 0.10 | 0.51 |
| 13 | 8.30 | 63.00 | 12.80 | 12.45 | 89.00 | 176.25 | 0.36 | 0.07 | 0.07 | 0.50 |
| 12 | 13.10 | 89.00 | 20.30 | 19.65 | 123.00 | 251.95 | 0.36 | 0.08 | 0.08 | 0.49 |
| 11 | 13.10 | 123.00 | 20.30 | 19.65 | 162.00 | 324.95 | 0.38 | 0.06 | 0.06 | 0.50 |
| 10 | 13.10 | 162.00 | 20.30 | 19.65 | 238.00 | 439.95 | 0.37 | 0.05 | 0.04 | 0.54 |
| 9 | 13.10 | 162.00 | 20.30 | 19.65 | 298.00 | 570.95 | 0.41 | 0.04 | 0.03 | 0.52 |
| 8 | 19.60 | 298.00 | 30.50 | 29.40 | 412.00 | 764.90 | 0.38 | 0.04 | 0.04 | 0.54 |
| 7 | 19.60 | 412.00 | 30.50 | 29.40 | 500.00 | 971.90 | 0.42 | 0.03 | 0.03 | 0.52 |
| 6 | 19.60 | 500.00 | 30.50 | 29.40 | 600.00 | 1159.90 | 0.43 | 0.03 | 0.02 | 0.52 |
| 5 | 19.60 | 600.00 | 30.50 | 29.40 | 770.00 | 1415.90 | 0.42 | 0.02 | 0.02 | 0.54 |
| 4 | 28.00 | 770.00 | 43.00 | 42.00 | 980.00 | 1821.20 | 0.42 | 0.02 | 0.02 | 0.54 |
| 3 | 28.00 | 980.00 | 43.00 | 42.00 | 980.00 | 2045.20 | 0.48 | 0.02 | 0.02 | 0.48 |
| 2 | 28.00 | 980.00 | 43.00 | 42.00 | 680.00 | 1745.20 | 0.36 | 0.03 | 0.02 | 0.39 |
| 1 | 88.00 | 680.00 | 43.00 | 42.00 | 740.00 | 1505.20 | 0.45 | 0.03 | 0.03 | 0.49 |

N.B. No analysis is conducted for this case for reasons which were discussed in chapter 7 (Text.)

CASE C

I Values For Beams

1. Sample Calculation



| | $A \text{ (m}^2\text{)}$ | $S_x \text{ (m}^3\text{)}$ | $I \text{ (m}^4\text{)}$ |
|--------------|---------------------------|--|--|
| | $b \times d$ | $\frac{bd^2}{8} = bd \left(\frac{d}{8}\right)$ | $\frac{bd^3}{3} = \left(\frac{bd^2}{8}\right) \left(\frac{2}{3}d\right)$ |
| | $0.30 \times 0.60 = 0.18$ | $0.18 \times 0.30 = 0.054$ | $0.054 \times \frac{2}{3} \times 0.60 = 0.0216$ |
| | $1.00 \times 0.30 = 0.30$ | $0.30 \times 0.15 = 0.045$ | $0.045 \times \frac{2}{3} \times 0.30 = 0.0090$ |
| Total | 0.48 | 0.099 | 0.0306 |

$$x_g = \frac{\sum S_x}{\sum A} = \frac{0.099}{0.48} = 0.206$$

$$\sum A \bar{x}_g^2 = 0.48 \times 0.206^2 = 0.48 \times 0.0424 = 0.0204 \text{ m}^4$$

$$I_{N.A} = 0.0306 - 0.0204 = 0.0102$$

$$(1) K_{g1} = \frac{0.0102}{4.20} = 0.0024$$

$$(2) K_{g1} (Rel) = 24$$

$$(1) K_{g2} = \frac{0.0102}{6.50} = 0.00154$$

$$(2) K_{g2} (Rel) = 15.40$$

N.B

(1) - K_{g1} represents the stiffness of the exterior beam whereas K_{g2} represents the stiffness of the central beam

(2) The relative values of K are multiplied by a factor of 10^4

2. Tabulated Results

| Floor | Dimensions b x d (m x m) | Overhangs (m) | A (m ²) | Sx (m ³) | I (m ⁴) | xg (m) | A · xg ² (m ⁴) | Kg ₁ | | Kg ₂ | |
|-------|--------------------------------|------------------|------------------------|-------------------------|------------------------|-----------|--|-----------------|--------|-----------------|-------|
| | | | | | | | | Abs. | Rel. | Abs. | Rel. |
| 20-17 | 0.30 x 0.60 | 1.00 | 0.48 | 0.099 | 0.0306 | 0.206 | 0.0206 | 0.0024 | 24.00 | 0.00154 | 15.40 |
| 16-13 | 0.30 x 0.70 | " | 0.51 | 0.1182 | 0.0432 | 0.232 | 0.0275 | 0.00373 | 37.30 | 0.00242 | 24.20 |
| 12-9 | 0.30 x 0.80 | " | 0.54 | 0.1410 | 0.0602 | 0.261 | 0.0368 | 0.00558 | 55.80 | 0.00360 | 36.00 |
| 8-5 | 0.30 x 0.90 | " | 0.57 | 0.1660 | 0.0816 | 0.291 | 0.0484 | 0.0079 | 79.00 | 0.00510 | 51.00 |
| 4-1 | 0.30 x 1.00 | " | 0.60 | 0.1950 | 0.1090 | 0.325 | 0.0636 | 0.0108 | 108.00 | 0.00700 | 70.00 |

K Values For Columns

The column sizes will be changed every four floors and will be taken as

50 x 40, 50 x 60, 50 x 80, 50 x 100, 50 x 120 cms

| Story | b/l_2 (m) | d^3 | bd^3 | l (m) | $K = I/l^3$ | $K(Rel)$ |
|-------|-------------|-------|---------|------------|-------------|----------|
| 20-16 | 0.0416 | 0.064 | 0.00268 | 3.40 | 0.00077 | 7.70 |
| 16-12 | " | 0.216 | 0.00900 | " | 0.00264 | 26.40 |
| 12-8 | " | 0.512 | 0.0213 | " | 0.00685 | 68.50 |
| 8-4 | " | 1.00 | 0.0416 | " | 0.01220 | 122.00 |
| 4-2 | " | 1.728 | 0.0720 | " | 0.02110 | 211.00 |
| 2-1 | " | " | " | 4.90 | 0.01470 | 147.00 |
| 1-0 | " | " | " | 4.50 | 0.01600 | 160.00 |

Physical Constants Assuming No Hinges In Columns

| Joint | Kg. | Kc | | ΣK | Distribution Factors | | | F.E.M. (T-m) | |
|------------|--------|--------|-------|------------|----------------------|------|------|---------------|------------------------|
| | | I | S | | | | | $\frac{6}{l}$ | $-\frac{6EK\Delta}{l}$ |
| 20 | 24 | 7.70 | 0 | 31.70 | 0.24 | 0.76 | 0 | 1.76 | - 13.50 |
| 19, 18, 17 | 24 | 7.70 | 7.70 | 39.40 | 0.20 | 0.60 | 0.20 | " | - " |
| 16 | 37.30 | 26.40 | " | 71.40 | 0.37 | 0.52 | 0.11 | " | - 46.50 |
| 15, 14, 13 | " | " | 26.40 | 90.10 | 0.29 | 0.42 | 0.29 | " | - " |
| 12 | 55.80 | 62.50 | " | 144.70 | 0.43 | 0.39 | 0.18 | " | - 110.00 |
| 11, 10, 9 | " | " | 62.50 | 180.80 | 0.34 | 0.32 | 0.34 | " | - " |
| 8 | 79.00 | 122.00 | " | 263.50 | 0.46 | 0.30 | 0.24 | " | - 214.00 |
| 7, 6, 5 | " | " | 122 | 323.00 | 0.38 | 0.24 | 0.38 | " | - " |
| 4 | 108.00 | 211.00 | " | 441.00 | 0.48 | 0.24 | 0.28 | " | - 370.00 |
| 3 | " | " | 211 | 530.00 | 0.40 | 0.20 | 0.40 | " | - " |
| 2 | " | 147.00 | " | 466.00 | 0.32 | 0.23 | 0.45 | 1.22 | - 179.00 |
| 1 | " | 160.00 | 147 | 415.00 | 0.39 | 0.26 | 0.35 | 1.33 | - 213.00 |

N.B The value of $E\Delta$ is taken as 10^4 , and its value is omitted because the relative K 's have been already multiplied by 10^4

| Joint (a) | Kg _s | Kc | Kg _i | Kg _(Mod) | Kc | ΣK | Distribution Factors | | | |
|-----------------|-----------------|--------|-----------------|---------------------|--------|--------|----------------------|------|------|------|
| | | S | L | R | I | | S | L | R | I |
| 20 _a | 15.40 | 0 | 24 | 23.00 | 7.70 | 54.70 | 0 | 0.44 | 0.42 | 0.14 |
| 19, 18, 17 | " | 7.70 | " | " | " | 62.40 | 0.12 | 0.39 | 0.37 | 0.18 |
| 16 | 24.20 | " | 37.30 | 36.20 | 26.40 | 107.60 | 0.07 | 0.35 | 0.34 | 0.24 |
| 15, 14, 13 | " | 26.40 | " | " | " | 126.30 | 0.21 | 0.30 | 0.28 | 0.21 |
| 12 | 36.00 | " | 55.80 | 53.90 | 62.50 | 198.60 | 0.13 | 0.28 | 0.27 | 0.32 |
| 11, 10, 9 | " | 62.50 | " | " | " | 234.70 | 0.27 | 0.24 | 0.23 | 0.26 |
| 8 | 51.00 | " | 79.00 | 76.20 | 122.00 | 339.70 | 0.18 | 0.23 | 0.23 | 0.36 |
| 7, 6, 5 | " | 122.00 | " | " | " | 339.20 | 0.30 | 0.20 | 0.20 | 0.30 |
| 4 | 70.00 | " | 108.00 | 105.00 | 211.00 | 546.00 | 0.22 | 0.20 | 0.19 | 0.39 |
| 3 | " | 211.00 | " | " | " | 635.00 | 0.33 | 0.17 | 0.17 | 0.33 |
| 2 | " | " | " | " | 147.00 | 571.00 | 0.37 | 0.19 | 0.18 | 0.26 |
| 1 | " | 147.00 | " | " | 160.00 | 520.00 | 0.28 | 0.21 | 0.20 | 0.31 |

Physical Constants Assuming Hinges At Mid-Height of Columns

(Excluding Two Top Most Columns)

| Joint | K _c (Mod) I | K _g R | K _c S | Σ K | Distribution factors | | | FEM (T-m) |
|-------|---------------------------|---------------------|---------------------|--------|----------------------|------|------|--------------|
| | | | | | I | R | S | |
| 18 | 11.50 | 24.00 | 7.70 | 43.20 | 0.26 | 0.56 | 0.18 | - 27 |
| 17 | " | " | " | " | " | " | " | - " |
| 16 | 39.50 | 37.30 | " | 84.50 | 0.47 | 0.44 | 0.09 | - 99 |
| 15 | " | " | 26.40 | 103.20 | 0.38 | 0.36 | 0.26 | - " |
| 14 | " | " | " | " | " | " | " | - " |
| 13 | " | " | " | " | " | " | " | - " |
| 12 | 92.30 | 55.80 | " | 175.50 | 0.53 | 0.32 | 0.15 | - 220 |
| 11 | " | " | 62.50 | 211.60 | 0.44 | 0.27 | 0.29 | - " |
| 10 | " | " | " | " | " | " | " | - " |
| 9 | " | " | " | " | " | " | " | - " |
| 8 | 183.00 | 79.00 | " | 324.50 | 0.56 | 0.25 | 0.19 | - 428 |
| 7 | " | " | 122.00 | 384.00 | 0.47 | 0.21 | 0.32 | - " |
| 6 | " | " | " | " | " | " | " | - " |
| 5 | " | " | " | " | " | " | " | - " |
| 4 | 315.00 | 108.00 | " | 545.00 | 0.58 | 0.20 | 0.22 | - 740 |
| 3 | " | " | 211.00 | 634.00 | 0.50 | 0.17 | 0.33 | - " |
| 2 | 220.00 | " | " | 539.00 | 0.41 | 0.20 | 0.39 | - 358 |
| 1 | 240.00 | " | 147.00 | 495.00 | 0.48 | 0.22 | 0.30 | - 426 |

N.B (FEM)₂ = -3EK₂ $\frac{\Delta}{L_2}$, K₂ = $\frac{I}{L_2^3} = \frac{2I}{L_1^3} = 2K$
(FEM)₂ = -3E x 2K x $\frac{\Delta}{L_1}$ x 2 = - $\frac{12EK\Delta}{L_1} = - \frac{2EK\Delta}{L_1}$

| Joint (a) | K-Values | | | | ΣK | Distribution Factors | | | |
|--------------|----------|--------|--------|--------|------------|----------------------|------|------|------|
| | S | L | R | I | | S | L | R | I |
| 18, 17 | 7.70 | 24 | 23 | 11.50 | 66.20 | 0.12 | 0.36 | 0.35 | 0.17 |
| 16 | " | 37.30 | 36.80 | 39.50 | 120.70 | 0.06 | 0.31 | 0.30 | 0.33 |
| 15, 14, 13 | 26.40 | " | " | " | 139.40 | 0.19 | 0.27 | 0.26 | 0.28 |
| 12 | " | 55.80 | 53.90 | 93.30 | 229.40 | 0.12 | 0.24 | 0.24 | 0.40 |
| 11, 10, 9 | 62.50 | " | " | " | 265.50 | 0.24 | 0.21 | 0.20 | 0.35 |
| 8 | " | 79.00 | 76.20 | 183.00 | 400.70 | 0.16 | 0.20 | 0.19 | 0.45 |
| 7, 6, 5 | 122.00 | " | " | " | 460.20 | 0.26 | 0.17 | 0.17 | 0.40 |
| 4 | " | 108.00 | 105.00 | 315.00 | 650.00 | 0.19 | 0.17 | 0.16 | 0.48 |
| 3 | 211.00 | " | " | " | 739.00 | 0.28 | 0.15 | 0.15 | 0.42 |
| 2 | " | " | " | 220.00 | 644.00 | 0.33 | 0.17 | 0.16 | 0.34 |
| 1 | 147.00 | " | " | 240.00 | 600.00 | 0.25 | 0.18 | 0.17 | 0.40 |

Physical Constants At Top Most Floors When Going One Floor Lower

| Joint | Kc | Kg | ΣK | Distribution Factors | | |
|------------|--------|--------|--------|----------------------|------|---|
| | I | R | | I | R | S |
| 19, 18, 17 | 7.70 | 24 | 31.70 | 0.24 | 0.76 | 0 |
| 16 | 26.40 | 37.30 | 63.70 | 0.42 | 0.58 | " |
| 15, 14, 13 | " | " | " | " | " | " |
| 12 | 62.50 | 55.80 | 118.30 | 0.53 | 0.47 | " |
| 11, 10, 9 | " | " | " | " | " | " |
| 8 | 122.00 | 79.00 | 201.00 | 0.61 | 0.39 | " |
| 7, 6, 5 | " | " | " | " | " | " |
| 4 | 211.00 | 108.00 | 319.00 | 0.66 | 0.34 | " |
| 3 | " | " | " | " | " | " |

| Joint (a) | Kc | Kg ₁ | Kg ₁ (Mod) | Kc | ΣK | Distribution Factors | | | |
|--------------|----|-----------------|-----------------------|--------|--------|----------------------|------|------|------|
| | S | L | R | I | | S | L | R | I |
| 19, 18, 17 | 0 | 24.00 | 23.00 | 7.70 | 54.70 | 0 | 0.44 | 0.42 | 0.14 |
| 16 | " | 37.30 | 36.20 | 26.40 | 99.90 | " | 0.37 | 0.36 | 0.27 |
| 15, 14, 13 | " | " | " | " | " | " | " | " | " |
| 12 | " | 55.80 | 53.90 | 62.50 | 172.20 | " | 0.32 | 0.32 | 0.36 |
| 11, 10, 9 | " | " | " | " | " | " | " | " | " |
| 8 | " | 79.00 | 76.20 | 122.00 | 277.20 | " | 0.29 | 0.27 | 0.44 |
| 7, 6, 5 | " | " | " | " | " | " | " | " | " |
| 4 | " | 108.00 | 105.00 | 211.00 | 424.00 | " | 0.25 | 0.25 | 0.50 |
| 3 | " | " | " | " | " | " | " | " | " |

20-19-18 Floors

1. Shears

$$V_{18} = -\frac{2}{1.70} (-30 + 0) = -\frac{2}{1.70} (-0.30) = +0.35 = +0.35 \times \frac{\Delta 20}{10^4}$$

$$V_{19} = -\frac{2}{3.40} (+0.90 + 1.90 + 0.50 + 1.10) = -\frac{2}{3.40} (+3.40) = -2 = -2 \times \frac{\Delta 20}{10^4}$$

$$V_{20} = -\frac{2}{3.40} (-10.10 - 9.90 - 11.70 - 11.70) = -\frac{2}{3.40} (-43.40) = +25.60 = +25.60 \times \frac{\Delta 20}{10^4}$$

$$V_{18} = -\frac{2}{1.70} (+2.70 + 1.60) = -\frac{2}{1.70} (+4.30) = -5.06 = -5.06 \times \frac{\Delta 19}{10^4}$$

$$V_{19} = -\frac{2}{3.40} (-10.40 - 10.40 - 11.70 - 11.70) = -\frac{2}{3.40} (-44.20) = +26 = +26 \times \frac{\Delta 19}{10^4}$$

$$V_{20} = -\frac{2}{3.40} (+2.00 + 0.90 + 1.10 + 0.60) = -\frac{2}{3.40} (+4.60) = -2.70 = -2.70 \times \frac{\Delta 19}{10^4}$$

$$V_{18} = -\frac{2}{1.70} (-20.90 - 23.60) = -\frac{2}{1.70} (-44.50) = +52.30 = 52.30 \times \frac{\Delta 18}{10^4}$$

$$V_{19} = -\frac{2}{3.40} (+4.10 + 1.70 + 2.40 + 1.20) = -\frac{2}{3.40} (+9.40) = -5.52 = -5.52 \times \frac{\Delta 18}{10^4}$$

$$V_{20} = -\frac{2}{3.40} (-0.40 - 0.20 - 0.10) = -\frac{2}{3.40} (-0.70) = +0.41 = +0.41 \times \frac{\Delta 18}{10^4}$$

2. Δ's

$$+0.35 \Delta 20 - 5.06 \Delta 19 + 52.30 \Delta 18 = 9.20 \times 10^4$$

$$-2 \Delta 20 + 26 \Delta 19 - 5.52 \Delta 18 = 5.55 \times 10^4$$

$$+25.60 \Delta 20 - 2.70 \Delta 19 + 0.41 \Delta 18 = 1.85 \times 10^4$$

$$\Delta 18 = 0.175 \times 10^4 - 0.00665 \Delta 20 + 0.0962 \Delta 19$$

$$\Delta 19 = 0.213 \times 10^4 + 0.077 \Delta 20 + 0.213 \Delta 18$$

$$\Delta 20 = 0.0722 \times 10^4 + 0.105 \Delta 19 - 0.016 \Delta 18$$

$$\text{Let } \Delta_{19} = 20.0$$

$$\Delta_{18} = 0.17 \times 10^4$$

$$\Delta_{19} = 0.813 \times 10^4 + 0 + 0.813 \times 0.175 \times 10^4 = 10^4(0.813 + 0.142) = 0.955 \times 10^4$$

$$\Delta_{20} = 0.0722 + 0.105 \times 0.955 - 0.016 \times 1.75 = 0.0722 + 0.100275 - 0.028 = 0.094475$$

$$\Delta_{18} = 0.175 - 0.00665 \times 0.094475 + 0.0962 \times 0.25 = 0.175 - 0.000628 + 0.02405 = 0.198422$$

$$\Delta_{19} = 0.213 + 0.077 \times 0.955 + 0.213 \times 0.198 = 0.213 + 0.073535 + 0.042174 = 0.328709$$

$$\Delta_{20} = 0.0722 + 0.105 \times 0.328709 - 0.016 \times 0.198 = 0.0722 + 0.034514 - 0.003168 = 0.099546$$

$$\Delta_{18} = 0.175 - 0.00665 \times 0.099546 + 0.0962 \times 0.26 = 0.175 - 0.000661 + 0.025012 = 0.200351$$

$$\Delta_{19} = 0.213 + 0.077 \times 0.99546 + 0.213 \times 0.200 = 0.213 + 0.076650 + 0.042600 = 0.332250$$

$$\Delta_{20} = 0.0722 + 0.105 \times 0.332250 - 0.016 \times 0.200 = 0.0722 + 0.034886 - 0.003200 = 0.099886$$

N. B Because 10^4 is always a common factor, it is omitted tentatively.

19-18-17 Floors

1 Shears (Same as previous case)

2 Effect of 20th Floor

$$V_{17} = 0$$

$$V_{18} = -\frac{2}{3.40} (0 - 0.01) = \frac{0.02}{3.40} = 0.006$$

$$V_{19} = -\frac{2}{3.40} (+0.03 + 0.09 + 0.10 + 0.04) = \frac{-2}{3.40} \times 0.26 = \frac{-0.52}{3.40} = -0.153$$

3 Δ 's

$$+ 0.35 \Delta_{19} - 5.06 \Delta_{18} + 52.30 \Delta_{17} = (12+0) 10^4$$

$$- 2 \Delta_{19} + 26 \Delta_{18} - 5.52 \Delta_{17} = (9.20 + 0.006) 10^4$$

$$+ 25.60 \Delta_{19} - 870 \Delta_{18} + 0.41 \Delta_{17} = (5.55 - 0.15) 10^4$$

$$\Delta_{17} = 0.244 \times 10^4 - 0.00665 \Delta_{19} + 0.0962 \Delta_{18}$$

$$\Delta_{18} = 0.344 \times 10^4 + 0.077 \Delta_{19} + 0.213 \Delta_{17}$$

$$\Delta_{19} = 0.211 \times 10^4 + 0.105 \Delta_{18} - 0.016 \Delta_{17}$$

Let $\Delta_{19} = \Delta_{18} = 0$

$$\Delta_{17} = 0.244 \times 10^4$$

$$\Delta_{18} = 0.344 + 0.077 \times 0.213 \times 0.244 = 0.344 + 0.0052 = 0.349$$

$$\Delta_{19} = 0.211 + 0.105 \times 0.349 - 0.016 \times 0.244 = 0.211 + 0.042 - 0.004 = 0.249$$

$$\Delta_{17} = 0.244 - 0.00665 \times 0.249 + 0.0962 \times 0.349 = 0.244 - 0.0017 + 0.038 = 0.280$$

$$\Delta_{18} = 0.344 + 0.077 \times 0.249 + 0.213 \times 0.280 = 0.344 + 0.019 + 0.060 = 0.423$$

$$\Delta_{19} = 0.211 + 0.105 \times 0.423 - 0.016 \times 0.280 = 0.211 + 0.044 - 0.005 = 0.250$$

$$\Delta_{17} = 0.244 - 0.00665 \times 0.250 + 0.0962 \times 0.423 = 0.244 - 0.0017 + 0.041 = 0.283$$

$$\Delta_{18} = 0.344 + 0.077 \times 0.250 + 0.213 \times 0.283 = 0.344 + 0.019 + 0.060 = 0.423$$

$$\Delta_{19} = 0.211 + 0.105 \times 0.423 - 0.016 \times 0.283 = 0.211 + 0.045 - 0.005 = 0.250$$

| JOINT MEMBER | 16 | | | 17 | | | 18 | | | 18B | | | 17B | | | 16B | | | |
|------------------------------------|------|--------|--------|--------|--------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|--------|-------|-------|-------|
| | I | R | S | I | R | S | I | R | L | R | I | S | L | R | I | S | L | R | I |
| DIST FACTOR | 0.47 | 0.44 | 0.09 | 0.20 | 0.60 | 0.20 | 0.24 | 0.76 | 0.44 | 0.42 | 0.14 | 0.12 | 0.39 | 0.37 | 0.12 | 0.06 | 0.31 | 0.30 | 0.33 |
| Influence of Δ 18 | | +1.40 | +2.70 | +8.10 | +2.70 | +1.40 | +3.00 | +5.90 | +5.70 | +1.90 | +1.00 | +4.10 | | | | | | | |
| | | -0.30 | -0.60 | -1.70 | -0.30 | -0.90 | -1.80 | -1.70 | -0.30 | -0.90 | | | | | | | | | |
| | | -0.50 | -0.50 | -0.10 | 0 | +0.30 | +0.20 | +0.30 | +0.90 | 0 | +0.10 | +0.50 | +0.10 | 0 | +0.50 | 0 | -0.30 | | |
| | | -0.50 | -0.50 | +1.00 | +2.00 | +0.10 | 10.10 | -9.90 | +9.90 | | | | | | | | | | |
| Influence of Δ 17 | | +6.30 | +5.90 | +1.30 | -13.50 | +0.70 | +2.70 | | | | | | | | | | | | |
| | | +1.50 | +1 | +2 | +6.10 | +2 | +1 | | | | | | | | | | | | |
| | | -1.20 | -1.10 | -0.20 | -0.10 | -0.70 | -0.10 | -0.20 | -0.80 | -0.40 | -0.20 | -0.40 | -1.30 | -1.30 | -0.40 | -0.20 | -0.60 | | |
| | | +0.10 | +0.10 | +0.10 | +0.20 | -0.50 | +0.20 | +0.10 | -0.10 | -0.10 | 0 | +0.30 | +0.30 | 0 | +0.10 | +0.20 | +0.20 | +0.30 | |
| Influence of Δ 16 | | +5.00 | +6.30 | -11.30 | +0.70 | +0.60 | +2.00 | +0.90 | -0.90 | -0.30 | +0.60 | +1.20 | +7.30 | +3.60 | -0.10 | -12.20 | +5.60 | 13.10 | +3.50 |
| | | -93 | | | | | | | | | | | | | | | | | |
| | | +43.60 | +41.00 | +8.40 | +4.20 | | | | | | | | | | | | | | |
| | | -5.30 | -5.00 | -1.00 | -0.50 | | | | | | | | | | | | | | |
| Influence of Moment of Above Floor | | 0 | 0 | 0 | +0.40 | -0.40 | -0.70 | -2.20 | -0.80 | -0.40 | +0.10 | +0.30 | +0.20 | -0.10 | -0.10 | -0.10 | -0.10 | -0.10 | |
| | | -54.70 | +47.00 | +7.00 | +3.00 | -2.20 | -0.80 | -0.30 | +0.30 | -0.10 | -0.10 | -0.10 | -0.10 | -0.10 | -0.10 | -0.10 | -0.10 | -0.10 | |
| | | | | | | | | | | | | | | | | | | | |
| | | | | | | | | | | | | | | | | | | | |
| Final Moments | | -0.20 | +2.82 | -8.23 | -5.61 | | | | | | | | | | | | | | |
| | | | | | | | | | | | | | | | | | | | |
| | | | | | | | | | | | | | | | | | | | |
| | | | | | | | | | | | | | | | | | | | |

Checking Results:

$$R_1 + R_2 = \frac{5.61 + 8.36}{1.70} = 8.20$$

$$\sum F_x = 16.40 - 2x \times 20 = 0$$

O.K.

ANALYSIS OF THE EFFECT OF WIND ON A HIGH REINFORCED CONCRETE BUILDING

Comparison of Approximate and Exact Methods

| | | |
|----------|-----------------|---------------------|
| COMPUTER | RIAD SHAHIN | WIND ANALYSIS |
| CHK'D BY | RIAD SHAHIN | HARDY CROSS METHOD |
| APP'D BY | DR. JACK MASSER | DATE: DECEMBER 1964 |
| | | SHEET NO. 57 |

18-17-16 Floors

1 Shears

$$V_{16} = \frac{-2}{1.70} (-0.50 - 0.10) = \frac{-2}{1.70} (-0.60) = +0.703 = +0.703 \times \frac{\Delta 18}{10^4}$$

$$V_{17} = \frac{-2}{3.40} (+1.00 + 2.00 + 0.50 + 1.10) = \frac{-2}{3.40} (+4.60) = -2.70 = -2.70 \frac{\Delta 18}{10^4}$$

$$V_{18} = \frac{-2}{3.40} (-10.10 - 9.90 - 11.70 - 11.70) = \frac{-2}{3.40} (-43.40) = 25.50 = 25.50 \frac{\Delta 18}{10^4}$$

$$V_{16} = \frac{-2}{1.70} (+5.00 + 3.50) = \frac{-2}{1.70} (+8.50) = -10 = -10 \frac{\Delta 17}{10^4}$$

$$V_{17} = \frac{-2}{3.40} (-11.30 - 10.70 - 12.20 - 12.10) = \frac{-2}{3.40} (-46.30) = +27.20 = 27.20 \frac{\Delta 17}{10^4}$$

$$V_{18} = \frac{-2}{3.40} (+2.10 + 0.90 + 1.30 + 0.60) = \frac{-2}{3.40} (+4.80) = -2.82 = -2.82 \frac{\Delta 17}{10^4}$$

$$V_{16} = \frac{-2}{1.70} (-54.70 - 68.20) = \frac{-2}{1.70} (-122.90) = +144 = 144 \frac{\Delta 16}{10^4}$$

$$V_{17} = \frac{-2}{3.40} (+7.00 + 3.00 + 4.40 + 2.10) = \frac{-2}{3.40} (+16.50) = -9.70 = -9.70 \frac{\Delta 16}{10^4}$$

$$V_{18} = \frac{-2}{3.40} (-0.80 - 0.30 - 0.10 + 0) = \frac{-2}{3.40} (-1.20) = 0.703 = +0.703 \frac{\Delta 16}{10^4}$$

2 Effect of the 19th floor

$$V_{16} = \frac{-2}{1.70} (0 + 0) = 0$$

$$V_{17} = \frac{-2}{3.40} (-0.01 - 0.02 - 0.01 - 0.01) = \frac{-2}{3.40} (-0.05) = +0.03$$

$$V_{18} = \frac{-2}{3.40} (+0.15 + 0.32 + 0.13 + 0.227) = -\frac{2}{3.40} (0.827) = 0.51$$

3 Δ 's

$$+0.703 \frac{\Delta 18}{10^4} - 10 \frac{\Delta 17}{10^4} + 144 \frac{\Delta 16}{10^4} = (16.40 + 0) = 16.40$$

$$-2.70 \frac{\Delta 18}{10^4} + 27.20 \frac{\Delta 17}{10^4} - 9.70 \frac{\Delta 16}{10^4} = (18.80 + 0.03) = 18.83$$

$$+25.50 \frac{\Delta 18}{10^4} - 2.82 \frac{\Delta 17}{10^4} + 0.703 \frac{\Delta 16}{10^4} = (9.20 - 0.51) = 8.69$$

$$\Delta_{16} = 0.151$$

$$\Delta_{17} = 0.565$$

$$\Delta_{18} = 0.398$$

| JOINT | 15 | | | 16 | | | 17 | | | 17a | | | 16a | | | 15a | | | | | |
|---------------------------------|--------|------|-------|-------|------|------|-------|-------|-------|-------|-------|------|------|------|------|------|------|------|------|---|--|
| | MEMBER | I | R | S | I | R | S | I | R | L | R | I | S | L | R | I | S | L | R | I | |
| DIST FACTOR | 0.38 | 0.36 | 0.26 | 0.37 | 0.52 | 0.11 | 0.24 | 0.76 | 0.44 | 0.42 | 0.14 | 0.07 | 0.35 | 0.34 | 0.24 | 0.19 | 0.27 | 0.26 | 0.28 | | |
| Influence of Δ 17 | | | -1.00 | -0.90 | 0.60 | 0.30 | +1.60 | +1.80 | +2.30 | +7.40 | +3.70 | | | | | | | | | | |
| | | | | | | | | | | | | | | | | | | | | | |
| | | | | | | | | | | | | | | | | | | | | | |
| Influence of Δ 16 | | | | | | | | | | | | | | | | | | | | | |
| | | | | | | | | | | | | | | | | | | | | | |
| | | | | | | | | | | | | | | | | | | | | | |
| Influence of Δ 15 | | | | | | | | | | | | | | | | | | | | | |
| | | | | | | | | | | | | | | | | | | | | | |
| | | | | | | | | | | | | | | | | | | | | | |
| Influence of Moment Above floor | | | | | | | | | | | | | | | | | | | | | |
| | | | | | | | | | | | | | | | | | | | | | |
| | | | | | | | | | | | | | | | | | | | | | |
| Final Moments | | | | | | | | | | | | | | | | | | | | | |
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| | | | | | | | | | | | | | | | | | | | | | |

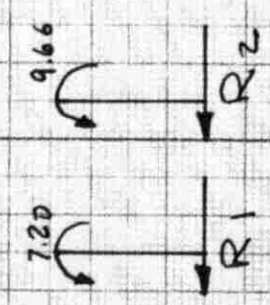
| ANALYSIS OF THE EFFECT OF WIND ON A HIGH REINFORCED CONCRETE BUILDING | | | | | | | | | | | | | | | | | | | | |
|---|--|--|--|--|--|--|--|--|--|---------------------------------|--|--|--|--|--|--|--|--|--|--|
| Comparison of Approximate and Exact Methods | | | | | | | | | | | | | | | | | | | | |
| COMPUTER: RIAO SHAHIN | | | | | | | | | | WIND ANALYSIS | | | | | | | | | | |
| CHK'D BY: RIAO SHAHIN | | | | | | | | | | HARDY CROSS METHOD | | | | | | | | | | |
| APP'D BY: JACK NASSER | | | | | | | | | | DATE: DECEMBER 1964 SHEET NO 59 | | | | | | | | | | |

Checking Results:

$$R_1 + R_2 = \frac{7.20 + 9.66}{1.70} + \frac{16.86}{1.70} = 9.957$$

$$\sum F_x = 19.90 - 2 \times 9.95 = 0$$

∴ O.K.



17-16-15 Floors

1 Shears

$$V_{15} = \frac{-2}{1.70} (-0.80 - 0.20) = \frac{-2}{1.70} (-1.00) = +1.18 = +1.18 \Delta 17/10^4$$

$$V_{16} = \frac{-2}{3.40} (+1.60 + 3.70 + 1.10 + 2.40) = \frac{-2}{3.40} (+8.80) = -5.16 = -5.16 \Delta 17/10^4$$

$$V_{17} = \frac{-2}{3.40} (-11.00 - 10.30 - 12.10 - 11.00) = \frac{-2}{3.40} (+45.80) = +86.50 = +26.50 \Delta 17/10^4$$

$$V_{15} = \frac{-2}{1.70} (+13.30 + 10.10) = \frac{-2}{1.70} (+23.40) = -27.50 = -27.50 \Delta 16/10^4$$

$$V_{16} = \frac{-2}{3.40} (-30.70 - 28.50 - 35.60 - 34.90) = \frac{-2}{3.40} (-129.70) = +76 = 76 \Delta 16/10^4$$

$$V_{17} = \frac{-2}{3.40} (+3.70 + 1.60 + 2.30 + 1.80) = \frac{-2}{3.40} (+8.80) = -5.16 = -5.16 \Delta 16/10^4$$

$$V_{15} = \frac{-2}{1.70} (-61 - 71.10) = \frac{-2}{1.70} (-132.10) = +155 = +155 \Delta 15/10^4$$

$$V_{16} = \frac{-2}{3.40} (+20 + 7.10 + 14.40 + 6.30) = \frac{-2}{3.40} (+47.80) = -28 = -28 \Delta 15/10^4$$

$$V_{17} = \frac{-2}{3.40} (-0.90 - 0.50 - 0.30 - 0.20) = \frac{-2}{3.40} (-1.90) = +1.11 = +1.11 \Delta 15/10^4$$

2 Effect of 18th Floor

$$V_{15} = \frac{-2}{1.70} (+0.02 + 0.01) = \frac{-2}{1.70} (+0.03) = -0.035$$

$$V_{16} = \frac{-2}{3.40} (-0.04 - 0.09 - 0.02 - 0.04) = \frac{-2}{3.40} (-0.19) = +0.11$$

$$V_{17} = \frac{-2}{3.40} (+0.25 + 0.53 + 0.21 + 0.44) = \frac{-2}{3.40} (+1.43) = -0.84$$

3 Δ 's

$$+1.18 \Delta 17 - 27.50 \Delta 16 + 155 \Delta 15 = (19.90 - 0.035) 10^4 = 19.86 \times 10^4$$

$$-5.16 \Delta 17 + 76 \Delta 16 - 28 \Delta 15 = (16.40 + 0.11) 10^4 = 16.51 \times 10^4$$

$$+26.50 \Delta 17 - 5.16 \Delta 16 + 1.11 \Delta 15 = (12.80 - 0.84) 10^4 = 11.96 \times 10^4$$

$$\Delta_{15} = 0.177$$

$$\Delta_{16} = 0.302$$

$$\Delta_{17} = 0.501$$

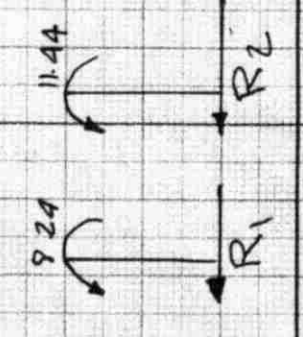
| JOINT MEMBER | 14 | | | 15 | | | 16 | | | 16a | | | 15a | | | 14a | | | | |
|------------------------------------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| | I | R | S | I | R | S | I | R | L | R | I | S | L | R | I | S | L | R | I | |
| DIST. FACTOR | 0.38 | 0.36 | 0.26 | 0.29 | 0.42 | 0.29 | 0.42 | 0.58 | 0.37 | 0.36 | 0.27 | 0.21 | 0.30 | 0.28 | 0.21 | 0.19 | 0.27 | 0.26 | 0.28 | |
| | | | | -46.50 | -46.50 | -46.50 | -46.50 | -46.50 | -46.50 | -46.50 | -46.50 | -46.50 | -46.50 | -46.50 | -46.50 | -46.50 | -46.50 | -46.50 | -46.50 | -46.50 |
| | | | | +7.00 | +10.00 | +19.50 | +27 | +13.50 | | | | | | | | | | | | |
| | | | | +4.30 | +8.60 | +12.40 | +8.50 | +4.30 | +5.20 | +10.40 | +10.10 | +7.60 | +3.90 | +6.20 | | | | | | |
| Influence of Δ 16 | -1.60 | -1.60 | -1.10 | -0.60 | -1.50 | -2.00 | -4.00 | -5.50 | -2.80 | | | | | | | | | | | |
| | | | | +0.60 | +1.20 | +1.70 | +0.60 | +0.70 | +1.40 | +1.40 | +1.10 | +0.60 | +0.90 | | | | | | | |
| | | | | -0.20 | -0.30 | -0.50 | -0.80 | -0.40 | | | | | | | | | | | | |
| | | | | +0.10 | +0.30 | +0.10 | | | +0.20 | +0.20 | +0.20 | +0.20 | +0.20 | +0.20 | +0.20 | +0.20 | +0.20 | +0.20 | +0.20 | +0.20 |
| Influence of Δ 15 | +17.70 | +16.70 | +12.70 | +6.10 | +7.00 | | | | | | | | | | | | | | | |
| | | | | -46.50 | -46.50 | -46.50 | -46.50 | -46.50 | -46.50 | -46.50 | -46.50 | -46.50 | -46.50 | -46.50 | -46.50 | -46.50 | -46.50 | -46.50 | -46.50 | -46.50 |
| | | | | +4.50 | +4.90 | +9.70 | +14.00 | +9.70 | +4.90 | | | | | | | | | | | |
| | | | | -3.60 | -3.40 | -2.40 | -1.20 | -1.10 | -2.10 | -2.80 | -1.40 | -1.10 | -2.10 | -2.90 | -2.10 | -1.10 | -1.70 | | | |
| Influence of Δ 14 | +0.40 | +0.60 | +1.10 | +1.70 | +1.10 | +0.60 | +0.50 | -0.90 | -0.90 | -0.60 | -0.60 | -0.30 | +0.90 | | | | | | | |
| | | | | -0.40 | -0.40 | -0.20 | -0.10 | -0.20 | | | | | | | | | | | | |
| | | | | +0.10 | +0.10 | +0.10 | | | | | | | | | | | | | | |
| | | | | +13.70 | 17.70 | -21.50 | -30.80 | +21 | +9.70 | | | | | | | | | | | |
| Influence of Δ 1A | -93 | | | | | | | | | | | | | | | | | | | |
| | | | | | | | | | | | | | | | | | | | | |
| | | | | | | | | | | | | | | | | | | | | |
| | | | | | | | | | | | | | | | | | | | | |
| Influence of Moment of Above Floor | +0.50 | +0.50 | +0.30 | +0.20 | | | | | | | | | | | | | | | | |
| | | | | | | | | | | | | | | | | | | | | |
| | | | | | | | | | | | | | | | | | | | | |
| | | | | | | | | | | | | | | | | | | | | |
| Final Moments | 61.10 | +40.90 | +20.20 | 0 | +0.10 | 0 | -0.90 | +0.90 | +0.50 | 0 | -0.50 | 0.90 | -1.40 | +6.60 | | | | | | |
| | | | | | | | | | | | | | | | | | | | | |
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| | | | | | | | | | | | | | | | | | | | | |

Check King Results:

$$R_1 + R_2 = \frac{(8.24 + 11.44)}{1.70} = \frac{19.68}{1.70} = 11.60T$$

$$\Sigma F_x = 23.30 - 2 \times 11.60 = 0.10T$$

∴ O.K.



ANALYSIS OF THE EFFECT OF WIND ON A HIGH REINFORCED CONCRETE BUILDING

Comparison of Approximate and Exact Methods

| | |
|---------------------------|---------------------|
| COMPUTER: RIAD SHAHIN | WIND ANALYSIS |
| CHK'D BY: RIAD SHAHIN | HARDY CROSS METHOD |
| APP'D BY: DR. JACK NASSER | DATE: DECEMBER 1964 |
| | SHEET NO 61/ |

16-15-14 Floors

1. Shears

$$V_{14} = \frac{-2}{1.70} (-1.70 - 0.80) = \frac{-2}{1.70} (-2.50) = +2.94 = 2.94 \Delta_{16}/10^4$$

$$V_{15} = \frac{-2}{3.40} (+3.80 + 9.30 + 3.20 + 7.70) = \frac{-2}{3.40} (+24.00) = -14.10 = 14.10 \Delta_{16}/10^4$$

$$V_{16} = \frac{-2}{3.40} (-2.9 - 26.60 - 35.30 - 34.00) = \frac{-2}{3.40} (-24.90) = +73.20 = +73.20 \Delta_{16}/10^4$$

$$V_{14} = \frac{-2}{1.70} (+13.70 + 10.20) = \frac{-2}{1.70} (+23.90) = -28.10 = 28.10 \Delta_{15}/10^4$$

$$V_{15} = \frac{-2}{3.40} (-31.50 - 30.80 - 36 - 35.50) = \frac{-2}{3.40} (-133.80) = +78.50 = 78.50 \Delta_{15}/10^4$$

$$V_{16} = \frac{-2}{3.40} (+9.80 + 3.40 + 7.30 + 3.20) = \frac{-2}{3.40} (+23.70) = -13.90 = 13.90 \Delta_{15}/10^4$$

$$V_{14} = \frac{-2}{1.70} (-61.10 - 71.10) = \frac{-2}{1.70} (-132.20) = +155 = 155 \Delta_{14}/10^4$$

$$V_{15} = \frac{-2}{3.40} (+20.20 + 7.80 + 14.50 + 6.50) = \frac{-2}{3.40} (+49.10) = -28.80 = -28.80 \Delta_{14}/10^4$$

$$V_{16} = \frac{-2}{3.40} (-2.70 - 0.90 - 0.90 - 0.50) = \frac{-2}{3.40} (-5.00) = +2.93 = +2.93 \Delta_{14}/10^4$$

2. Effect of 17th floor.

$$V_{14} = \frac{-2}{1.70} (+0.04 + 0.01) = \frac{-2}{1.70} (+0.05) = -0.06$$

$$V_{15} = \frac{-2}{3.40} (-0.08 - 0.20 - 0.05 - 0.09) = \frac{-2}{3.40} (-0.42) = +0.25$$

$$V_{16} = \frac{-2}{3.40} (+0.59 + 1.50 + 0.50 + 1.12) = \frac{-2}{3.40} (+3.71) = -2.18$$

3. Δ 'S

$$+ 2.94 \Delta_{16} - 28.10 \Delta_{15} + 155 \Delta_{14} = (23.30 - 0.06) 10^4 = 23.24 \times 10^4$$

$$- 14.10 \Delta_{16} + 78.50 \Delta_{15} - 28.80 \Delta_{14} = (19.90 + 0.25) 10^4 = 20.15 \times 10^4$$

$$+ 73.20 \Delta_{16} - 13.90 \Delta_{15} + 2.93 \Delta_{14} = (16.40 - 2.18) 10^4 = 14.20 \times 10^4$$

$$\Delta_{14} = 0.212$$

$$\Delta_{15} = 0.380$$

$$\Delta_{16} = 0.258$$

| JOINT | 13 | | | 14 | | | 15 | | 15a | | 14a | | | | 13a | | | | |
|-----------------------|--------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|--------|-------|-------|-------|-------|-------|-------|--------|
| MEMBER | I | R | S | I | R | S | I | R | L | R | I | S | L | R | I | S | L | R | I |
| DIST. FACTOR | 0.38 | 0.36 | 0.26 | 0.29 | 0.42 | 0.29 | 0.42 | 0.58 | 0.37 | 0.36 | 0.27 | 0.21 | 0.30 | 0.28 | 0.21 | 0.19 | 0.27 | 0.26 | 0.28 |
| Moment of Above Floor | | | | | | | | -4.50 | -6.52 | | | | | | | | | | |
| | | | | | -0.13 | +0.65 | +1.30 | +1.80 | +0.90 | | -0.09 | -0.18 | -0.26 | -0.26 | -0.18 | -0.09 | | | |
| | | | -0.08 | -0.15 | -0.22 | -0.15 | -0.08 | -0.15 | -0.30 | -0.29 | -0.22 | -0.11 | -0.11 | | | | | | |
| | | | | | +0.03 | +0.05 | +0.09 | +0.14 | +0.07 | | +0.03 | +0.05 | +0.06 | +0.06 | +0.05 | +0.03 | | | |
| | | +0.01 | -0.01 | -0.02 | -0.04 | -0.02 | -0.01 | -0.02 | -0.04 | -0.04 | -0.02 | -0.01 | -0.02 | | | 0 | +0.02 | +0.02 | +0.02 |
| | | +0.03 | +0.03 | +0.02 | +0.01 | 0 | 0 | +0.01 | +0.02 | +3.04 | +2.02 | +1.46 | | +0.01 | +0.01 | +0.01 | 0 | +0.02 | 0 |
| Final Moments | +0.03 | +0.04 | -0.07 | -0.16 | -0.37 | +0.53 | +1.31 | +2.99 | | | | +0.63 | -0.32 | -0.19 | -0.12 | -0.06 | +0.03 | +0.02 | +0.01 |
| | -0.53 | | | | | | -9.05 | -8.32 | +8.32 | +7.00 | +3.66 | -10.66 | -4.05 | | | | | | -0.25 |
| | +6.10 | | | | | | +4.35 | +1.51 | -1.51 | -1.02 | -0.40 | +1.42 | +3.25 | | | | | | +4.55 |
| | -15.00 | | | | | | -0.66 | -0.22 | +0.22 | +0.12 | 0 | -0.12 | -0.22 | | | | | | -17.50 |
| | -9.43 | | | | | | -5.36 | -7.03 | +7.03 | +6.10 | +3.26 | -9.36 | -8.02 | | | | | | 13.20 |

Checking Results:

$$R_1 + R_2 = \frac{9.43}{1.70} + \frac{17.65}{1.70} = \frac{27.08}{1.70} = 15.93T$$

$$\sum F_x = 26.70 - 2 \times 13.35 = 0T$$

∴ O.K.



ANALYSIS OF THE EFFECT OF WIND ON A HIGH REINFORCED CONCRETE BUILDING

Comparison of Approximate and Exact Methods

| | | |
|------------|-----------------|---------------------|
| COMPUTER : | RIAD SHAHIN | WIND ANALYSIS |
| CHK'D BY : | RIAD SHAHIN | HARDY CROSS METHOD |
| APP'D BY : | DR. JACK NASSER | DATE: DECEMBER 1964 |
| | | SHEET N° 63 / |

15-14-13 Floors

1 Shears (same as previous case)

2 Effect of 16th floor

$$V_{13} = \frac{-2}{1.70} (+0.03 + 0.01) = \frac{-2}{1.70} (+0.04) = -0.05$$

$$V_{14} = \frac{-2}{3.40} (-0.07 - 0.16 - 0.06 - 0.12) = \frac{-2}{3.40} (-0.41) = +0.24$$

$$V_{15} = \frac{-2}{3.40} (+0.53 + 1.31 + 0.63 + 1.46) = \frac{-2}{3.40} (+3.93) = -2.30$$

3 Δ 's

$$+ 2.94 \Delta_{15} - 28.10 \Delta_{14} + 15.5 \Delta_{13} = (26.70 - 0.05) 10^4 = 26.65 \times 10^4$$

$$- 14.10 \Delta_{15} + 78.50 \Delta_{14} - 28.80 \Delta_{13} = (23.30 + 0.24) 10^4 = 23.54 \times 10^4$$

$$+ 73.20 \Delta_{15} - 13.90 \Delta_{14} + 8.93 \Delta_{13} = (19.90 - 2.30) 10^4 = 17.60 \times 10^4$$

$$\Delta_{13} = 0.245$$

$$\Delta_{14} = 0.446$$

$$\Delta_{15} = 0.314$$

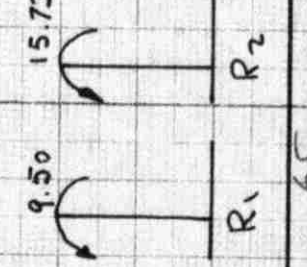
| JOINT | 12 | | | 13 | | | 14 | | | 14a | | | 13a | | | 12a | | | |
|---------------------------------|------|---------|--------|--------|--------|--------|--------|-------|--------|--------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| | I | R | S | I | R | S | I | R | L | R | I | S | L | R | I | S | L | R | I |
| DIST FACTOR | 0.53 | 0.32 | 0.15 | 0.29 | 0.42 | 0.29 | 0.42 | 0.58 | 0.37 | 0.36 | 0.27 | 0.21 | 0.30 | 0.28 | 0.21 | 0.12 | 0.24 | 0.24 | 0.40 |
| Influence of Δ 14 | | | +4.30 | +8.60 | +12.40 | +8.50 | +4.30 | +5.20 | +10.90 | +10.10 | +7.60 | +3.80 | +6.20 | | | | | | |
| | | -2.30 | -1.40 | -0.60 | -0.30 | -1.50 | -2.00 | -4.00 | -5.50 | -2.80 | -1.10 | -2.10 | -3.00 | -2.80 | -2.10 | -1.10 | -0.70 | | |
| | | -0.40 | +0.60 | +1.10 | +1.60 | +1.10 | +0.60 | +0.70 | +1.40 | +1.40 | +1.10 | +0.60 | +0.80 | | | | | | |
| | | -0.10 | -0.10 | 0 | -0.20 | -0.30 | -0.50 | -0.80 | -0.40 | -0.40 | -0.20 | -0.30 | -0.30 | -0.30 | -0.30 | -0.20 | -0.20 | | |
| Influence of Δ 13 | | -2.40 | -1.90 | +4.30 | +0.20 | +0.20 | +0.10 | 0 | +0.20 | +0.20 | +0.20 | +0.10 | +0.10 | | | | | | |
| | | | | +9.60 | +14.50 | +9.10 | 0 | -0.10 | +22.30 | +11.70 | -34 | 0 | -0.10 | -0.10 | 0 | +3.20 | -1.30 | -0.70 | -1.20 |
| | | | | -26.60 | +26.60 | | | | | | | | | | | | | | |
| | | | | | | | | | | | | | | | | | | | |
| Influence of Δ 12 | | +24.50 | +15.00 | +7.00 | -46.50 | +3.50 | +7.00 | | | | | | | | | | | | |
| | | +4.10 | +5.10 | +10.30 | +15.40 | +10.30 | +5.10 | | | | | | | | | | | | |
| | | -4.90 | -2.90 | -1.40 | -0.70 | -1.40 | -1.10 | -2.20 | -2.90 | -1.50 | -1.00 | -2.00 | -3.00 | -2.80 | -2.00 | -1.80 | -1.50 | | |
| | | +0.30 | +0.50 | +1.00 | +1.20 | +1.00 | +0.50 | -0.50 | -0.90 | -0.90 | -0.60 | -0.30 | +0.60 | | | | | | |
| Influence of Moment Above floor | | -0.40 | -0.20 | -0.20 | -0.10 | -0.10 | 0 | 0 | -2.40 | -0.90 | -0.30 | -0.10 | -0.10 | | | | | | |
| | | +19.20 | +16.30 | -35.50 | -32.50 | +22.30 | +10.20 | +3.40 | -3.40 | | | | | | | | | | |
| | | -2.20 | | | | | | | | | | | | | | | | | |
| | | +1.16 | +70 | +34 | +17 | | | | | | | | | | | | | | |
| Final Moments | | +0.90 | +0.50 | +0.20 | +0.10 | -1.20 | 0 | +0.10 | +0.10 | 0 | 0 | +0.10 | +0.10 | | | | | | |
| | | -114.90 | +86.20 | +287.0 | +11.10 | -7.40 | -3.70 | -1.20 | +1.20 | -1.20 | -1.20 | -1.20 | -1.20 | | | | | | |
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Checking Results:

$$R_1 + R_2 = \frac{9.50 + 15.73}{1.70} = 25.23 \approx 14.95$$

$$\sum F_x = 30 - 14.95 \times 2 = 0.10T$$

∴ O.K.



ANALYSIS OF THE EFFECT OF WIND ON A HIGH REINFORCED CONCRETE BUILDING

Comparison of Approximate and Exact Methods

| | | |
|----------|-----------------|---------------------|
| COMPUTER | RIAD SHAHIN | WIND ANALYSIS |
| CHK'D BY | RIAD SHAHIN | HARDY CROSS METHOD |
| APP'D BY | DR. JACK NASSER | DATE: DECEMBER 1964 |
| | | SHEET NO 65/ |

14-13-12 Floors

1. Shears

$$V_{12} = \frac{-2}{1.70} (-2.40 - 1.20) = \frac{-2}{1.70} (-3.60) = +4.42 = +4.42 \Delta_{14}/10^4$$

$$V_{13} = \frac{-2}{3.40} (+4.30 + 9.60 + 3.20 + 7.20) = \frac{-2}{3.40} (+24.30) = 14.20 = 14.20 \Delta_{14}/10^4$$

$$V_{14} = \frac{-2}{3.40} (-29.10 - 26.60 - 34.60 - 34.00) = \frac{-2}{3.40} (124.30) = +73 = +73 \Delta_{14}/10^4$$

$$V_{12} = \frac{-2}{1.70} (+19.20 + 14.70) = \frac{-2}{1.70} (+33.90) = -40 = -40 \Delta_{13}/10^4$$

$$V_{13} = \frac{-2}{3.40} (-35.50 - 32.50 - 38.20 - 36.50) = \frac{-2}{3.40} (-142.70) = +84 = +84 \Delta_{13}/10^4$$

$$V_{14} = \frac{-2}{3.40} (+10.20 + 9.40 + 7.40 + 3.30) = \frac{-2}{3.40} (+84.30) = -14.10 = -14.10 \Delta_{13}/10^4$$

$$V_{12} = \frac{-2}{1.70} (-114.90 - 144.30) = \frac{-2}{1.70} (-259.20) = +305 = +305 \Delta_{12}/10^4$$

$$V_{13} = \frac{-2}{3.40} (-28.70 + 11.10 + 21.80 + 9.18) = \frac{-2}{3.40} (+71.20) = -41.80 = -41.80 \Delta_{12}/10^4$$

$$V_{14} = \frac{-2}{3.40} (-3.70 - 1.20 - 1.80 - 0.90) = \frac{-2}{3.40} (-7.60) = +4.45 = +4.45 \Delta_{12}/10^4$$

2. Effect of 15th floor.

$$V_{12} = \frac{-2}{1.70} (+0.05 + 0.02) = \frac{-2}{1.70} (+0.07) = -0.08$$

$$V_{13} = \frac{-2}{3.40} (-0.08 - 0.22 - 0.08 - 0.16) = \frac{-2}{3.40} (-0.54) = +0.32$$

$$V_{14} = \frac{-2}{3.40} (+0.66 + 1.65 + 0.75 + 1.74) = \frac{-2}{3.40} (+4.80) = -2.82$$

3. Δ 's

$$+4.42 \Delta_{14} - 40 \Delta_{13} + 305 \Delta_{12} = (30.00 - 0.08) 10^4 = 29.92 \times 10^4$$

$$-14.20 \Delta_{14} + 84 \Delta_{13} - 41.80 \Delta_{12} = (26.70 + 0.32) 10^4 = 27.02 \times 10^4$$

$$+73 \Delta_{14} - 14.10 \Delta_{13} + 4.45 \Delta_{12} = (23.30 - 2.82) 10^4 = 20.48 \times 10^4$$

$$\Delta_{12} = 0.152$$

$$\Delta_{13} = 0.457$$

$$\Delta_{14} = 0.359$$

13 - 12 - 11 Floors

1. Shears

$$V_{11} = \frac{-2}{1.70} (-300 - 1.80) + \frac{-2}{1.70} (-4.80) = +5.65 = 5.65 \Delta_{13}/10^4$$

$$V_{12} = \frac{-2}{3.40} (+5.40 + 13.80 + 4.70 + 11.00) = \frac{-2}{3.40} (+34.90) = -20.50 = -20.50 \Delta_{13}/10^4$$

$$V_{13} = \frac{-2}{3.40} (-32.30 - 27.80 - 37.40 - 35.40) = \frac{-2}{3.40} (-132.90) = +78 = +78 \Delta_{13}/10^4$$

$$V_{14} = \frac{-2}{1.70} (+35.80 - 29.80) = \frac{-2}{1.70} (+6.00) = -7.06 = -7.06 \Delta_{12}/10^4$$

$$V_{15} = \frac{-2}{3.40} (-67.30 - 60.30 - 76.20 - 73.50) = \frac{-2}{3.40} (-277.30) = +163 = +163 \Delta_{12}/10^4$$

$$V_{16} = \frac{-2}{3.40} (+14.20 + 4.80 + 10.00 + 4.50) = \frac{-2}{3.40} (+33.50) = -19.70 = -19.70 \Delta_{12}/10^4$$

$$V_{17} = \frac{-2}{1.70} (-129.40 - 151.70) = \frac{-2}{1.70} (-281.10) = +330 = +330 \Delta_{11}/10^4$$

$$V_{18} = \frac{-2}{3.40} (+53.70 + 18.00 + 44 + 17.80) = \frac{-2}{3.40} (+133.50) = -78.20 = -78.20 \Delta_{11}/10^4$$

2. Effect of 14th floor

$$V_{11} = \frac{-2}{1.70} (+0.09 + 0.04) = \frac{-2}{1.70} (+0.13) = -0.15$$

$$V_{12} = \frac{-2}{3.40} (-0.16 - 0.37 - 0.11 - 0.28) = \frac{-2}{3.40} (-0.92) = +0.54$$

$$V_{13} = \frac{-2}{3.40} (+0.87 + 1.99 + 0.95 + 2.08) = \frac{-2}{3.40} (+5.89) = -3.46$$

3. Δ 's

$$+5.65 \Delta_{13} - 78.20 \Delta_{12} + 330 \Delta_{11} = (33.20 - 0.15) 10^4 = 33.05 \times 10^4$$

$$-20.50 \Delta_{13} + 163 \Delta_{12} - 78.20 \Delta_{11} = (30.00 + 0.54) 10^4 = 30.54 \times 10^4$$

$$+78 \Delta_{13} - 19.70 \Delta_{12} + 5.64 \Delta_{11} = (26.70 - 3.46) 10^4 = 23.24 \times 10^4$$

$$\Delta_{11} = 0.166$$

$$\Delta_{12} = 0.312$$

$$\Delta_{13} = 0.363$$

12 - 11 - 10 Floors

1. Shears

$$V_{10} = \frac{-2}{1.70} (-5.60 - 3.60) = \frac{-2}{1.70} (-9.20) = +10.80 = +10.80 \Delta_{12} / 10^4$$

$$V_{11} = \frac{-2}{3.40} (+10 + 25.60 + 9.50 + 20.50) = \frac{-2}{3.40} (+65.60) = -38.50 = 38.50 \Delta_{12} / 10^4$$

$$V_{12} = \frac{-2}{3.40} (-61.40 - 52.20 - 71.30 - 70.20) = \frac{-2}{3.40} (-255.10) = +150 = +150 \Delta_{12} / 10^4$$

$$V_{10} = \frac{-2}{1.70} (+37.20 + 30.40) = \frac{-2}{1.70} (+67.60) = -79.50 = -79.50 \Delta_{11} / 10^4$$

$$V_{11} = \frac{-2}{3.40} (-69.90 - 66.60 - 77.80 - 76.70) = \frac{-2}{3.40} (-291.30) = +171 = +171 \Delta_{11} / 10^4$$

$$V_{12} = \frac{-2}{3.40} (+27.30 + 0 + 22.20 + 8.90) = \frac{-2}{3.40} (+58.40) = -34.30 = -34.30 \Delta_{11} / 10^4$$

$$V_{10} = \frac{-2}{1.70} (-129.80 - 151.90) = \frac{-2}{1.70} (-281.70) = +331 = +331 \Delta_{10} / 10^4$$

$$V_{11} = \frac{-2}{3.40} (+54.40 + 19.80 + 44.60 + 18.40) = \frac{-2}{3.40} (+137.20) = -80.20 = -80.20 \Delta_{10} / 10^4$$

$$V_{12} = \frac{-2}{3.40} (-8.60 - 2.50 - 5.2.10) = \frac{-2}{3.40} (-18.20) = +10.70 = +10.70 \Delta_{10} / 10^4$$

2. Effect of 13th floor.

$$V_{10} = \frac{-2}{1.70} (+0.11 + 0.05) = \frac{-2}{1.70} (+0.16) = -0.19$$

$$V_{11} = \frac{-2}{3.40} (-0.20 - 0.53 - 0.15) = \frac{-2}{3.40} (-1.23) = +0.72$$

$$V_{12} = \frac{-2}{3.40} (+1.25 + 3.36 + 1.31 + 3.18) = \frac{-2}{3.40} (+9.10) = -5.32$$

3. Δ 's

$$+10.80 \Delta_{12} - 79.50 \Delta_{11} + 331 \Delta_{10} = (.36.40 - 0.19) 10^4 = 36.21 \times 10^4$$

$$-38.50 \Delta_{12} + 171 \Delta_{11} - 80.20 \Delta_{10} = (.23.20 + 0.72) 10^4 = 33.92 \times 10^4$$

$$+151 \Delta_{12} - 34.30 \Delta_{11} + 10.70 \Delta_{10} = (.30.00 - 5.30) 10^4 = 24.68 \times 10^4$$

$$\Delta_{10} = 0.182$$

$$\Delta_{11} = 0.334$$

$$\Delta_{12} = 0.228$$

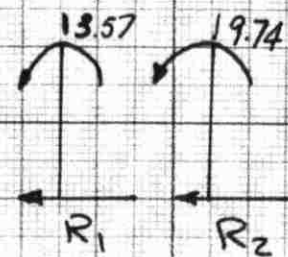
| JOINT | 9 | | | 10 | | | 11 | | 11a | | 10a | | | | 9a | | | | |
|-----------------------|--------|-------|-------|-------|-------|-------|--------|--------|--------|--------|-------|--------|--------|-------|-------|-------|-------|-------|-------|
| MEMBER | I | R | S | I | R | S | I | R | L | R | I | S | L | R | I | S | L | R | I |
| DIST. FACTOR | 0.44 | 0.27 | 0.29 | 0.34 | 0.32 | 0.34 | 0.53 | 0.47 | 0.32 | 0.32 | 0.36 | 0.27 | 0.24 | 0.23 | 0.26 | 0.24 | 0.21 | 0.20 | 0.35 |
| Moment of Above Floor | | | | | | | -6.46 | | -9.83 | | | | | | | | | | |
| | | | | | | | | +1.58 | +3.15 | +3.15 | +3.53 | +1.77 | | | | | | | |
| | | | | | -0.21 | +1.29 | +2.58 | +2.30 | +1.15 | | -0.24 | -0.48 | -0.42 | -0.41 | -0.46 | -0.23 | | | |
| | | | -0.19 | -0.37 | -0.34 | -0.37 | -0.19 | -0.15 | -0.29 | -0.29 | -0.33 | -0.17 | -0.17 | | | | | | |
| | +0.08 | +0.05 | +0.06 | +0.03 | +0.04 | +0.09 | +0.18 | +0.16 | +0.08 | | +0.05 | +0.09 | +0.08 | +0.08 | +0.09 | +0.05 | +0.03 | | |
| | | +0.02 | -0.03 | -0.06 | -0.05 | -0.05 | -0.03 | -0.02 | -0.04 | -0.04 | -0.05 | -0.03 | | -0.03 | | +0.02 | +0.04 | +0.03 | +0.03 |
| +0.01 | 0 | 0 | | | | +0.03 | +0.02 | +4.05 | +2.82 | +2.96 | -0.01 | +0.01 | +0.01 | +0.01 | | | | | |
| +0.09 | +0.07 | -0.16 | -0.40 | -0.56 | +0.96 | | | -12.57 | +3.89 | | | +1.19 | -0.53 | -0.32 | -0.34 | -0.14 | +0.06 | +0.03 | +0.05 |
| Final Moments | -1.47 | | | | | | -16.10 | -13.70 | +13.70 | +11.80 | +6.55 | -18.35 | -18.70 | | | | | | |
| | +13.60 | | | | | | +10.50 | +2.95 | -2.95 | -2.25 | -1.03 | +3.28 | +8.20 | | | | | | |
| | -25.76 | | | | | | -1.70 | -0.50 | +0.50 | +0.34 | +0.08 | -0.42 | -1.00 | | | | | | |
| | -13.57 | | | | | | -7.80 | -11.25 | +11.25 | +9.89 | +5.60 | -15.49 | -11.50 | | | | | | |

Checking Results:

$$R_1 + R_2 = \frac{13.57 + 19.74}{1.70} = 19.75T$$

$$\sum F_x = 39.55 - 2 \times 19.75 = 0.05$$

∴ O.K.



ANALYSIS OF THE EFFECT OF WIND ON A HIGH REINFORCED CONCRETE BUILDING

Comparison of Approximate and Exact Methods

COMPUTER: RIAD SHAHIN

CHK'D BY: RIAD SHAHIN

APP'D BY: D^S JACK NASSER

WIND ANALYSIS

HARDY CROSS METHOD

DATE: DECEMBER 1964

SHEET N^o: 71 / 1

11 - 10 - 9 Floors

1. Shears (same as previous case)

2. Effect of 13th floor

$$V_9 = \frac{-2}{1.70} (+0.09 + 0.05) = \frac{-2}{1.70} (+0.14) = 0.17$$

$$V_{10} = \frac{-2}{3.40} (-0.16 - 0.40 - 0.14 - 0.34) = \frac{-2}{3.40} (-1.04) = +0.60$$

$$V_{11} = \frac{-2}{3.40} (+0.96 + 2.57 + 1.19 + 0.96) = \frac{-2}{3.40} (+7.68) = -4.42$$

3. Δ 's

$$+ 10.80 \Delta_{11} - 79.50 \Delta_{10} + 331 \Delta_9 = (3955 - 0.17) 10^4 = 39.38 \times 10^4$$

$$- 38.50 \Delta_{11} + 171 \Delta_{10} - 80.80 \Delta_9 = (36.40 + 0.60) 10^4 = 37.00 \times 10^4$$

$$+ 150 \Delta_{11} - 34.30 \Delta_{10} + 10.70 \Delta_9 = (33.20 - 4.42) 10^4 = 28.78 \times 10^4$$

$$\Delta_9 = 0.198$$

$$\Delta_{10} = 0.369$$

$$\Delta_{11} = 0.262$$

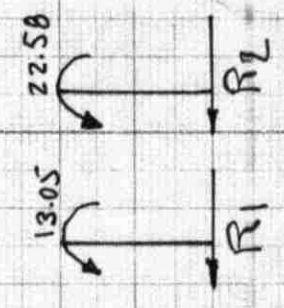
| JOINT | 8 | | | 9 | | | 10 | | | 10a | | | 9a | | | 8a | | | | |
|------------------------------------|------|------|------|------|-------|------|------|------|--------|-------|------|-------|--------|-------|-------|-------|--------|------|------|------|
| | I | R | S | I | R | S | I | R | S | L | R | I | S | L | R | I | S | L | R | I |
| DIST FACTOR | 0.56 | 0.25 | 0.19 | 0.34 | 0.32 | 0.34 | 0.53 | 0.47 | 0.32 | 0.32 | 0.32 | 0.36 | 0.27 | 0.24 | 0.23 | 0.26 | 0.16 | 0.20 | 0.19 | 0.45 |
| Influence of Δ_{10} | | | | | | | -110 | +52 | +26 | | | -110 | +30 | +26 | +25 | +29 | +15.50 | | | |
| | | | | +13 | | | +29 | | | | | +15 | | | | | | | | |
| | | | | +22 | | | +29 | +11 | +22 | +22 | +22 | +25 | +14.50 | +11 | | | | | | |
| | | | | | -3.10 | | -6 | -12 | -10.50 | -5.30 | | -3.40 | -6.80 | -6.20 | -5.90 | -6.60 | -3.30 | | | |
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| Influence of Δ_9 | | | | | | | | | | | | | | | | | | | | |
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| Influence of Δ_8 | | | | | | | | | | | | | | | | | | | | |
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| Influence of Moment of Above Floor | | | | | | | | | | | | | | | | | | | | |
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| Final Moments | | | | | | | | | | | | | | | | | | | | |
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Checking Results:

$$R_1 + R_2 = \frac{13.05 + 22.58 - 35.63}{1.70} = 21.20 T$$

$$\sum F_x = 42.45 - 21.20 \times 2 = 0.05 T$$

OK



ANALYSIS OF THE EFFECT OF WIND ON A HIGH REINFORCED CONCRETE BUILDING

Comparison of Approximate and Exact Methods

| | | |
|------------|----------------|----------------------|
| COMPUTER : | RIAD SHAHIN | WIND ANALYSIS |
| CHK'D BY : | RIAD SHAHIN | HARDY CROSS METHOD |
| APP'D BY : | DR JACK NASSER | DATE : DECEMBER 1964 |
| | | SHEET N° 73 / |

10 - 9 - 8 Floors

1. Shears

$$V_8 = \frac{-2}{1.70} (-6.90 - 4.00) = \frac{-2}{1.70} (-11.70) = +13.70 = +13.70 \Delta_{10} / 10^4$$

$$V_9 = \frac{-2}{3.40} (+10.90 + 25.40 + 10.80 + 20.90) = \frac{-2}{3.40} (+66.40) = -39 = -39 \Delta_{10} / 10^4$$

$$V_{10} = \frac{-2}{3.40} (-60.40 - 50.90 - 81.30 - 70.40) = \frac{-2}{3.40} (-263.00) = 154.00 = +154.00 \Delta_{10} / 10^4$$

$$V_8 = \frac{2}{1.70} (+47.70 + 39) = \frac{2}{1.70} (+86.70) = -102 = -102 \Delta_9 / 10^4$$

$$V_9 = \frac{-2}{3.40} (-76.60 - 69.40 - 83.90 - 79.30) = \frac{-2}{3.40} (-309.20) = +181 = +181 \Delta_9 / 10^4$$

$$V_{10} = \frac{-2}{3.40} (+28.40 + 8.40 + 22.40 + 9) = \frac{-2}{3.40} (+68.20) = -40 = -40 \Delta_9 / 10^4$$

$$V_8 = \frac{-2}{1.70} (-205.90 - 257) = \frac{-2}{1.70} (-462.90) = +544 = +544 \Delta_8 / 10^4$$

$$V_9 = \frac{-2}{3.40} (+68.90 + 25.30 + 58.40 + 24.20) = \frac{-2}{3.40} (+176.80) = -104 = -104 \Delta_8 / 10^4$$

$$V_{10} = \frac{-2}{3.40} (-10.60 - 3.10 - 6.40 - 2.70) = \frac{-2}{3.40} (-22.80) = +13.40 = 13.40 \Delta_8 / 10^4$$

2. Effect of 11th floor.

$$V_8 = \frac{-2}{1.70} (+0.14 + 0.08) = \frac{-2}{1.70} (+0.22) = -0.26$$

$$V_9 = \frac{-2}{3.40} (-0.22 - 0.49 - 0.18 - 0.40) = \frac{-2}{3.40} (-1.29) = +0.75$$

$$V_{10} = \frac{-2}{3.40} (+1.18 + 3.14 + 1.39 + 3.42) = \frac{-2}{3.40} (+9.13) = -5.35$$

3. Δ 's

$$+13.70 \Delta_{10} - 102 \Delta_9 + 544 \Delta_8 = (48.45 - 0.26) 10^4 = 48.19 \times 10^4$$

$$-39 \Delta_{10} + 181 \Delta_9 - 104 \Delta_8 = (39.55 + 0.75) 10^4 = 40.30 \times 10^4$$

$$+154 \Delta_{10} - 40 \Delta_9 + 13.40 \Delta_8 = (38.40 - 5.35) 10^4 = 31.05 \times 10^4$$

$$\Delta_8 = 0.137$$

$$\Delta_9 = 0.361$$

$$\Delta_{10} = 0.283$$

9 - 8 - 7 Floors

1. Shears

$$V_7 = \frac{-2}{1.70} (-7.90 - 5.70) = \frac{-2}{1.70} (-13.60) = +16 = +16 \Delta_9 / 10^4$$

$$V_8 = \frac{-2}{3.40} (+12.70 + 33.20 + 12.30 + 30.10) = \frac{-2}{3.40} (+88.30) = -52 = -52 \Delta_9 / 10^4$$

$$V_9 = \frac{-2}{3.40} (-66.40 - 52.70 - 81.20 - 66.20) = \frac{-2}{3.40} (-266.50) = +157 = +157 \Delta_9 / 10^4$$

$$V_7 = \frac{-2}{1.70} (+75.10 + 67.10) = \frac{-2}{1.70} (+142.20) = -167 = -167 \Delta_8 / 10^4$$

$$V_8 = \frac{-2}{3.40} (-108.20 - 122.90 - 139.80 - 131.20) = \frac{-2}{3.40} (-503.10) = +296 = +296 \Delta_8 / 10^4$$

$$V_9 = \frac{-2}{3.40} (+37.10 + 10.90 + 28.70 + 11.40) = \frac{-2}{3.40} (+88.10) = -51.80 = -51.80 \Delta_8 / 10^4$$

$$V_7 = \frac{-2}{1.70} (-235.30 - 271.00) = \frac{-2}{1.70} (-506.30) = +592 = +592 \Delta_7 / 10^4$$

$$V_8 = \frac{-2}{3.40} (+116.20 + 36.30 + 94.30 + 35.70) = \frac{-2}{3.40} (+282.50) = 166 = -166 \Delta_7 / 10^4$$

$$V_9 = \frac{-2}{3.40} (-13.00 - 3.70 - 7.20 - 3.10) = \frac{-2}{3.40} (-27.00) = +15.90 = +15.90 \Delta_7 / 10^4$$

2. Effect of 10th floor.

$$V_7 = \frac{-2}{1.70} (+0.13 + 0.18) = \frac{-2}{1.70} (+0.31) = -0.36$$

$$V_8 = \frac{-2}{3.40} (-0.22 - 0.60 - 0.34 - 0.81) = \frac{-2}{3.40} (-1.97) = +1.26$$

$$V_9 = \frac{-2}{3.40} (+1.31 + 3.13 + 2.19 + 5.03) = \frac{-2}{3.40} (+11.66) = -6.85$$

3 Δ 's

$$+16 \Delta_9 - 167 \Delta_8 + 592 \Delta_7 = (45.35 - 0.36) 10^4 = 44.99 \times 10^4$$

$$-52 \Delta_9 + 296 \Delta_8 - 166 \Delta_7 = (48.45 + 1.26) 10^4 = 49.71 \times 10^4$$

$$+157 \Delta_9 - 51.80 \Delta_8 + 15.90 \Delta_7 = (39.55 - 6.85) 10^4 = 32.70 \times 10^4$$

$$\Delta_7 = 0.145$$

$$\Delta_8 = 0.278$$

$$\Delta_9 = 0.284$$

8 - 7 - 6 Floors

1. Shears

$$V_6 = \frac{-2}{1.70} (-12.70 - 8.70) = \frac{-2}{1.70} (-21.40) = +25.20 = +25.20 \Delta_8 / 10^4$$

$$V_7 = \frac{-2}{3.40} (+20.48 + 53.70 + 19 + 44.6.30) = \frac{-2}{3.40} (+139.40) = -82 = -82 \Delta_8 / 10^4$$

$$V_8 = \frac{-2}{3.40} (-106.60 - 86.60 - 130.60 - 120.60) = \frac{-2}{3.40} (-444.40) = +260 = +260 \Delta_8 / 10^4$$

$$V_6 = \frac{-2}{1.70} (+77.80 + 68.60) = \frac{-2}{1.70} (+146.40) = -172 = -172 \Delta_7 / 10^4$$

$$V_6 = \frac{-2}{3.40} (-126.70 - 119.30 - 143.10 - 139.30) = \frac{-2}{3.40} (-528.40) = +310 = +310 \Delta_7 / 10^4$$

$$V_8 = \frac{2}{3.40} (+58.30 + 15 + 47.90 + 17.20) = \frac{2}{3.40} (+138.40) = -80 = -80 \Delta_7 / 10^4$$

$$V_6 = \frac{-2}{1.70} (-236.80 - 271.30) = \frac{-2}{1.70} (-508.10) = +595 = +595 \Delta_6 / 10^4$$

$$V_7 = \frac{-2}{3.40} (+118.30 + 40.80 + 95.00 + 37.50) = \frac{-2}{3.40} (+291.60) = 171 = -171 \Delta_6 / 10^4$$

$$V_8 = \frac{-2}{3.40} (-20.80 - 5.10 - 12.20 - 4.70) = \frac{-2}{3.40} (-42.80) = +25.20 = +25.20 \Delta_6 / 10^4$$

2. Effect of 9th floor.

$$V_6 = \frac{-2}{1.70} (+0.18 + 0.17) = \frac{-2}{1.70} (+0.35) = -0.41$$

$$V_6 = \frac{-2}{3.40} (-0.32 - 0.83 - 0.36 - 0.87) = \frac{-2}{3.40} (-2.38) = +1.40$$

$$V_7 = \frac{-2}{3.40} (+1.72 + 4.84 + 2.37 + 6.11) = \frac{-2}{3.40} (+15.04) = -8.70$$

3 Δ's

$$+25.20 \Delta_8 - 172 \Delta_7 + 595 \Delta_6 = (48.10 - 0.41) 10^4 = 47.69 \times 10^4$$

$$-82 \Delta_8 + 310 \Delta_7 - 171 \Delta_6 = (45.35 + 1.40) 10^4 = 46.75 \times 10^4$$

$$+260 \Delta_8 - 80 \Delta_7 + 25.20 \Delta_6 = (42.45 - 8.70) 10^4 = 33.75 \times 10^4$$

$$\Delta_6 = 0.154$$

$$\Delta_7 = 0.288$$

$$\Delta_8 = 0.202$$

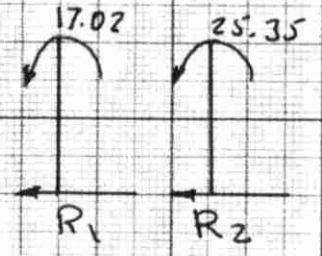
| JOINT | 5 | | | 6 | | | 7 | | 7a | | 6a | | | | 5a | | | | | |
|-----------------------|--------|------|------|------|------|------|------|------|-------|--------|-------|-------|-------|------|------|------|------|------|------|--|
| MEMBER | I | R | S | I | R | S | I | R | L | R | I | S | L | R | I | S | L | R | I | |
| DIST. FACTOR | 0.47 | 0.21 | 0.32 | 0.38 | 0.24 | 0.38 | 0.61 | 0.39 | 0.29 | 0.27 | 0.44 | 0.30 | 0.20 | 0.20 | 0.30 | 0.26 | 0.17 | 0.17 | 0.40 | |
| Moment of Above Floor | | | | | | | | | -7.90 | -14.47 | | | | | | | | | | |
| | | | | | | | | | +2.10 | +4.20 | +3.90 | +6.37 | +3.19 | | | | | | | |
| | | | | | | | | | +1.77 | +3.54 | +2.26 | +1.13 | | | | | | | | |
| | | | | | | | | | | | | | | | | | | | | |
| | | | | | | | | | | | | | | | | | | | | |
| | | | | | | | | | | | | | | | | | | | | |
| Final Moments | -2.82 | | | | | | | | | | | | | | | | | | | |
| | +23.80 | | | | | | | | | | | | | | | | | | | |
| | 40.00 | | | | | | | | | | | | | | | | | | | |
| | -17.02 | | | | | | | | | | | | | | | | | | | |
| | | | | | | | | | | | | | | | | | | | | |
| | | | | | | | | | | | | | | | | | | | | |

Checking Results

$$R_1 + R_2 = \frac{17.02}{1.70} + \frac{25.95}{1.70} = \frac{42.97}{1.70} = 25.30T$$

$$\sum F_x = 50.70 - 25.30 \times 2 = 0.10T$$

∴ OK



ANALYSIS OF THE EFFECT OF WIND ON A HIGH REINFORCED CONCRETE BUILDING

Comparison of Approximate and Exact Methods

COMPUTER : RIAD SHAHIN
 CHK'D BY : RIAD SHAHIN
 APP'D BY : DR. JACK NASSER

WIND ANALYSIS
 HARDY CROSS METHOD

DATE : DECEMBER 1964 SHEET No 79 /

7 - 6 - 5 Floors

1. Shears (same as previous case)

2. Effect of 8th floor.

$$V_5 = \frac{-2}{1.70} (+0.13 + 0.16) = \frac{-2}{1.70} (+0.29) = -0.34$$

$$V_6 = \frac{-2}{3.40} (-0.23 - 0.58 - 0.33 - 0.80) = \frac{-2}{3.40} (-1.94) = +1.14$$

$$V_7 = \frac{-2}{3.40} (+1.27 + 3.47 + 2.16 + 5.59) = \frac{-2}{3.40} (12.49) = -7.35$$

3. Δ 's

$$+25.20\Delta_7 - 172\Delta_6 + 595\Delta_5 = (50.70 - 0.34)10^4 = 50.36 \times 10^4$$

$$-82\Delta_7 + 310\Delta_6 - 171\Delta_5 = (88.10 + 1.14)10^4 = 89.24 \times 10^4$$

$$+260\Delta_7 - 80\Delta_6 + 25.20\Delta_5 = (45.35 - 7.35)10^4 = 38.00 \times 10^4$$

$$\Delta_5 = 0.165$$

$$\Delta_6 = 0.308$$

$$\Delta_7 = 0.224$$

6 - 5 - 4 Floors

1. Shears

$$V_4 = \frac{-2}{1.70} (-15.60 - 10.30) = \frac{-2}{1.70} (-25.90) = +30.50 = +30.50 \Delta_6 / 10^4$$

$$V_5 = \frac{-2}{3.40} (+22.70 + 54.70 + 20.30 + 46.80) = \frac{-2}{3.40} (+144.50) = -85 = -85 \Delta_6 / 10^4$$

$$V_6 = \frac{-2}{3.40} (-107.20 - 86.80 - 130.80 - 120.80) = \frac{-2}{3.40} (-445.60) = +262 = 262 \Delta_6 / 10^4$$

$$V_4 = \frac{-2}{1.70} (+95.00 + 82.20) = \frac{-2}{1.70} (+177.20) = -208 = -208 \Delta_5 / 10^4$$

$$V_5 = \frac{-2}{3.40} (-142.10 - 124.70 - 154.50 - 144.00) = \frac{-2}{3.40} (-565.30) = +332 = 332 \Delta_5 / 10^4$$

$$V_6 = \frac{-2}{3.40} (+61 + 15.80 + 49 + 17.70) = \frac{-2}{3.40} (+143.50) = -84.20 = -84.20 \Delta_5 / 10^4$$

$$V_4 = \frac{-2}{1.70} (-336.90 - 411.80) = \frac{-2}{1.70} (-748.70) = +880 = +880 \Delta_4 / 10^4$$

$$V_5 = \frac{-2}{3.40} (+139.80 + 48.50 + 181.70 + 47.90) = \frac{-2}{3.40} (+357.90) = -210 = -210 \Delta_4 / 10^4$$

$$V_6 = \frac{-2}{3.40} (-24.60 - 6.20 - 15.90 - 6.00) = \frac{-2}{3.40} (-52.70) = +31 = 31 \Delta_4 / 10^4$$

2. Effect of 7th floor

$$V_4 = \frac{-2}{1.70} (+0.17 + 0.24) = \frac{-2}{1.70} (+0.41) = -0.48$$

$$V_5 = \frac{-2}{3.40} (-0.29 - 0.69 - 0.41 - 0.92) = \frac{-2}{3.40} (-2.31) = +1.38$$

$$V_6 = \frac{-2}{3.40} (+1.49 + 4.08 + 2.45 + 6.35) = \frac{-2}{3.40} (+14.37) = -8.45$$

3. Δ 'S

$$+30.50 \Delta_6 - 208 \Delta_5 + 880 \Delta_4 = (53.30 - 0.48) 10^4 = 52.82 \times 10^4$$

$$-85 \Delta_5 + 332 \Delta_5 - 210 \Delta_4 = (50.70 + 1.38) 10^4 = 49.32 \times 10^4$$

$$+262 \Delta_6 - 84.20 \Delta_5 + 31 \Delta_4 = (48.10 - 8.45) 10^4 = 39.65 \times 10^4$$

$$\Delta_4 = 0.118$$

$$\Delta_5 = 0.281$$

$$\Delta_6 = 0.227$$

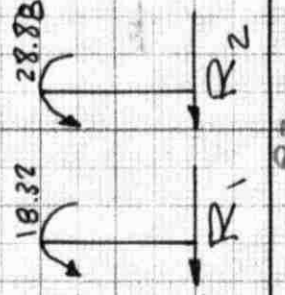
| JOINT | 3 | | | 4 | | | 5 | | | 5a | | | 4a | | | 3a | | | | | | |
|------------------------------|------------------------------------|------|---------|---------|---------|---------|---------|---------|--------|--------|--------|--------|--------|-------|-------|--------|--------|-------|-------|--------|--|--|
| | I | R | S | I | R | S | I | R | S | L | R | I | S | L | R | I | S | L | R | I | | |
| DIST FACTOR | 0.50 | 0.17 | 0.33 | 0.48 | 0.24 | 0.24 | 0.24 | 0.38 | 0.29 | 0.27 | 0.44 | 0.22 | 0.20 | 0.20 | 0.19 | 0.39 | 0.28 | 0.15 | 0.15 | 0.42 | | |
| Influence of Δ ₁₅ | | | +30.50 | +61 | +30.50 | +34 | +18 | +21.50 | +43 | +40 | +65.50 | +32.80 | +15.30 | +43 | +41 | +83 | +41.50 | | | | | |
| | | | -15.30 | -5.20 | -10.00 | -5 | -4.80 | -12 | -15.50 | -7.80 | -5.30 | -10.60 | -9.60 | -9.60 | -9.20 | -18.70 | -9.40 | -2.60 | | | | |
| | | | -2.20 | +5.30 | +10.50 | +10.50 | +6.10 | +3.10 | +1.90 | +3.80 | +5.70 | +2.90 | +2.90 | +2.60 | +2.60 | -4.10 | -8.20 | -4.40 | -4.40 | -12.60 | | |
| | | | -1.60 | -0.50 | -1.00 | -0.50 | -0.20 | -1.50 | -2.00 | -1.50 | | | | | | | | | | | | |
| | | | -0.30 | -0.10 | -0.10 | +1.00 | +0.50 | +0.60 | +0.30 | +0.40 | +0.70 | -0.30 | -0.40 | +0.30 | +0.30 | -0.20 | -0.40 | -0.20 | -0.30 | | | |
| | | | -17.20 | -8.00 | +25.20 | +6.7 | +52.70 | -119.70 | -89.90 | +89.90 | | | | | | | | | | | | |
| | | | +28 | +89 | +178 | +89 | +103 | +51.50 | | | | | | | | | | | | | | |
| | | | +126 | +43 | +84 | +42 | +21.50 | | | | | | | | | | | | | | | |
| | | | -5.60 | -16.70 | -33.30 | -16.70 | -19.10 | -9.80 | | | | | | | | | | | | | | |
| | | | +11.20 | +3.80 | +7.30 | +3.70 | | | | | | | | | | | | | | | | |
| Influence of Δ ₄ | | | -3.70 | -3.70 | | | | | | | | | | | | | | | | | | |
| | | | +89 | +178 | +89 | +103 | +51.50 | | | | | | | | | | | | | | | |
| | | | +43 | +84 | +42 | +21.50 | | | | | | | | | | | | | | | | |
| | | | -5.60 | -16.70 | -33.30 | -16.70 | -19.10 | -9.80 | | | | | | | | | | | | | | |
| | | | +11.20 | +3.80 | +7.30 | +3.70 | | | | | | | | | | | | | | | | |
| | | | -0.50 | +1.60 | +3.20 | +1.60 | +1.80 | +0.90 | | | | | | | | | | | | | | |
| | | | -0.20 | -0.30 | -0.20 | | | | | | | | | | | | | | | | | |
| | | | +0.20 | 0 | 0 | -171.90 | +107.70 | +73.90 | +0.20 | +0.20 | | | | | | | | | | | | |
| | | | +136.80 | +68.50 | +205.30 | | | | | | | | | | | | | | | | | |
| | | | -740 | +55.50 | +116 | +224 | +113 | | | | | | | | | | | | | | | |
| Influence of Δ ₅ | | | -24.60 | -49.20 | -24.60 | -28.90 | -14.50 | | | | | | | | | | | | | | | |
| | | | +4.20 | +8.10 | +4.10 | | | | | | | | | | | | | | | | | |
| | | | -3.00 | -2.40 | -4.90 | -2.50 | -2.90 | -1.40 | | | | | | | | | | | | | | |
| | | | +2.70 | +0.90 | +1.80 | +0.90 | | | | | | | | | | | | | | | | |
| | | | -0.30 | -0.20 | -0.50 | -0.20 | -0.30 | -0.10 | | | | | | | | | | | | | | |
| | | | +0.20 | +0.10 | +0.20 | +63.40 | -35.80 | -27.60 | +0.10 | 0 | | | | | | | | | | | | |
| | | | -382.30 | +123.40 | -208.90 | | | | | | | | | | | | | | | | | |
| | | | +55.50 | +116 | +224 | +113 | | | | | | | | | | | | | | | | |
| | | | +12.30 | +4.20 | +8.10 | +4.10 | | | | | | | | | | | | | | | | |
| | Influence of Moment of Above Floor | | | -2.40 | -4.90 | -2.50 | -2.90 | -1.40 | | | | | | | | | | | | | | |
| | | | +2.70 | +0.90 | +1.80 | +0.90 | | | | | | | | | | | | | | | | |
| | | | -0.30 | -0.20 | -0.50 | -0.20 | -0.30 | -0.10 | | | | | | | | | | | | | | |
| | | | +0.20 | +0.10 | +0.20 | +63.40 | -35.80 | -27.60 | +0.10 | 0 | | | | | | | | | | | | |
| | | | -382.30 | +123.40 | -208.90 | | | | | | | | | | | | | | | | | |
| | | | +55.50 | +116 | +224 | +113 | | | | | | | | | | | | | | | | |
| | | | +12.30 | +4.20 | +8.10 | +4.10 | | | | | | | | | | | | | | | | |
| | | | -2.40 | -4.90 | -2.50 | -2.90 | -1.40 | | | | | | | | | | | | | | | |
| | | | +2.70 | +0.90 | +1.80 | +0.90 | | | | | | | | | | | | | | | | |
| Final Moments | | | | +0.06 | -0.54 | -1.08 | -0.54 | -0.63 | -0.32 | -0.15 | -0.30 | -0.28 | -0.45 | | | | | | | | | |
| | | | +0.24 | +0.08 | +0.16 | +0.08 | +0.04 | +0.22 | +0.19 | +0.10 | +0.05 | +0.09 | +0.08 | +0.07 | +0.15 | +0.08 | +0.04 | | | | | |
| | | | +0.04 | -0.01 | -0.07 | -0.13 | -0.06 | -0.07 | -0.04 | -0.04 | -0.07 | +2.93 | -0.97 | -0.68 | -1.28 | -0.93 | -0.02 | -0.01 | -0.03 | | | |
| | | | +0.28 | +0.15 | -0.43 | | | | | | | | | | | | | | | | | |
| | | | -3.72 | +32.00 | -46.60 | | | | | | | | | | | | | | | | | |
| | | | -19.32 | | | | | | | | | | | | | | | | | | | |
| | | | | | | | | | | | | | | | | | | | | | | |
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| | | | | | | | | | | | | | | | | | | | | | | |

Checking Results:

$$R_1 + R_2 = 18.32 + 28.88 = 47.20 = 27.80 \times 1.70$$

$$\sum F_x = 55.70 - 2 \times 27.80 = 0.107$$

∴ O.K.



ANALYSIS OF THE EFFECT OF WIND ON A HIGH REINFORCED CONCRETE BUILDING

Comparison of Approximate and Exact Methods

| | | |
|------------|-----------------|----------------------|
| COMPUTER : | RIAD SHAHIN | WIND ANALYSIS |
| CHK'D BY : | RIAD SHAHIN | HARDY CROSS METHOD |
| APP'D BY : | DR. JACK NASSER | DATE : DECEMBER 1964 |
| | | SHEET NO 83 / |

5 - 4 - 3 Floors

1. Shears

$$V_3 = \frac{-2}{1.70} (-17.20 - 12.20) = \frac{-2}{1.70} (-29.40) = +34.60 = +34.60 \Delta 5/10^4$$

$$V_4 = \frac{-2}{3.40} (+25.20 + 67.00 + 23.70 + 59.50) = \frac{-2}{3.40} (+175.40) = -103 = -103 \Delta 5/10^4$$

$$V_5 = \frac{-2}{3.40} (-119.70 - 89.90 - 142.00 - 123.90) = \frac{-2}{3.40} (-475.50) = +280 = +280 \Delta 5/10^4$$

$$V_3 = \frac{-2}{1.70} (+136.80 + 100.70) = \frac{-2}{1.70} (+237.50) = -303 = -303 \Delta 4/10^4$$

$$V_4 = \frac{-2}{3.40} (-205.30 - 176.90 - 231.60 - 213.50) = \frac{-2}{3.40} (-827.30) = +485 = +485 \Delta 4/10^4$$

$$V_5 = \frac{-2}{3.40} (+73.20 + 10.80 + 59.90 + 21.60) = \frac{-2}{3.40} (+173.50) = -102 = -102 \Delta 4/10^4$$

$$V_3 = \frac{-2}{1.70} (-382.30 - 447.30) = \frac{-2}{1.70} (-829.60) = +975 = +975 \Delta 3/10^4$$

$$V_4 = \frac{-2}{3.40} (+200.90 + 63.40 + 177.80 + 63.90) = \frac{-2}{3.40} (+514.00) = -302 = -302 \Delta 3/10^4$$

$$V_5 = \frac{-2}{3.40} (-27.60 - 6.90 - 17.20 - 6.50) = \frac{-2}{3.40} (-58.20) = +34.30 = +34.30 \Delta 3/10^4$$

2. Effect of 6th floor

$$V_3 = \frac{-2}{1.70} (+0.20 + 0.29) = \frac{-2}{1.70} (+0.57) = -0.67$$

$$V_4 = \frac{-2}{3.40} (-0.43 - 1.13 - 0.50 - 1.20) = \frac{-2}{3.40} (-3.34) = +1.97$$

$$V_5 = \frac{-2}{3.40} (+1.69 + 4.45 + 2.93 + 6.95) = \frac{-2}{3.40} (+16.02) = -9.40$$

3. Δ 's

$$+34.60 \Delta 5 - 303 \Delta 4 + 975 \Delta 3 = (55.70 - 0.67) 10^4 = 55.03 \times 10^4$$

$$-103 \Delta 5 + 485 \Delta 4 - 302 \Delta 3 = (53.30 + 1.97) 10^4 = 55.27 \times 10^4$$

$$+280 \Delta 5 - 102 \Delta 4 + 34.30 \Delta 3 = (50.70 - 9.40) 10^4 = 41.30 \times 10^4$$

$$\Delta 3 = 0.122$$

$$\Delta 4 = 0.236$$

$$\Delta 5 = 0.218$$

4 - 3 - 2 Floors

1. Shears

$$V_2 = \frac{-2}{2.45} (-20.00 - 14.00) = \frac{-2}{2.45} (-34.00) = +27.70 = +27.70 \Delta_4 / 10^4$$

$$V_3 = \frac{-2}{3.40} (+33.30 + 95.30 + 32.80 + 85.80) = \frac{-2}{3.40} (+247.20) = -145 = -145 \Delta_4 / 10^4$$

$$V_4 = \frac{-2}{3.40} (-171.90 - 131.30 - 208.20 - 185.60) = \frac{-2}{3.40} (-697.00) = +410 = +410 \Delta_4 / 10^4$$

$$V_8 = \frac{-2}{2.45} (+115.80 + 119.50) = \frac{-2}{2.45} (+235.30) = -192 = -192 \Delta_3 / 10^4$$

$$V_3 = \frac{-2}{3.40} (-197.00 - 191.40 - 284 - 282.30) = \frac{-2}{3.40} (-854.70) = +490 = +490 \Delta_3 / 10^4$$

$$V_4 = \frac{-2}{3.40} (+104.40 + 24.20 + 89.50 + 29.60) = \frac{-2}{3.40} (+247.70) = -146 = -146 \Delta_3 / 10^4$$

$$V_2 = \frac{-2}{2.45} (-217.60 - 244.90) = \frac{-2}{2.45} (-462.50) = +377 = +377 \Delta_2 / 10^4$$

$$V_3 = \frac{-2}{3.40} (+120.80 + 40.20 + 38.50) = \frac{-2}{3.40} (+300.70) = -177 = -177 \Delta_2 / 10^4$$

$$V_4 = \frac{-2}{3.40} (-22.40 - 5.10 - 14.80 - 5.30) = \frac{-2}{3.40} (-47.60) = +28 = +28 \Delta_2 / 10^4$$

2. Effect of 5th floor.

$$V_2 = \frac{-2}{2.45} (+0.23 + 0.23) = \frac{-2}{2.45} (+0.46) = -0.38$$

$$V_3 = \frac{-2}{3.40} (-0.41 - 1.18 - 0.50 - 1.29) = \frac{-2}{3.40} (-3.38) = +2.00$$

$$V_4 = \frac{-2}{3.40} (+2.21 + 6.40 + 3.07 + 0.24) = \frac{-2}{3.40} (+19.92) = -12.70$$

3. Δ 's

$$+27.70 \Delta_4 - 192 \Delta_3 + 377 \Delta_2 = (58.40 - 0.38) 10^4 = 58.02 \times 10^4$$

$$-145 \Delta_4 + 490 \Delta_3 - 177 \Delta_2 = (55.70 + 2.00) 10^4 = 57.70 \times 10^4$$

$$+410 \Delta_4 - 146 \Delta_3 + 28 \Delta_2 = (53.30 - 12.70) 10^4 = 40.60 \times 10^4$$

$$\Delta_2 = 0.277$$

$$\Delta_3 = 0.267$$

$$\Delta_4 = 0.174$$

| JOINT | 1 | | | 2 | | | 3 | | | 3a | | | 2a | | | 1a | | | 0a | |
|------------------------------------|---|------|------|------|------|------|------|------|------|------|--------|------|--------|--------|------|------|------|---|----|--|
| | M | I | S | I | R | S | I | R | S | L | R | I | S | L | R | I | S | | | |
| MEMBER | 0 | 0.48 | 0.22 | 0.30 | 0.32 | 0.23 | 0.45 | 0.66 | 0.54 | 0.25 | 0.25 | 0.50 | 0.37 | 0.19 | 0.18 | 0.25 | 0.25 | 0 | | |
| DIST. FACTOR | 0 | | | | | | | | | | | | | | | | | | 0 | |
| Influence of ΔW | | | | +34 | +6.8 | +49 | +96 | +48 | +30 | +60 | +59.50 | +119 | +59.50 | +24.50 | | | | | | |
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| Influence of ΔZ | | | | | | | | | | | | | | | | | | | | |
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| Influence of $\Delta 1$ | | | | | | | | | | | | | | | | | | | | |
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| Influence of Moment of Above Floor | | | | | | | | | | | | | | | | | | | | |
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| Final Moments | | | | | | | | | | | | | | | | | | | | |
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Checking Results:

$R_1 + R_2 = 46.22 + 12.70 + 23.20 + 57.60 = 33.72 = 30T$

$\sum F_x = 60 - 30 \times 2 = 0T$

O.K.

ANALYSIS OF THE EFFECT OF WIND ON A HIGH REINFORCED CONCRETE BUILDING

Comparison of Approximate and Exact Methods

| COMPUTER : | RIAD SHAHIN | WIND ANALYSIS |
|------------|-----------------|---------------------|
| CHK'D BY : | RIAD SHAHIN | HARDY CROSS METHOD |
| APP'D BY : | DR. JACK NASSER | DATE: DECEMBER 1964 |

SHEET N° 87 /

3 - 2 - 1 Floors

1. Shears

$$V_1 = \frac{-2}{4.50} (-9.30 - 10.40 - 6.50 - 12.70) = \frac{-2}{4.50} (-46.90) = +20.80 = +20.80 \Delta_3 / 10^4$$

$$V_2 = \frac{-2}{4.90} (+29.70 + 76.70 + 20.20 + 60.20) = \frac{-2}{4.90} (+202.80) = -83 = -83 \Delta_3 / 10^4$$

$$V_3 = \frac{-2}{3.40} (-162.30 - 120.90 - 201.30 - 175.80) = \frac{-2}{3.40} (-660.30) = +391 = 391 \Delta_3 / 10^4$$

$$V_1 = \frac{-2}{4.50} (+34.00 + 67.80 + 29.10 + 58.10) = \frac{-2}{4.50} (+189.00) = -84 = -84 \Delta_2 / 10^4$$

$$V_2 = \frac{-2}{4.90} (-111.70 - 108.50 - 123.60 - 122.70) = \frac{-2}{4.90} (-466.50) = +190 = +190 \Delta_2 / 10^4$$

$$V_3 = \frac{-2}{3.40} (+59.00 + 13.80 + 49.30 + 16.30) = \frac{-2}{3.40} (+138.40) = -81.20 = -81.20 \Delta_2 / 10^4$$

$$V_1 = \frac{-2}{4.50} (-154.90 - 116.90 - 174.20 - 135.90) = \frac{-2}{4.50} (-591.90) = +263 = +263 \Delta_1 / 10^4$$

$$V_2 = \frac{-2}{4.90} (+55.20 + 20.50 + 45.50 + 10.60) = \frac{-2}{4.90} (+139.80) = -57 = -57 \Delta_1 / 10^4$$

$$V_3 = \frac{-2}{3.40} (-11.20 - 2.50 - 7.10 - 2.50) = \frac{-2}{3.40} (-23.30) = +13.70 = 13.70 \Delta_1 / 10^4$$

2. Effect of 4th floor

$$V_1 = \frac{-2}{4.50} (+0.05 + 0.11 + 0.10 + 0.19) = \frac{-2}{4.50} (+0.45) = -0.20$$

$$V_2 = \frac{-2}{4.90} (-0.22 - 0.55 - 0.39 - 0.95) = \frac{-2}{4.90} (-2.11) = +0.86$$

$$V_3 = \frac{-2}{3.40} (+1.34 + 3.94 + 2.50 + 7.29) = \frac{-2}{3.40} (+15.15) = -0.90$$

3. Δ . S

$$+20.80 \Delta_3 - 84 \Delta_2 + 263 \Delta_1 = (60.00 - 0.20) 10^4 = 59.80 \times 10^4$$

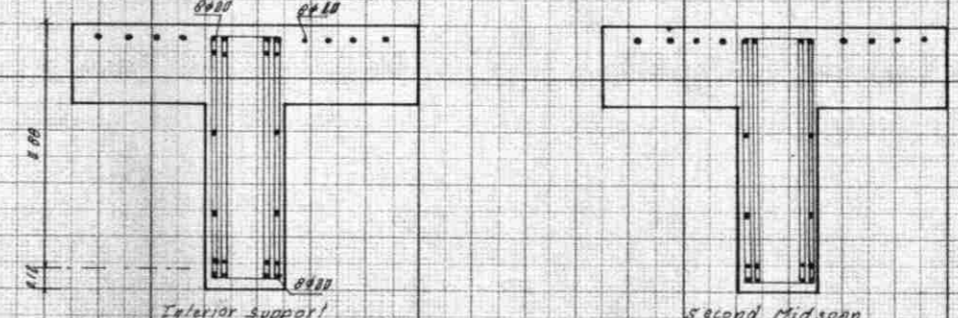
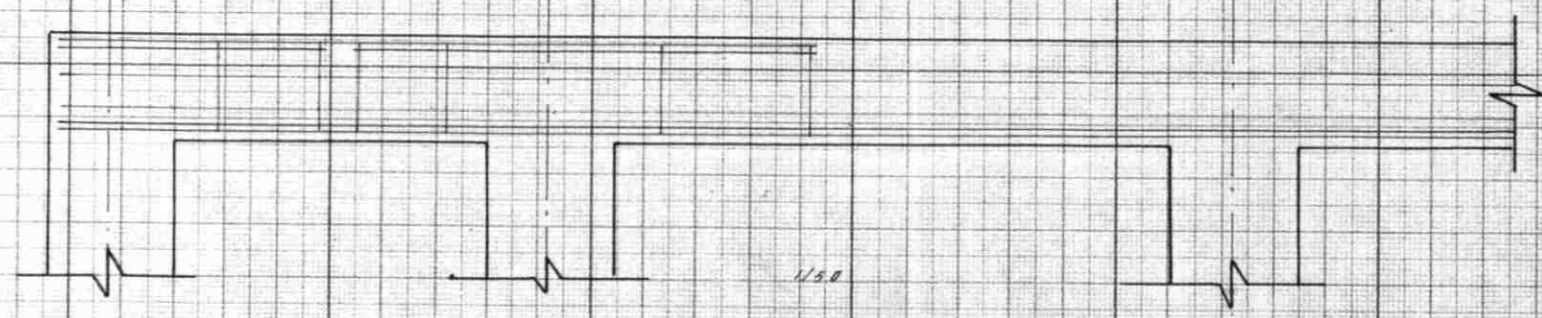
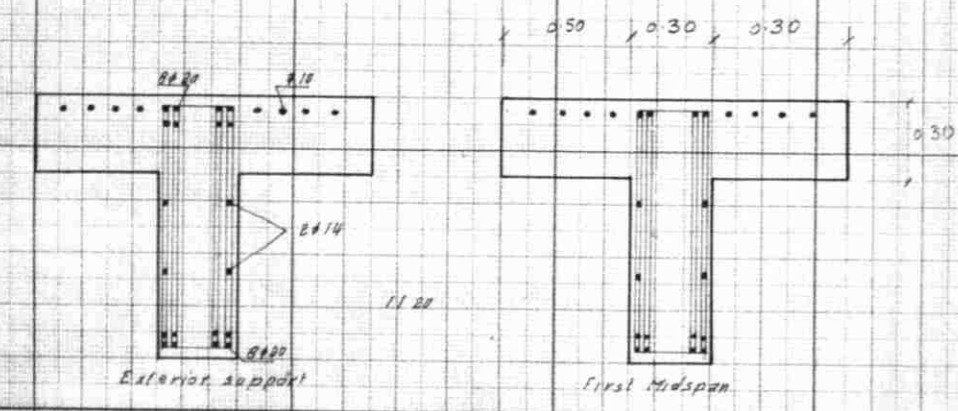
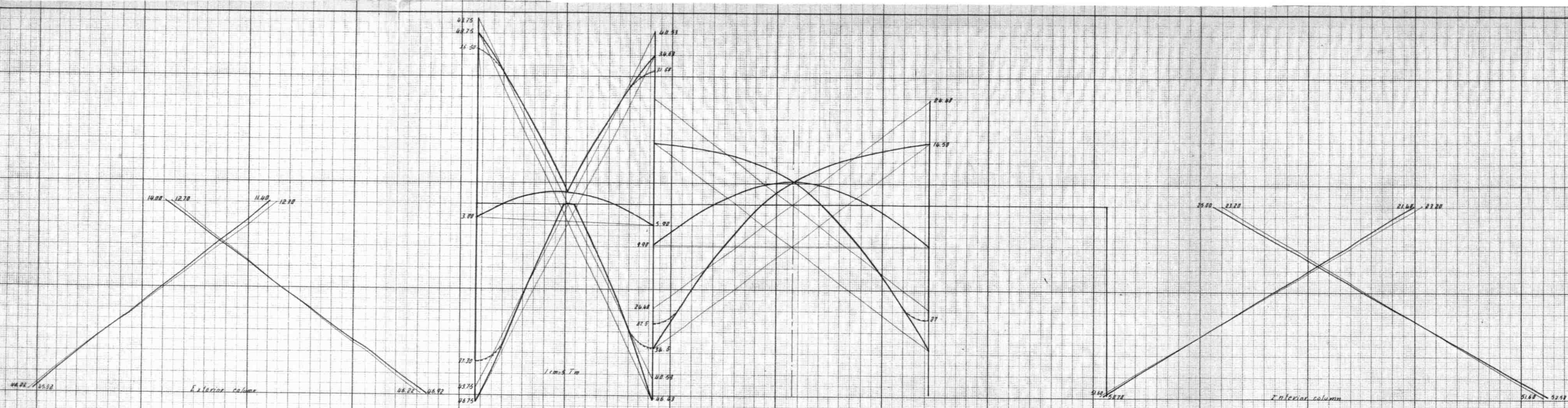
$$-83 \Delta_3 + 190 \Delta_2 - 57 \Delta_1 = (58.40 + 0.86) 10^4 = 59.26 \times 10^4$$

$$+391 \Delta_3 - 81.20 \Delta_2 + 13.70 \Delta_1 = (55.70 - 8.90) 10^4 = 46.80 \times 10^4$$

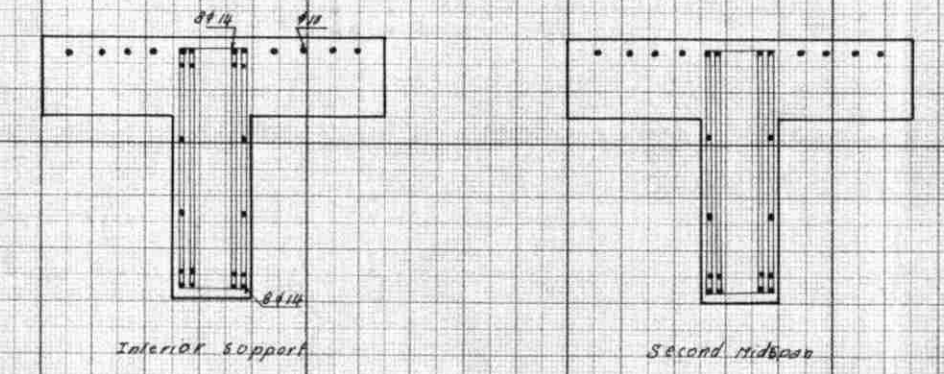
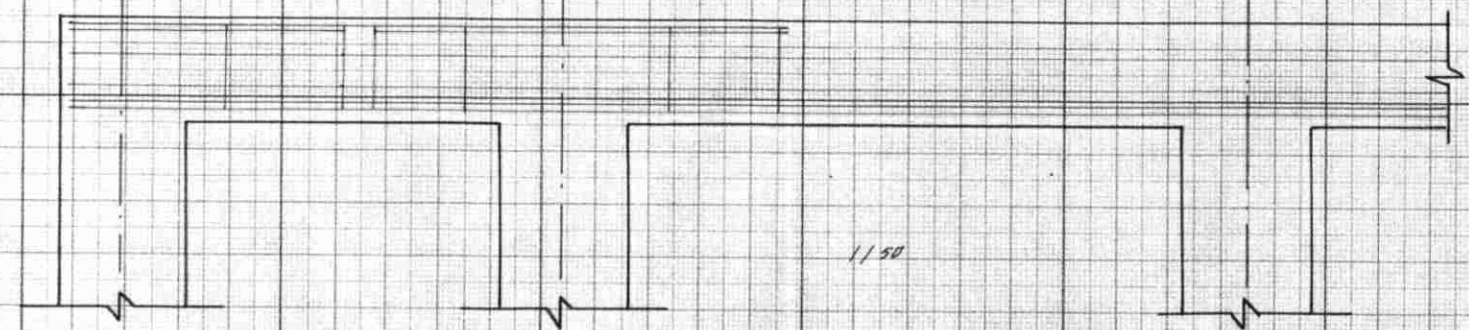
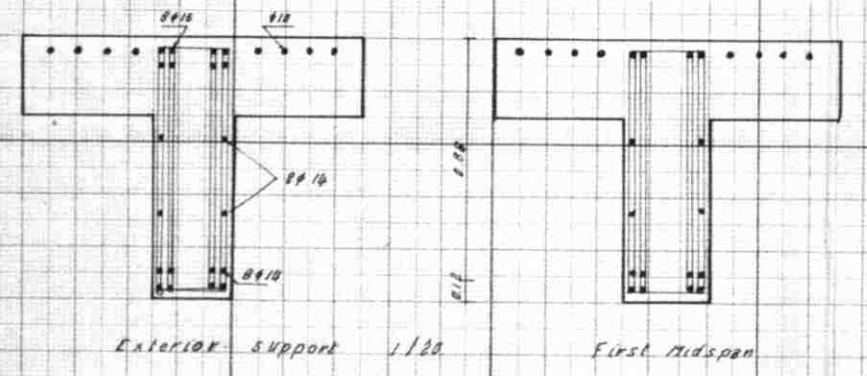
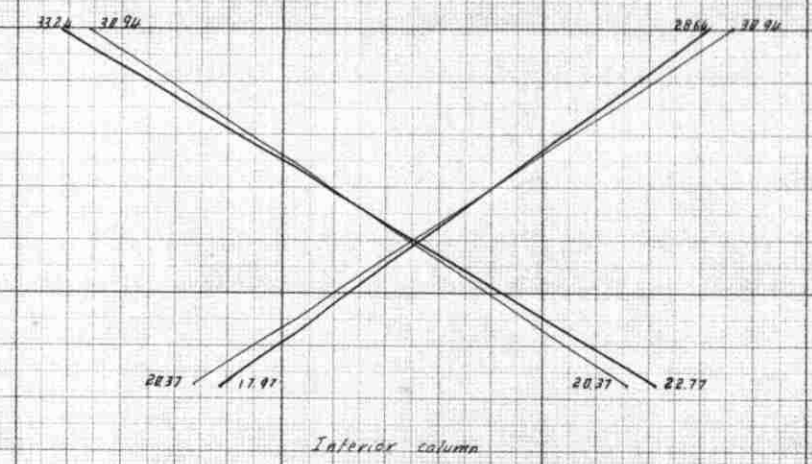
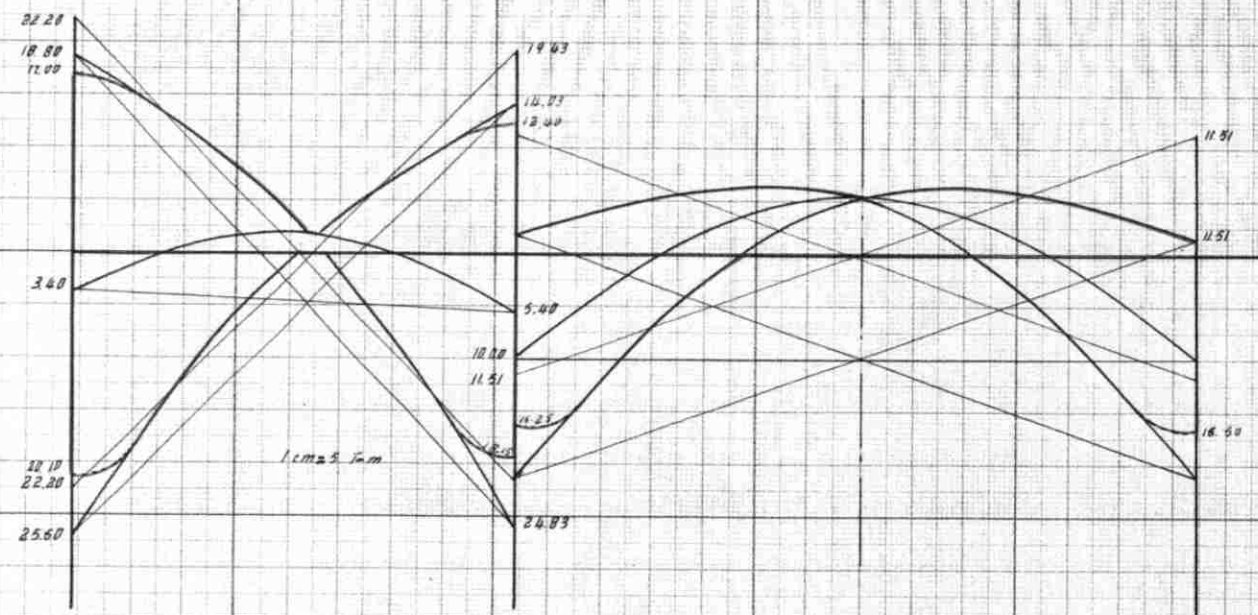
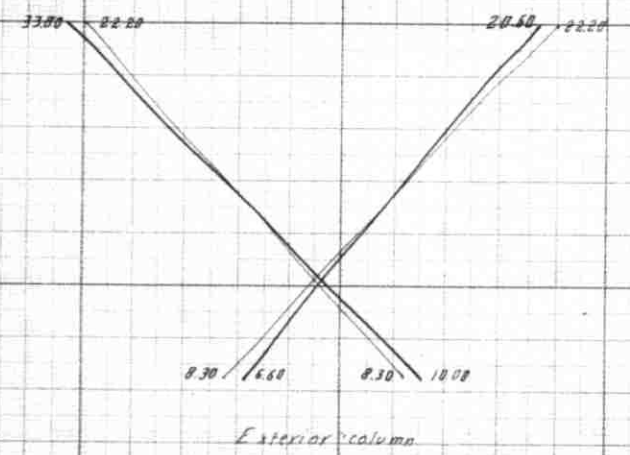
$$\Delta_1 = 0.376$$

$$\Delta_2 = 0.527$$

$$\Delta_3 = 0.217$$



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|--|-----------------|------------------------|---------------|
| ANALYSIS OF THE EFFECT OF WIND ON A HIGH REINFORCED CONCRETE BUILDING | | | |
| Comparison of Approximate and Exact Methods | | | |
| DRAWN BY : | RIAD SHAHIN | ENVELOPE DIAGRAMS | |
| CHK'D BY : | RIAD SHAHIN | REINFORCEMENT IN BEAMS | |
| APP'D BY : | DR. JACK NASSER | DATE : DECEMBER 1964 | SHEET NO 09 / |

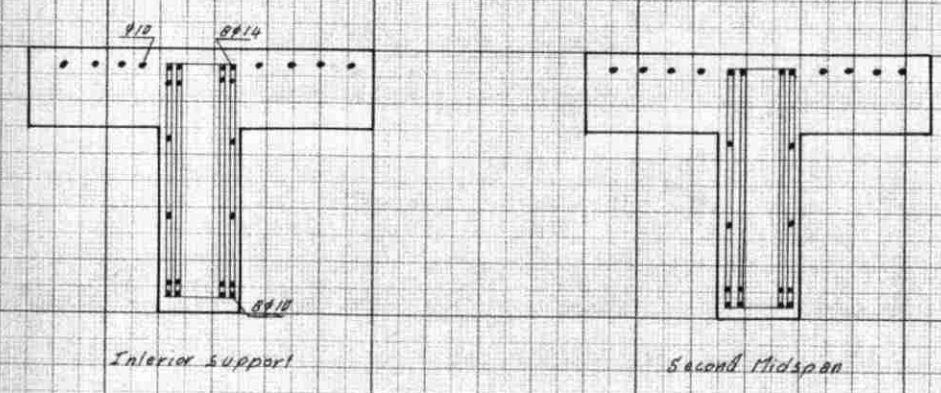
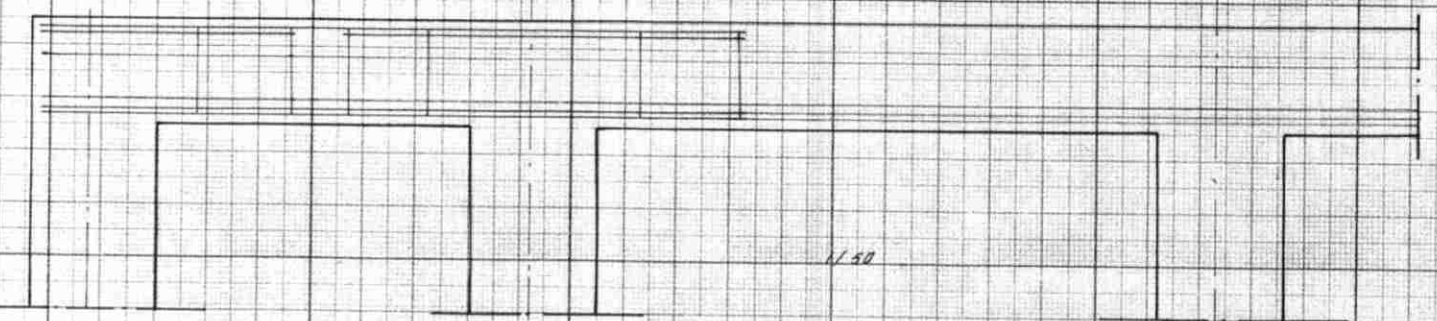
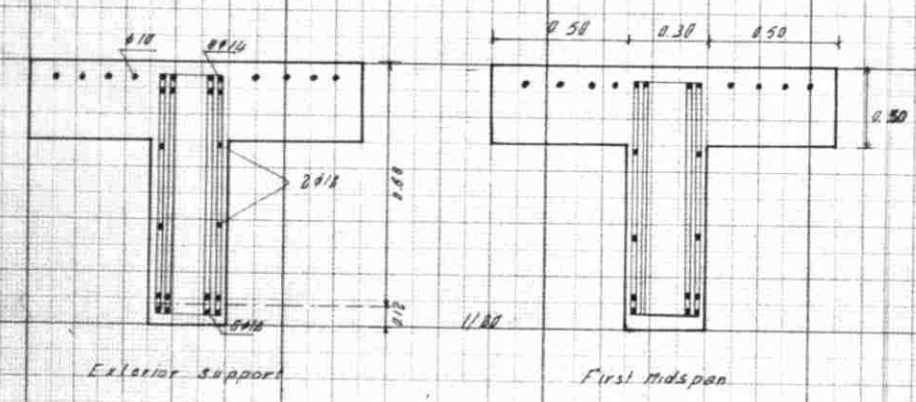
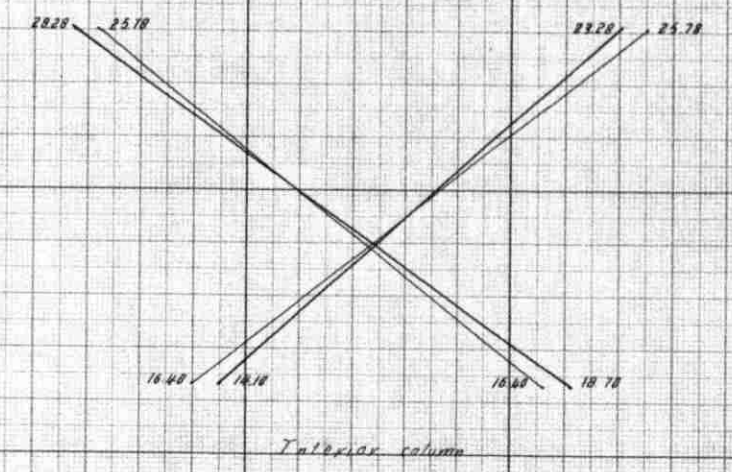
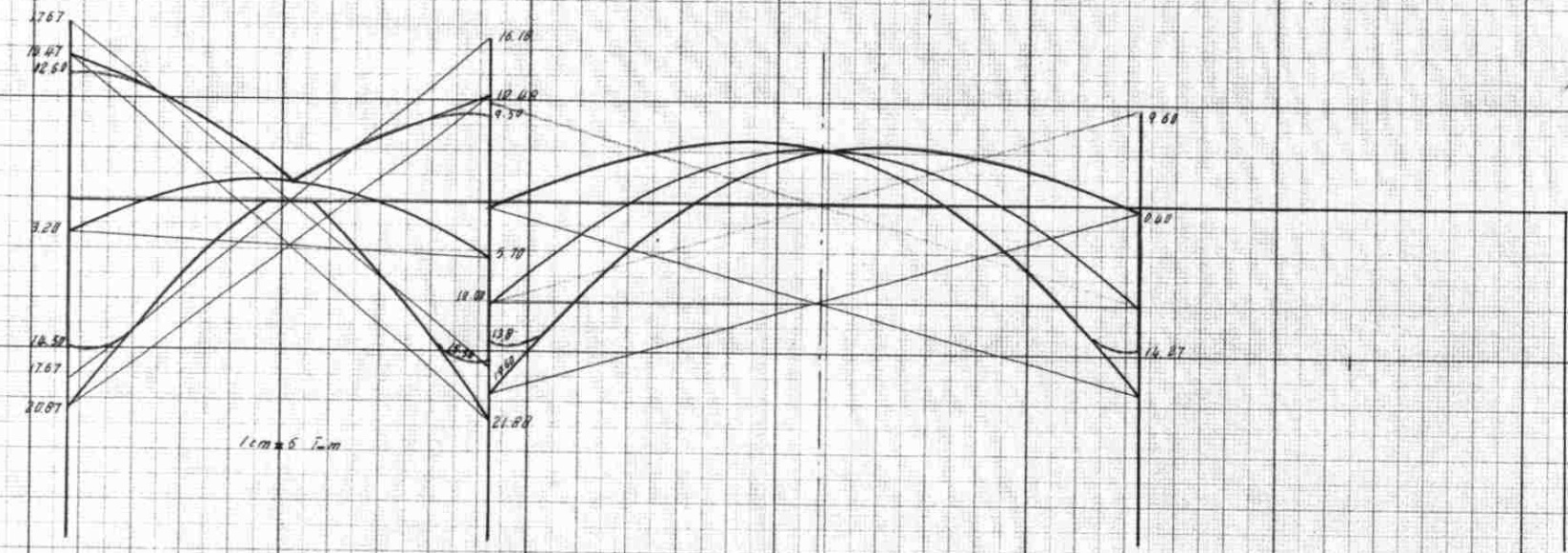
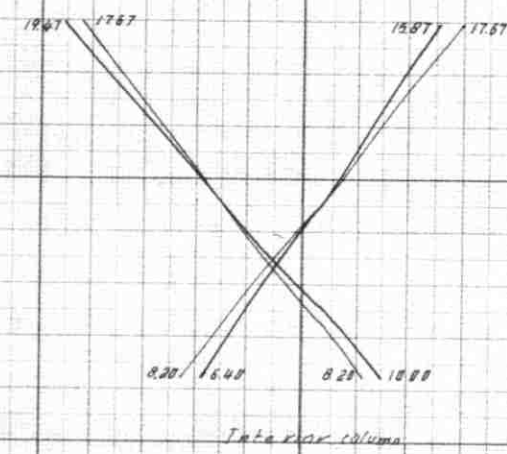


ANALYSIS OF THE EFFECT OF WIND ON A HIGH REINFORCED CONCRETE BUILDING
 Comparison of Approximate and Exact Methods

ENVELOPE DIAGRAMS
 REINFORCEMENT IN BEAMS

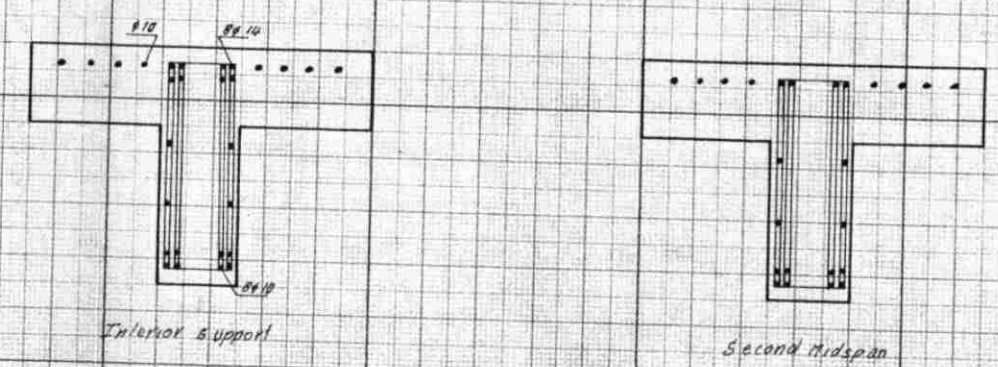
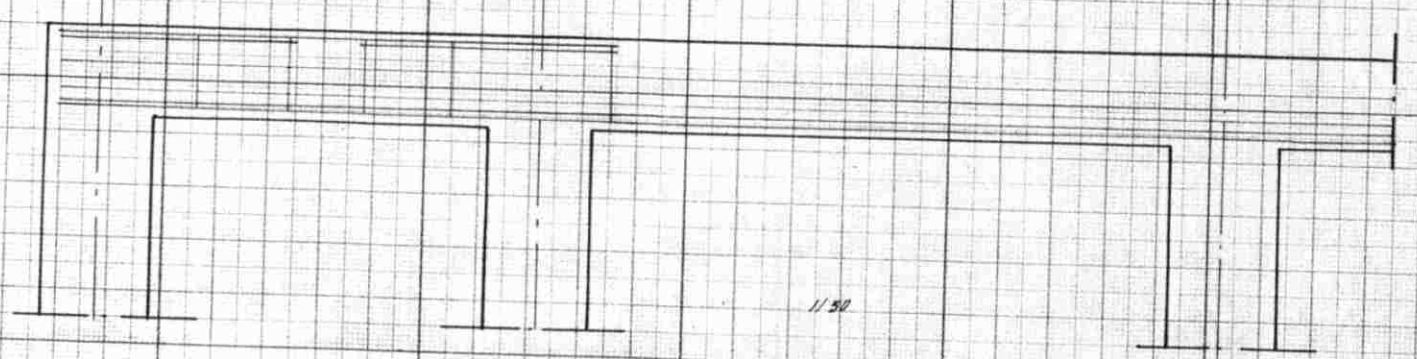
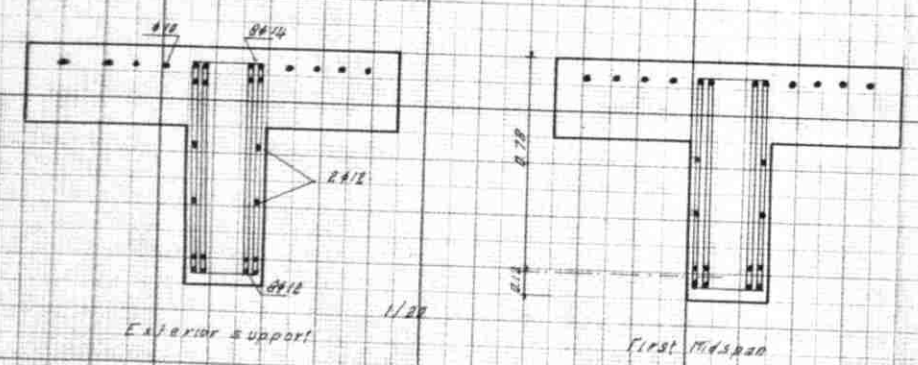
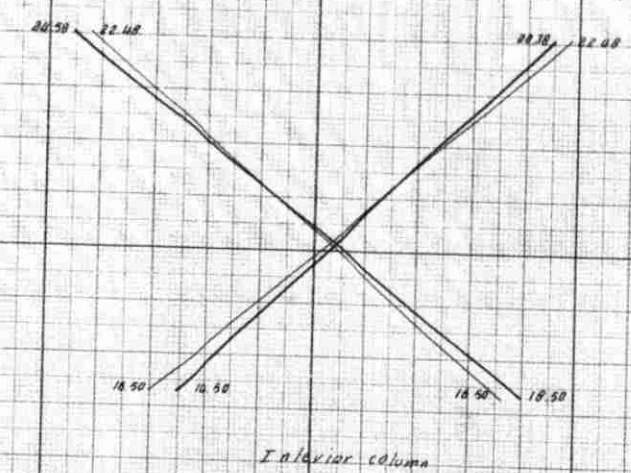
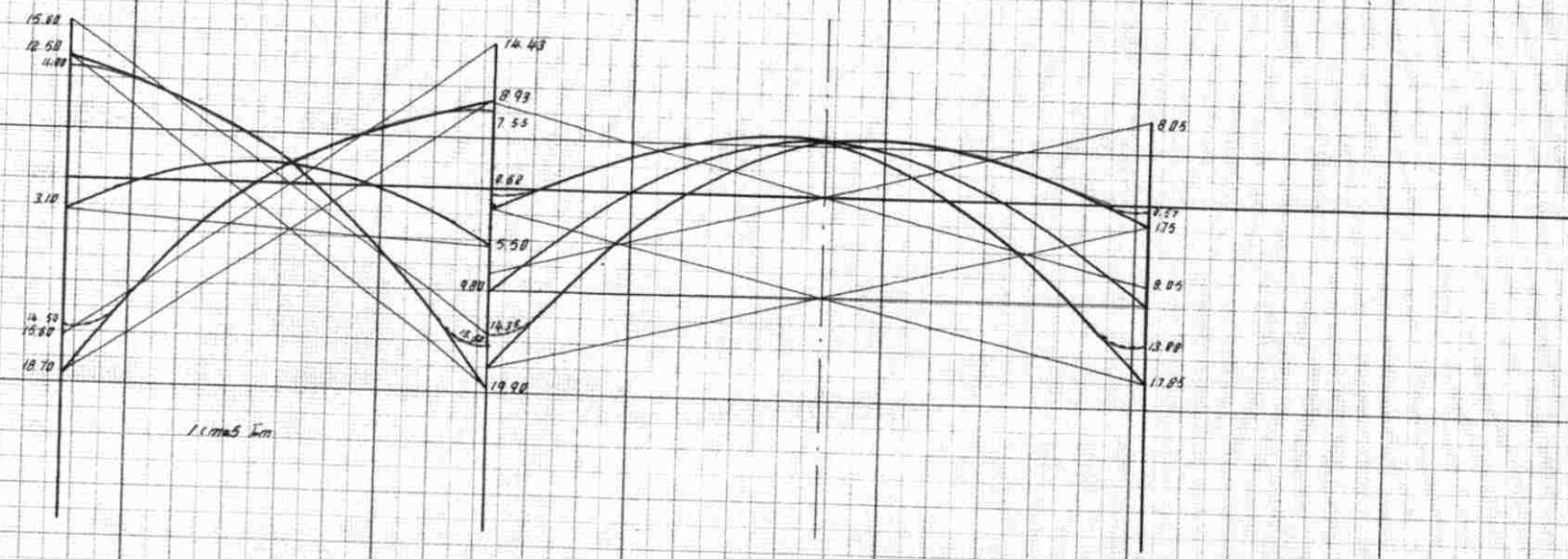
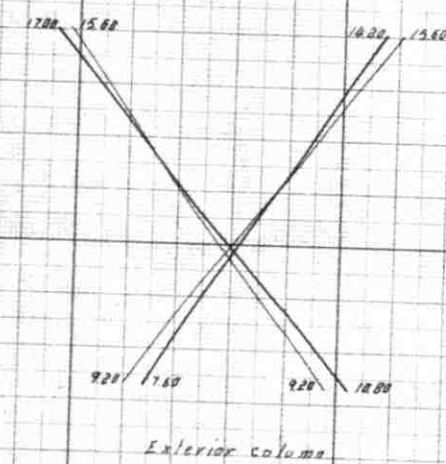
DRAWN BY: RIAD SHAHIN
 CH'D BY: RIAD SHAHIN
 APP'D BY: DR. JACK NASSER

DATE: DECEMBER 1964 SHEET NO 9/

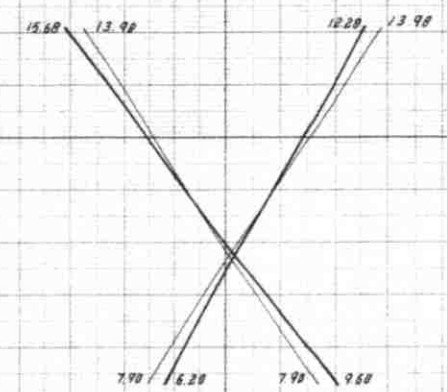


ANALYSIS OF THE EFFECT OF WIND ON A HIGH REINFORCED CONCRETE BUILDING
Comparison of Approximate and Exact Methods

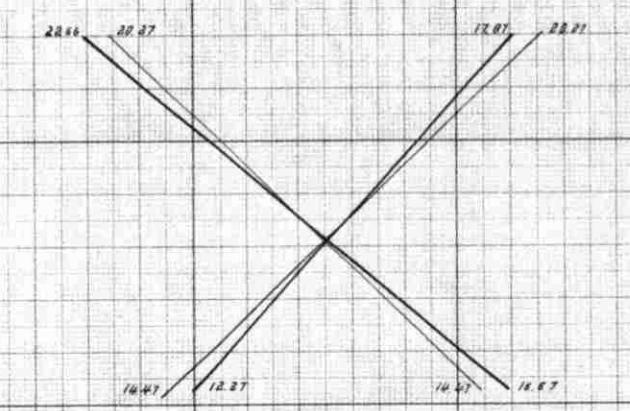
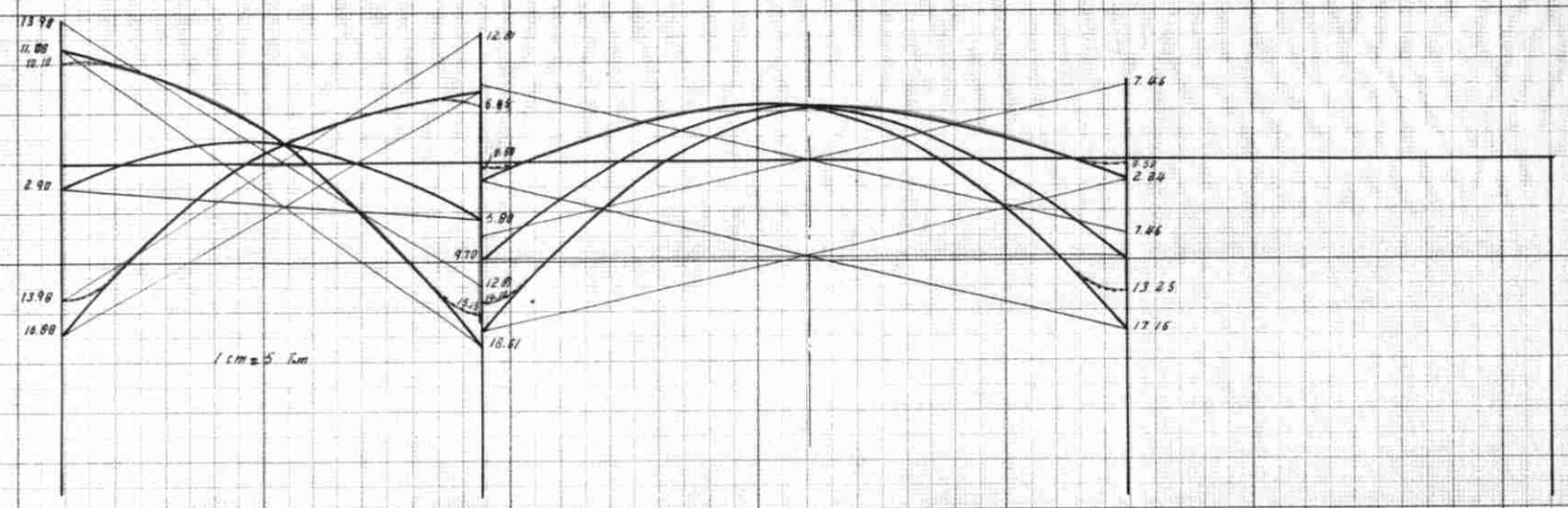
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|------------|----------------------------|------------------------|
| DRAWN BY : | RIAD SHAHIN | ENVELOPE DIAGRAMS |
| CHK'D BY : | RIAD SHAHIN | REINFORCEMENT IN BEAMS |
| APP'D BY : | D ^r JACK NASSER | DATE : DECEMBER 1964 |
| | | SHEET NO 92 |



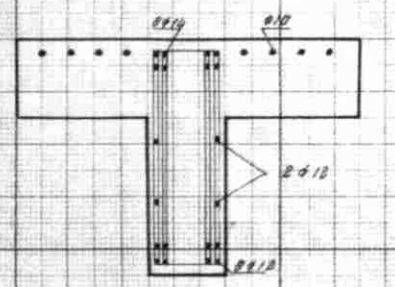
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| ANALYSIS OF THE EFFECT OF WIND ON A HIGH REINFORCED CONCRETE BUILDING. Comparison of Approximate and Exact Methods | |
| DRAWN BY : RIAD SHAHIN CHK'D BY : RIAD SHAHIN APP'D BY : DR. JACK NASSER | ENVELOPE DIAGRAMS REINFORCEMENT IN BEAMS |
| DATE: DECEMBER 1964 | SHEET NO. 35 |



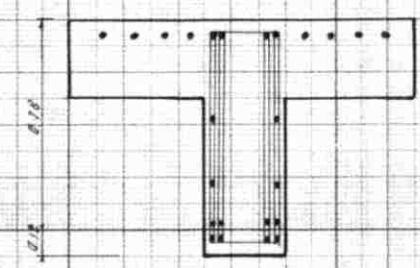
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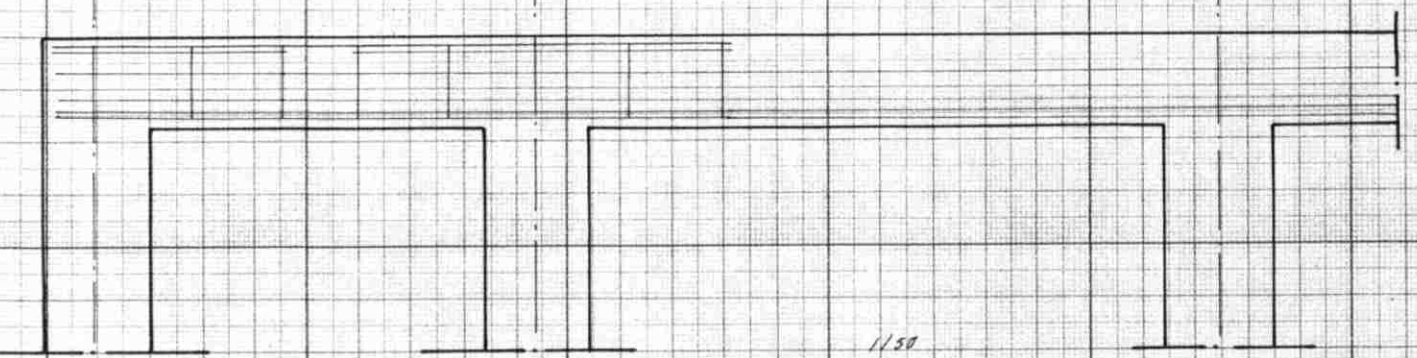
Interior column



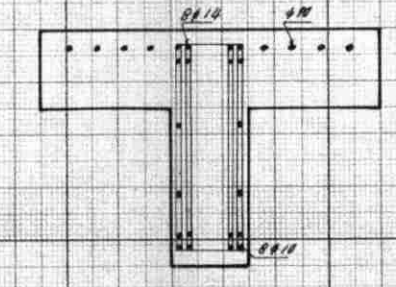
Exterior support



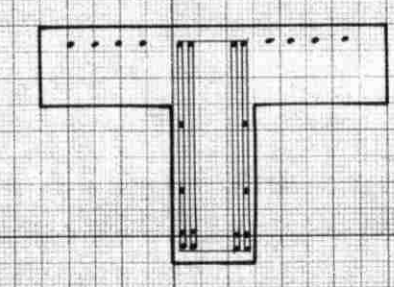
First midspan



1/50

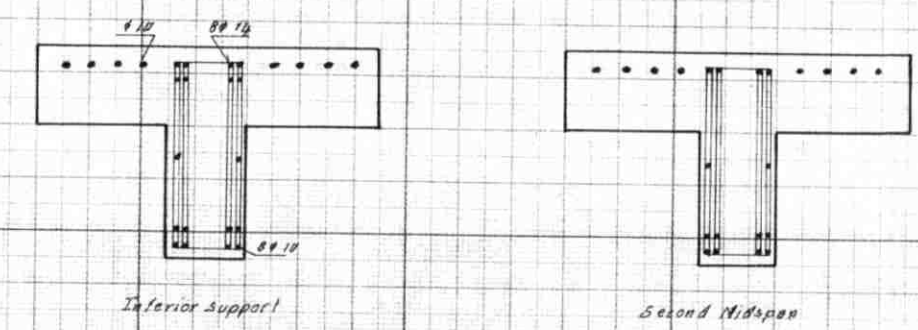
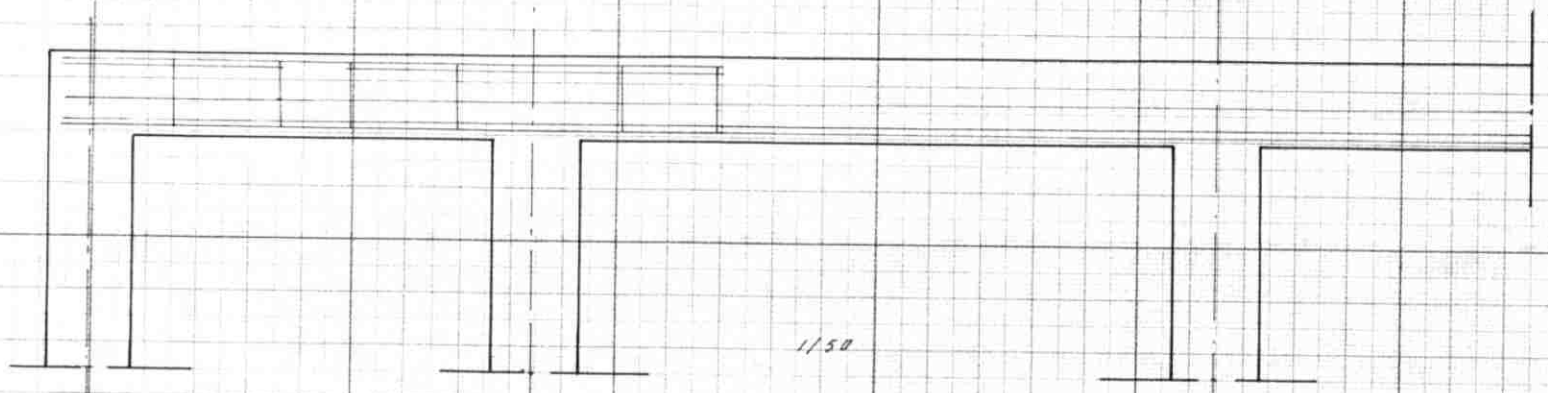
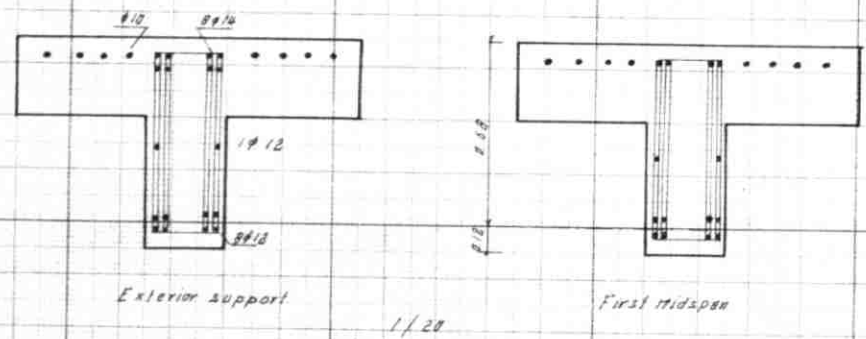
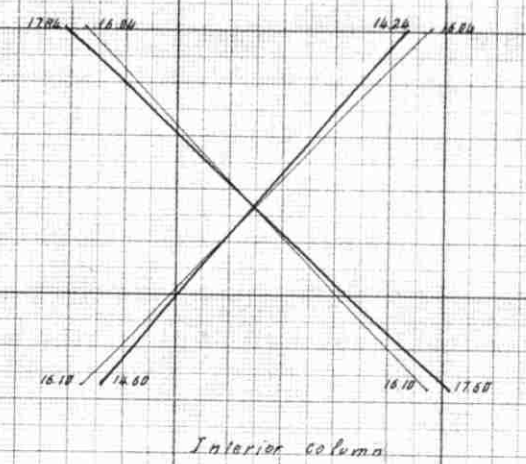
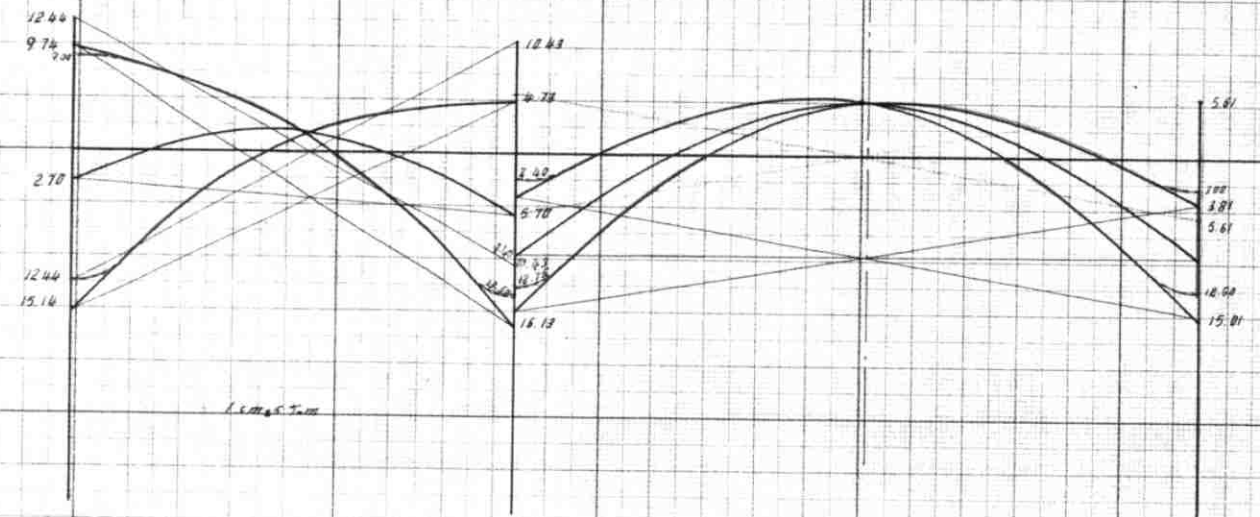
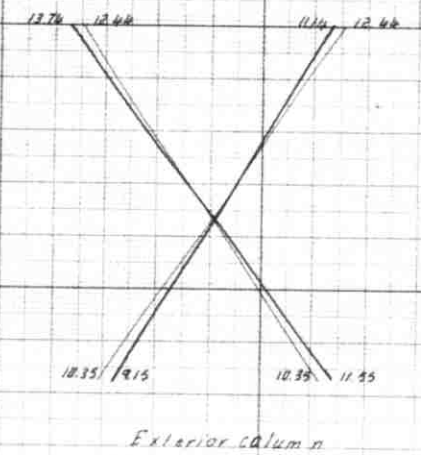


Interior support

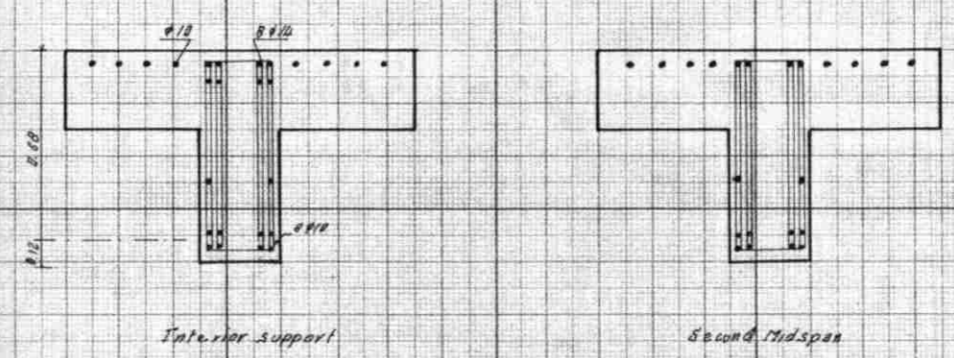
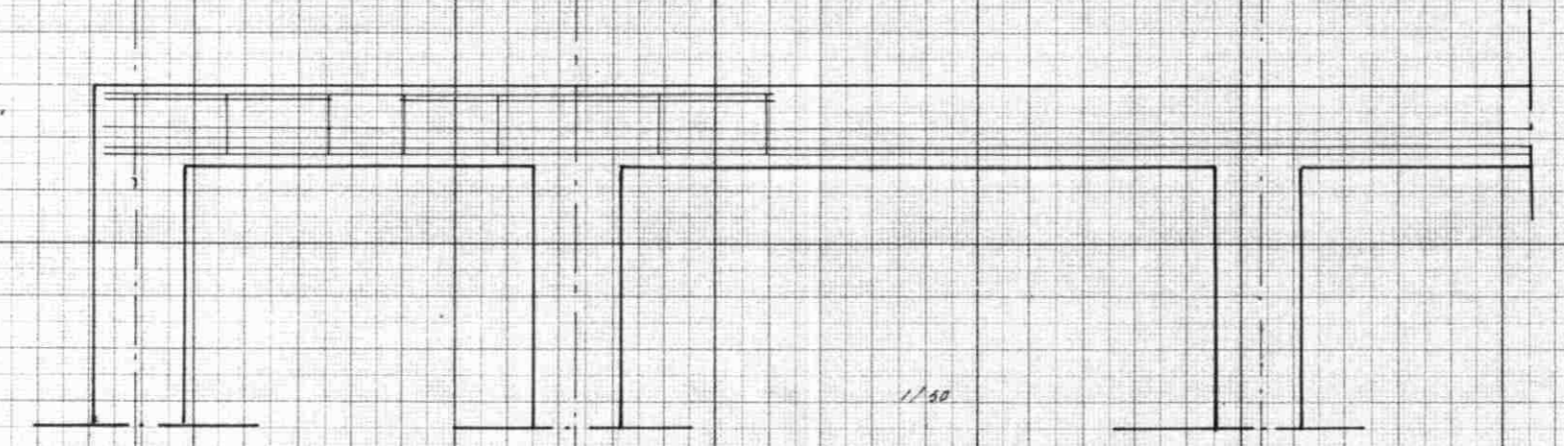
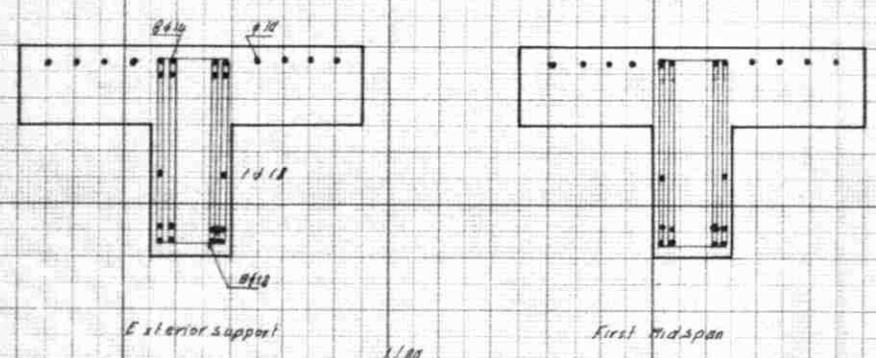
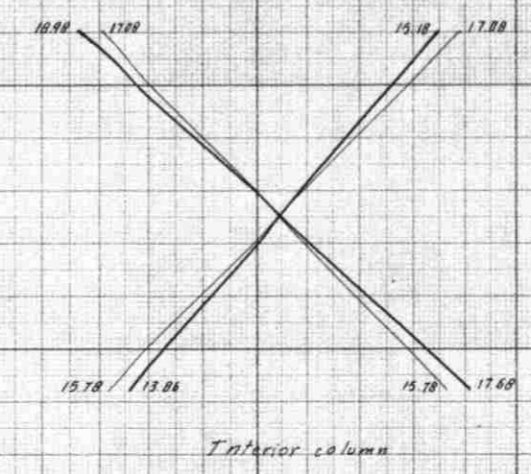
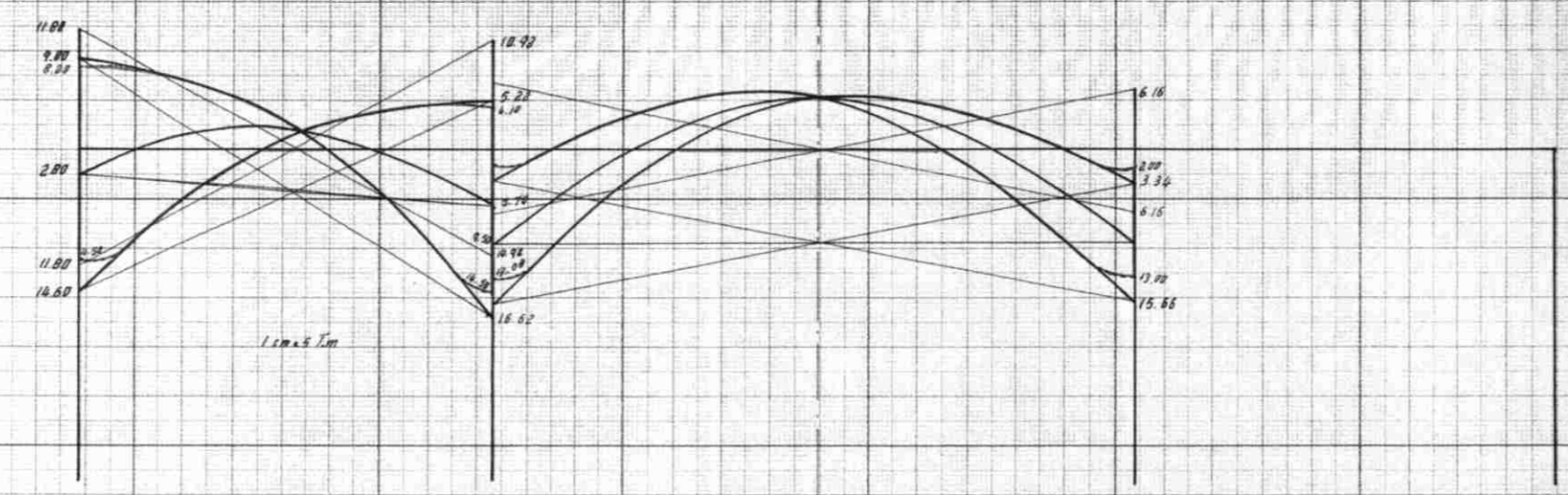
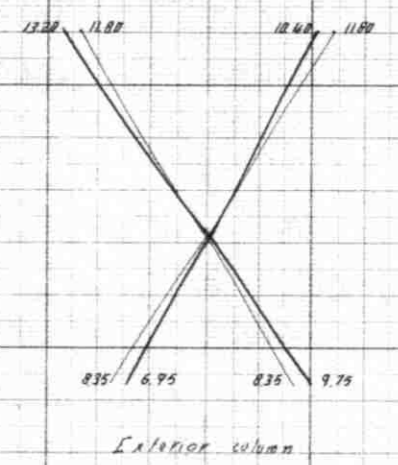


Second midspan

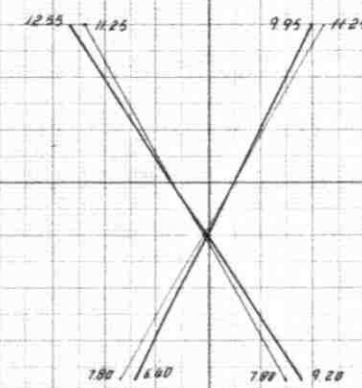
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| ANALYSIS OF THE EFFECT OF WIND ON A HIGH REINFORCED CONCRETE BUILDING | | | |
| Comparison of Approximate and Exact Methods | | | |
| DRAWN BY : | RIAD SHAHIN | ENVELOPE DIAGRAMS | |
| CHK'D BY : | RIAD SHAHIN | REINFORCEMENT IN BEAMS | |
| APP'D BY : | DR JACK NASSER | DATE: DECEMBER 1964 | SHEET N° 96 / |



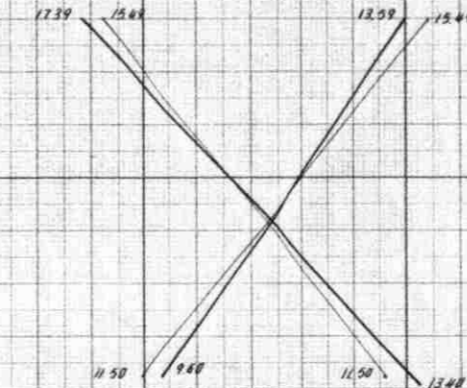
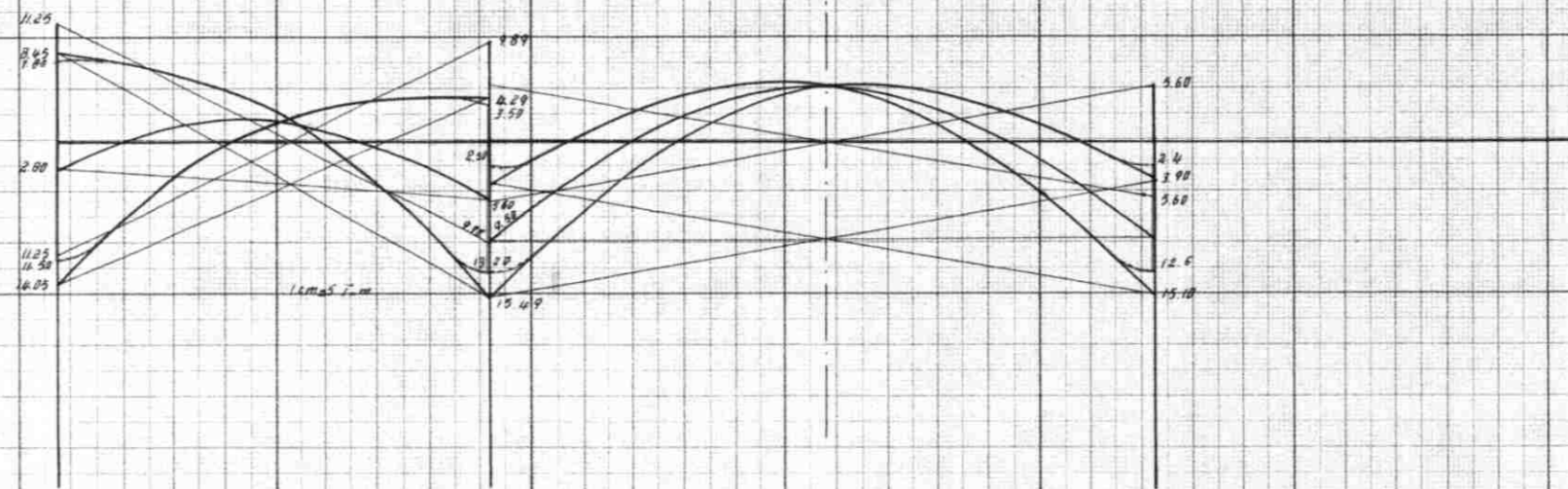
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| ANALYSIS OF THE EFFECT OF WIND ON A HIGH REINFORCED CONCRETE BUILDING | | | |
| Comparison of Approximate and Exact Methods | | | |
| DRAWN BY : RIAH SHAHIN | | ENVELOPE DIAGRAMS | |
| CHK'D BY : RIAH SHAHIN | | REINFORCEMENT IN BEAMS | |
| APP'D BY : DR. JACK NASSER | | DATE : DECEMBER 1964 | SHEET N° 97 / |



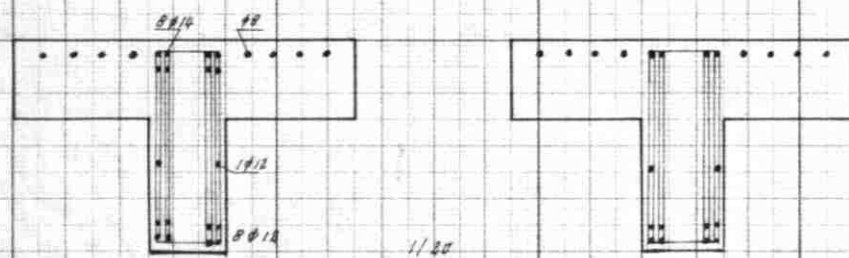
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| DRAWN BY | RIAD SHAHIN | ENVELOPE DIAGRAMS | |
| CHECKED BY | RIAD SHAHIN | REINFORCEMENT IN BEAMS | |
| APPROVED BY | DR. JACK NASSER | DATE: DECEMBER 1964 | SHEET N° 98 / |



Exterior column

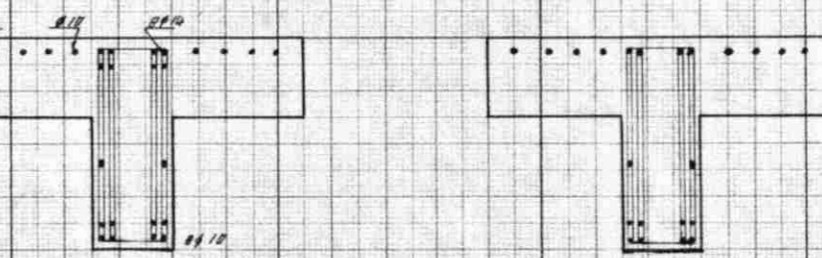
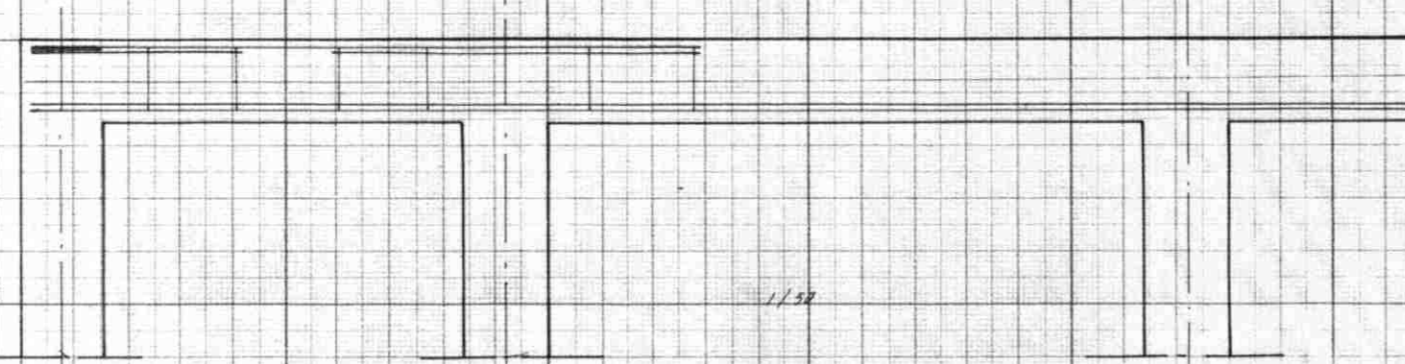


Interior column



Exterior support

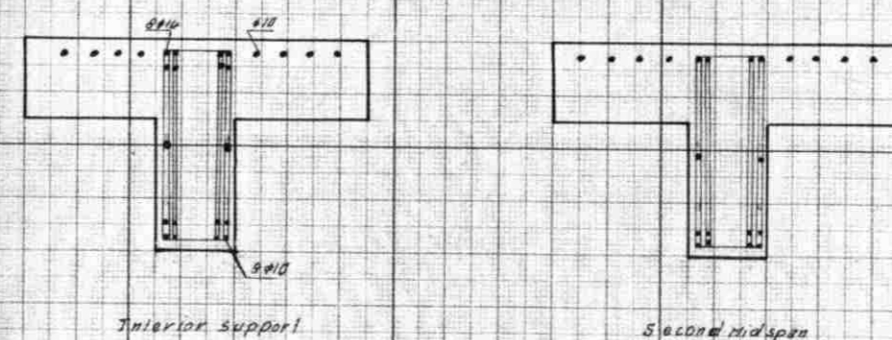
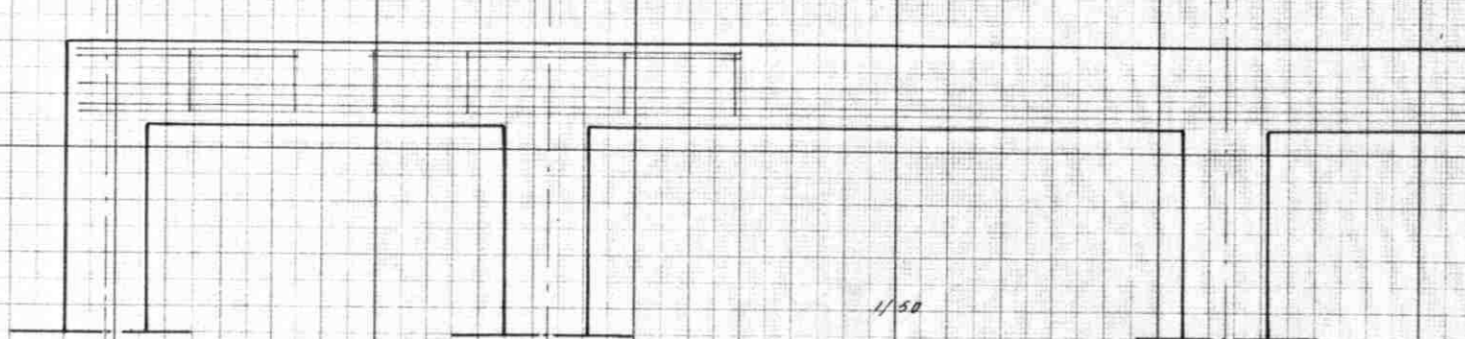
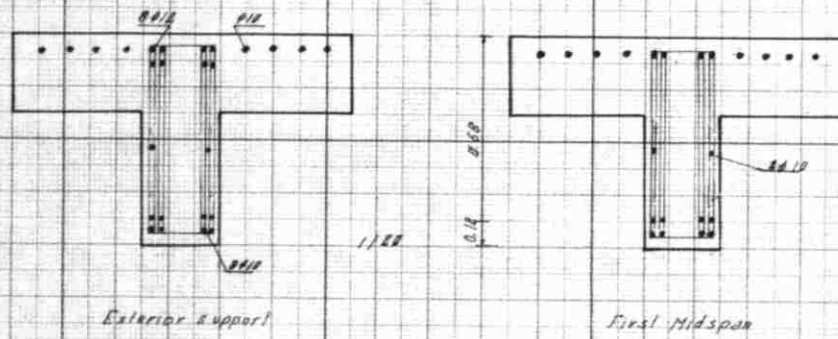
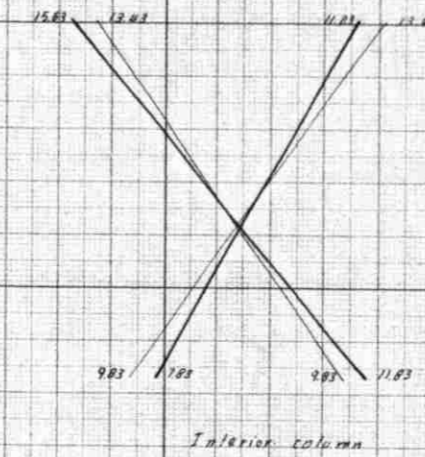
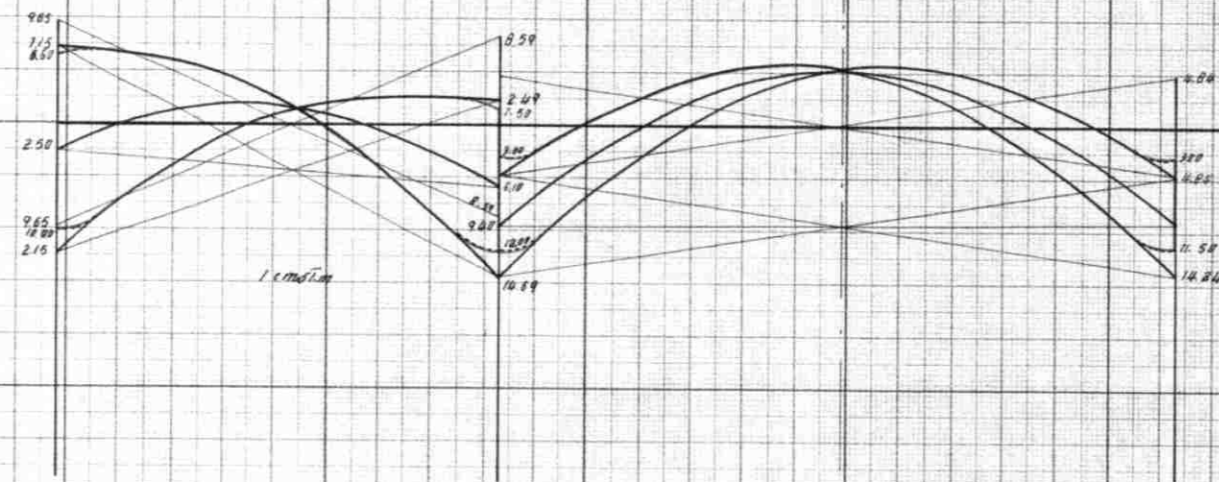
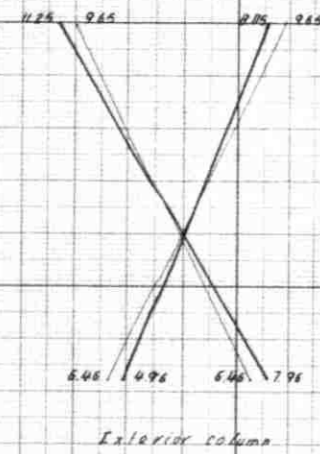
First midspan



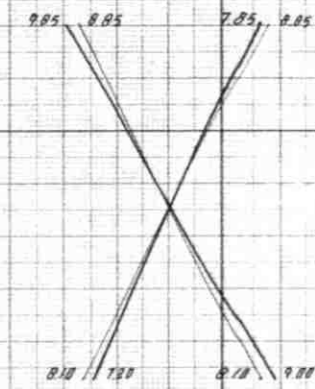
Interior support

Second midspan

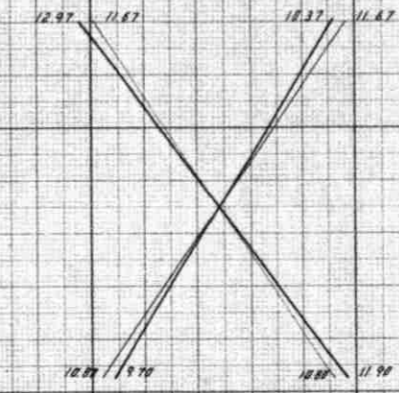
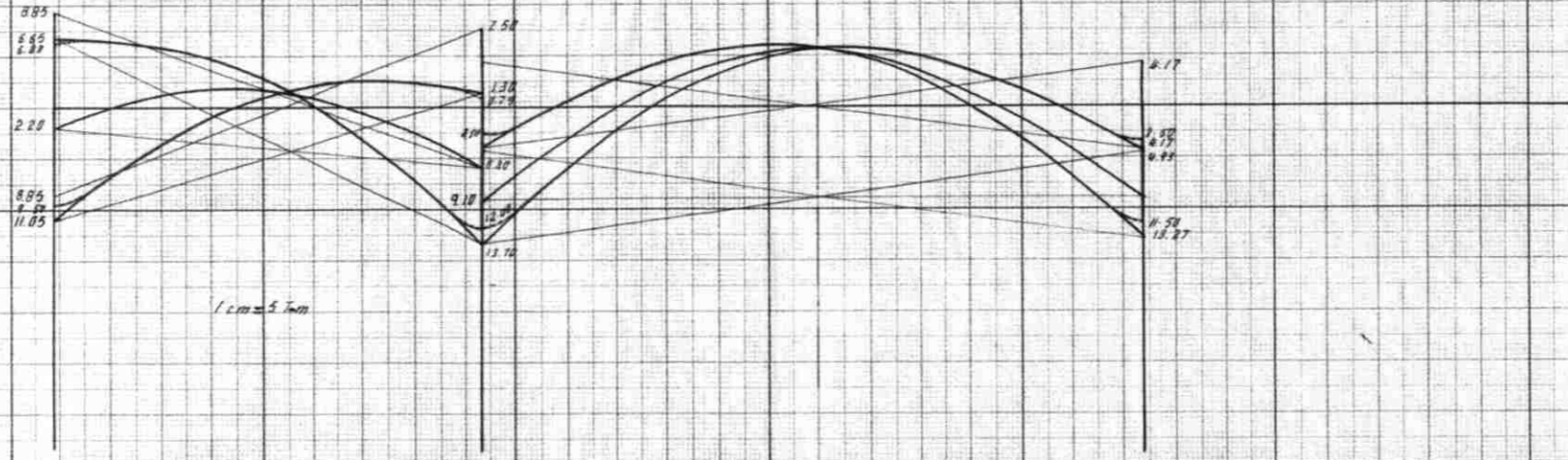
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| DRAWN BY : | RIAD SHAHIN | ENVELOPE DIAGRAMS | |
| CHK'D BY : | RIAD SHAHIN | REINFORCEMENT IN BEAMS | |
| APP'D BY : | DR. JACK NASSER | DATE : DECEMBER 1964 | SHEET NO 29 / |



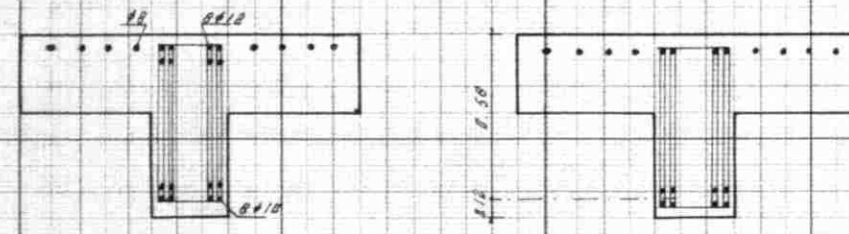
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| CHK'D BY : | RIAD SHAHIN | REINFORCEMENT IN BEAMS | |
| APP'D BY : | DR. JACK NASSER | DATE : DECEMBER 1964 | SHEET N° 100 / |



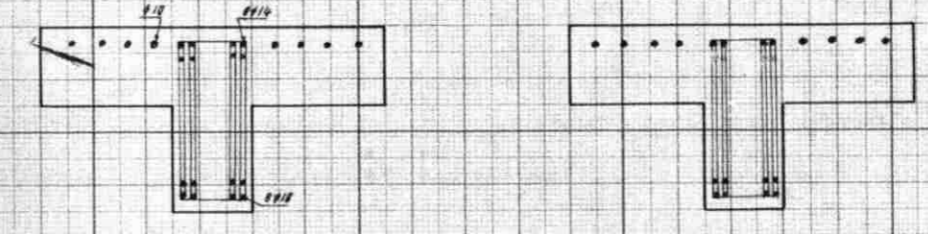
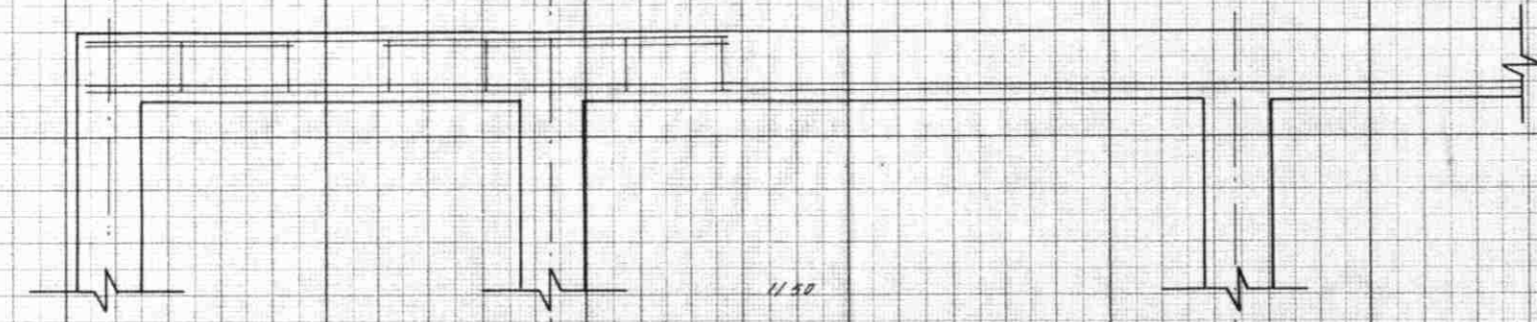
Exterior column



Interior column

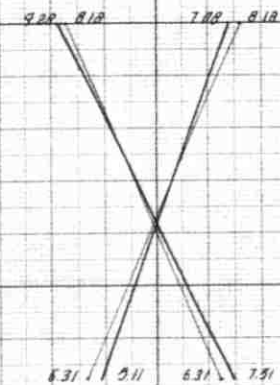


Exterior support First Midspan

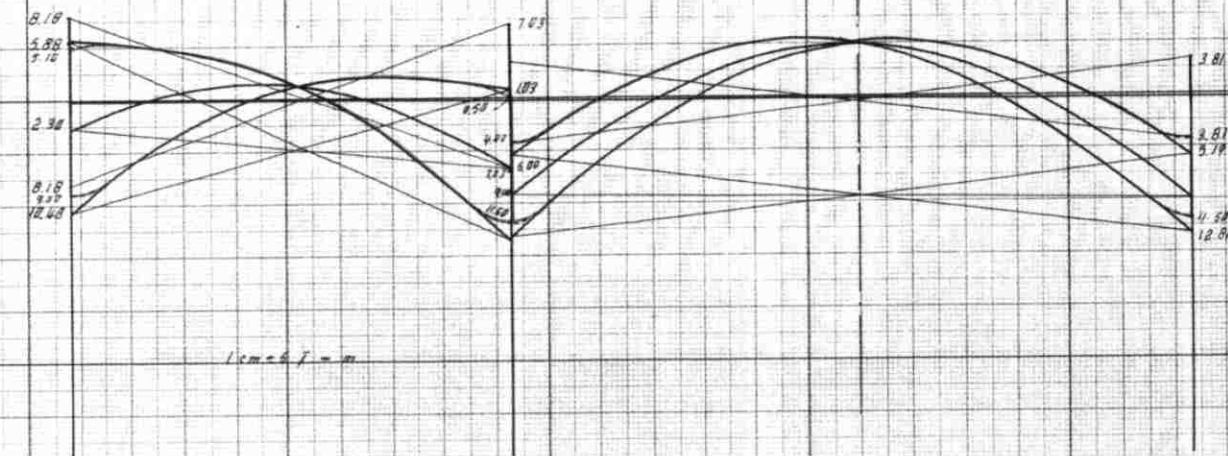


Interior support Second Midspan

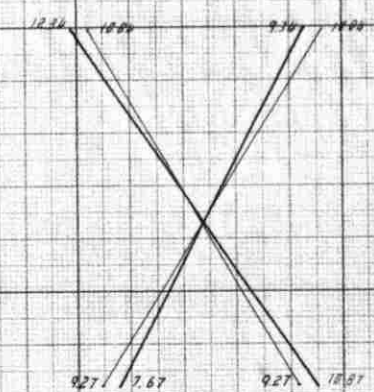
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| CHK'D BY : RIAD SHAHIN | REINFORCEMENT IN BEAMS | |
| APP'D BY : DR. JACK HASSER | DATE : DECEMBER 1964 | SHEET NO 101/ |



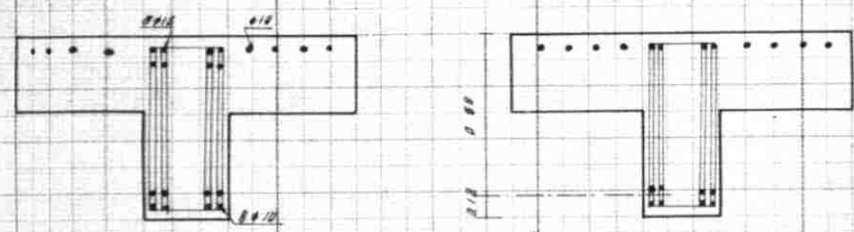
Exterior column



1 cm = 5 T = m



Interior column

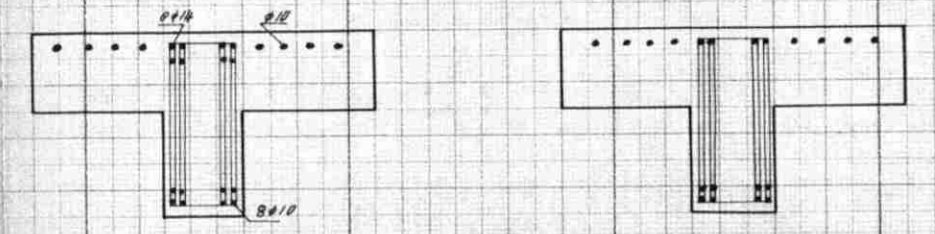


Exterior support

First midspan



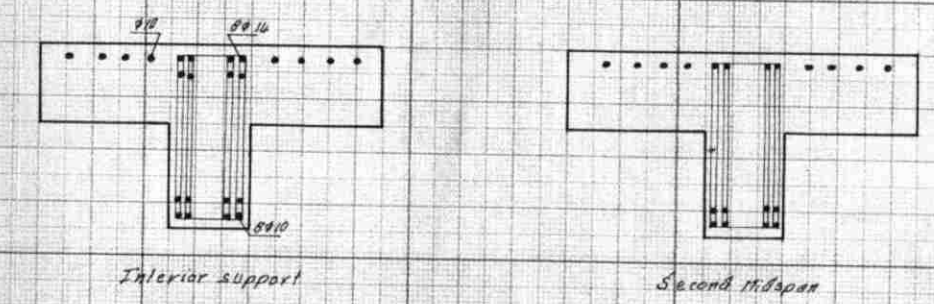
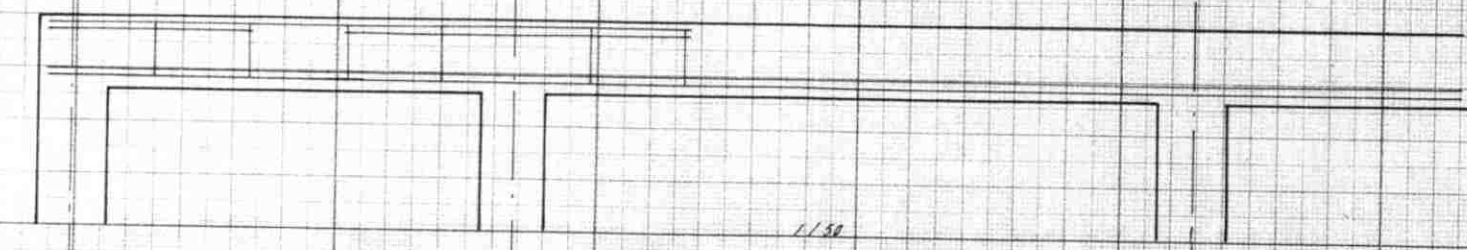
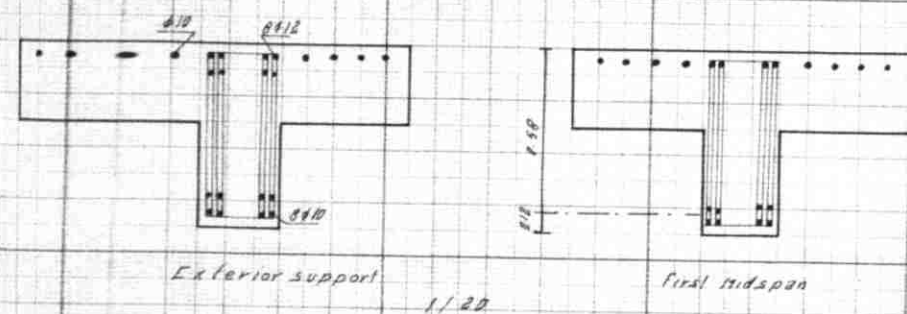
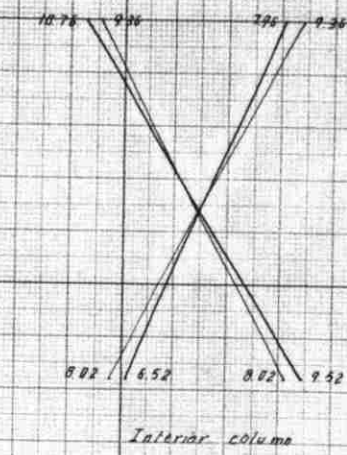
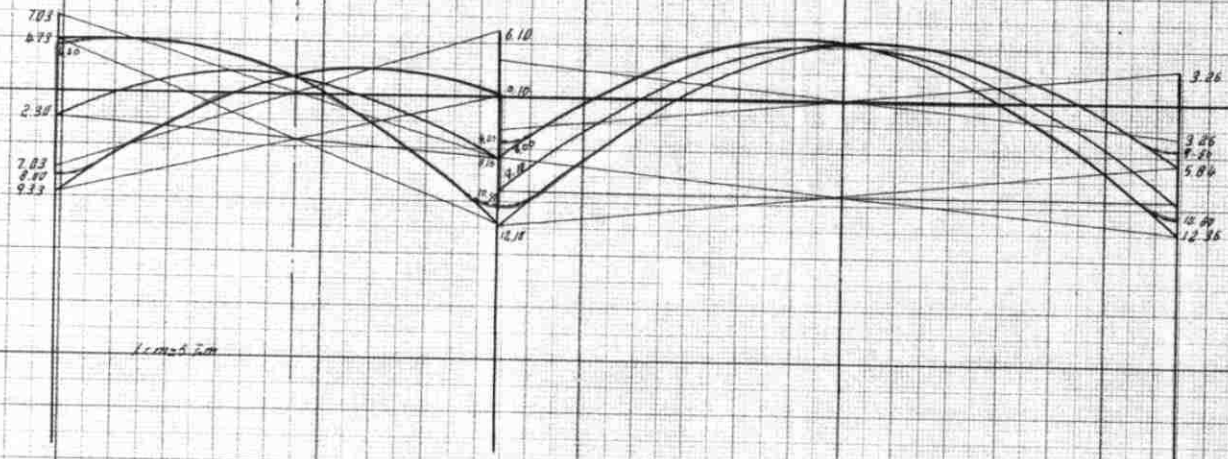
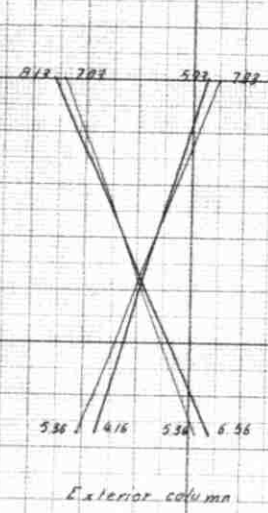
1/20



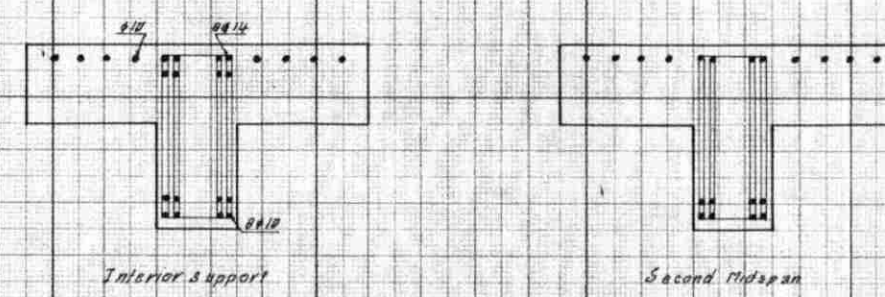
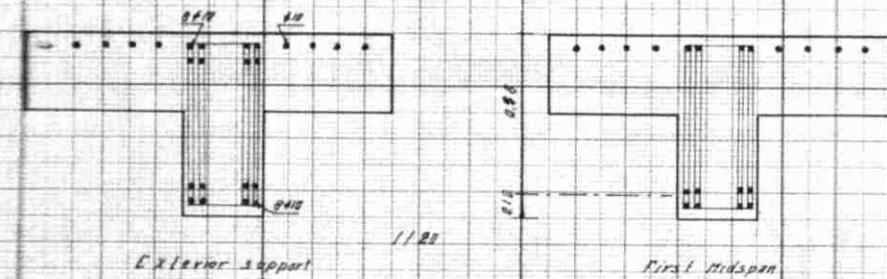
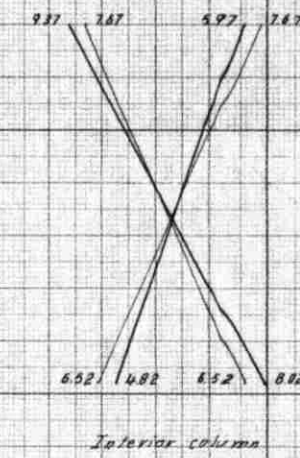
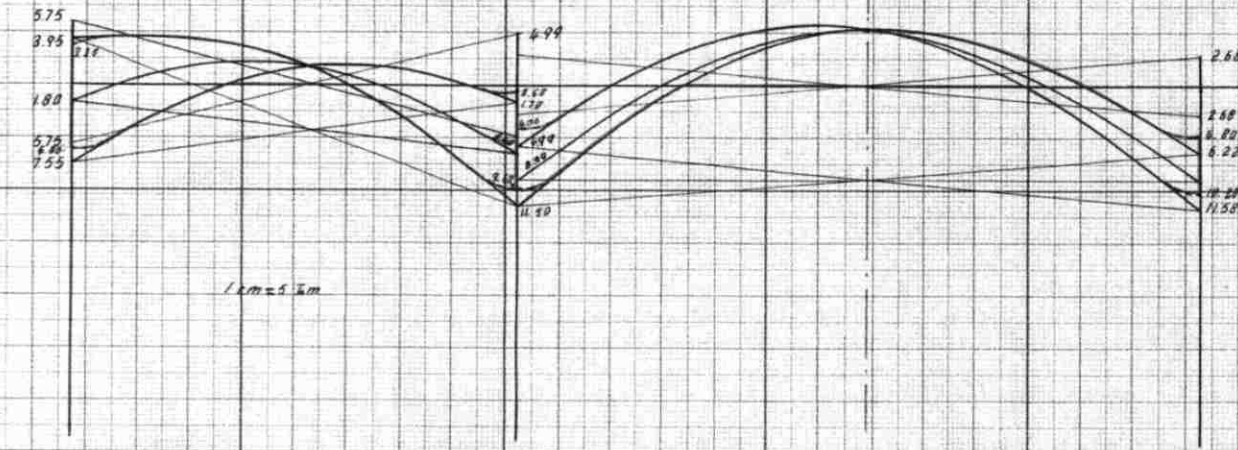
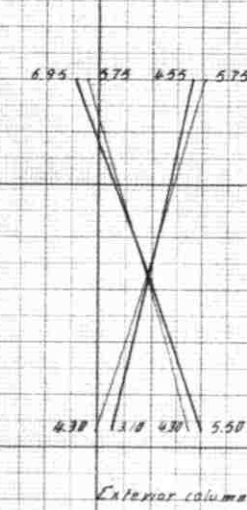
Interior support

Second midspan

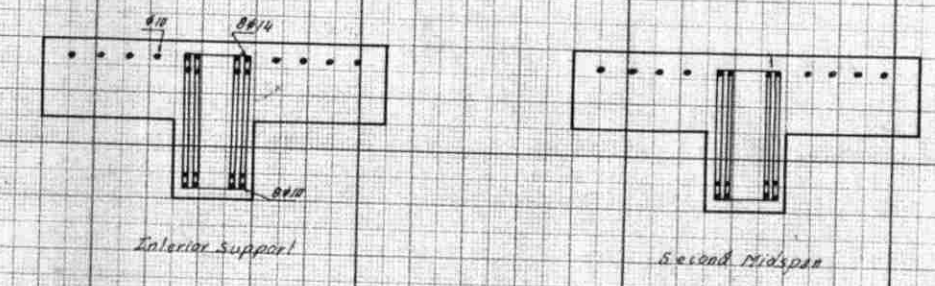
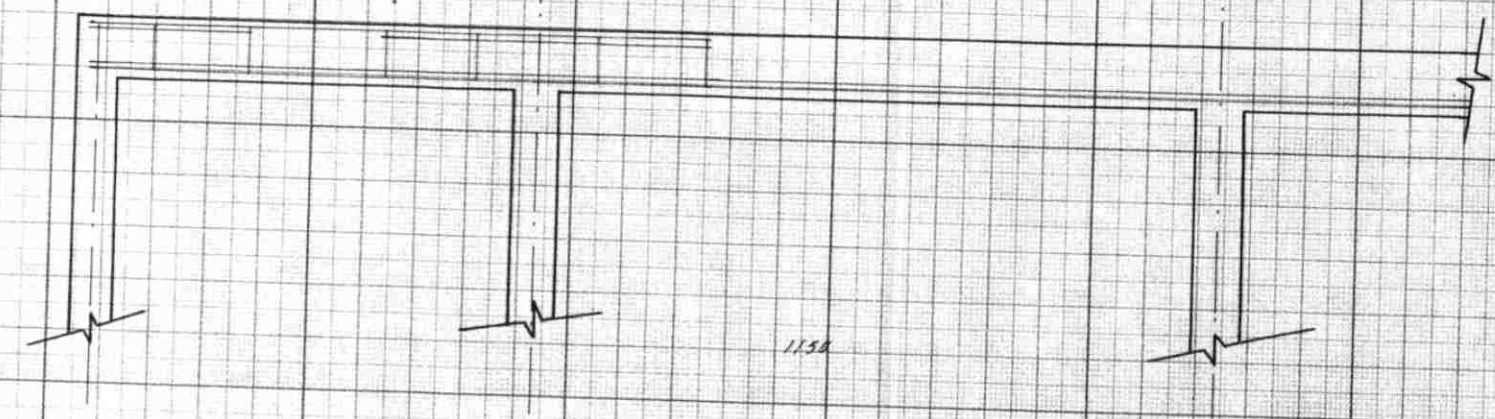
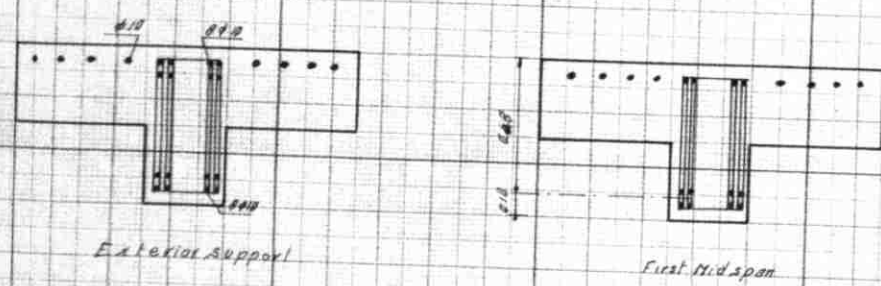
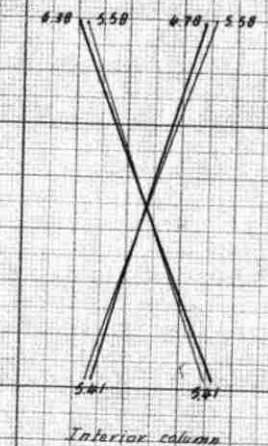
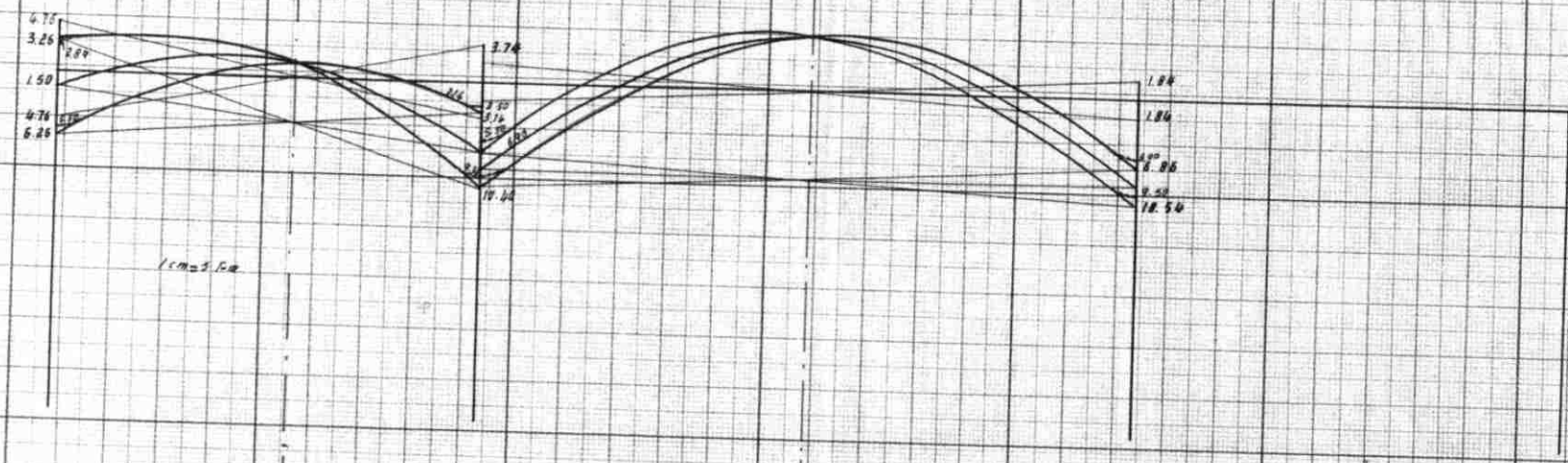
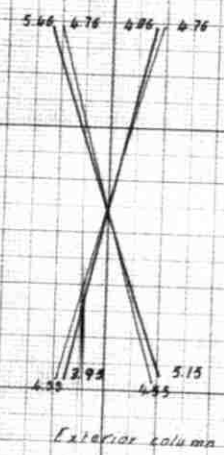
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| ANALYSIS OF THE EFFECT OF WIND ON A HIGH REINFORCED CONCRETE BUILDING | |
| Comparison of Approximate and Exact Methods | |
| DRAWN BY : RIAD SHAHIN | ENVELOPE DIAGRAMS |
| CHK'D BY : RIAD SHAHIN | REINFORCEMENT IN BEAMS |
| APP'D BY : DR. JACK HASSER | DATE : DECEMBER 1964 SHEET NO. 102/ |



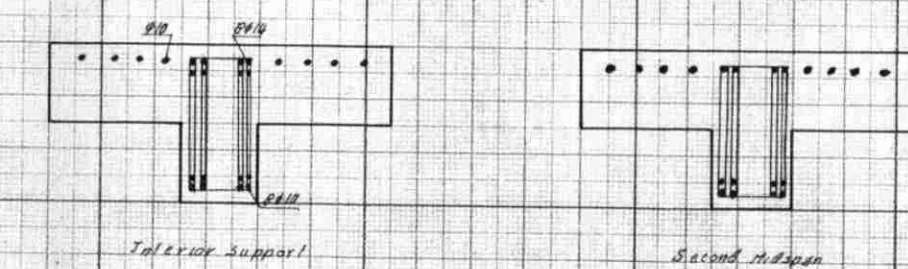
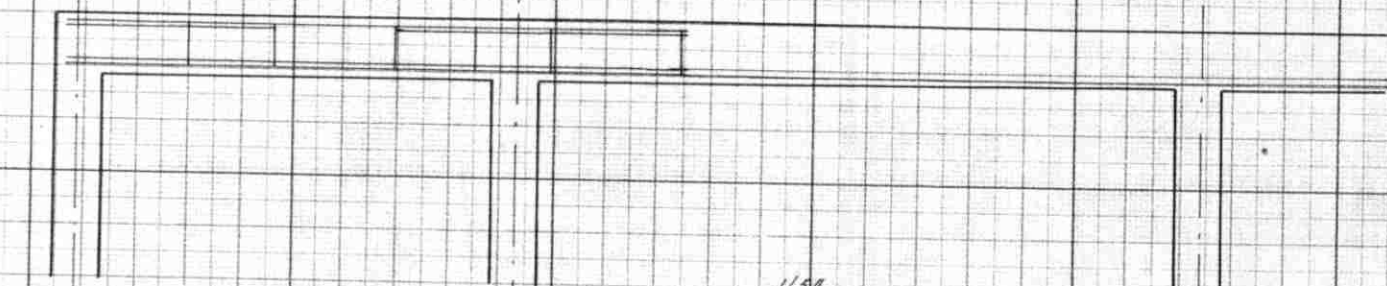
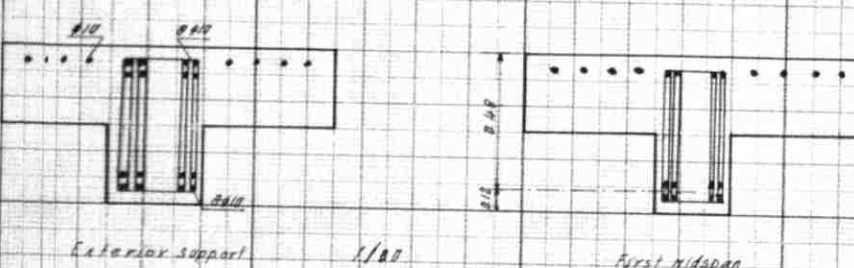
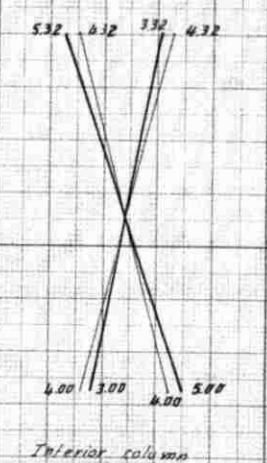
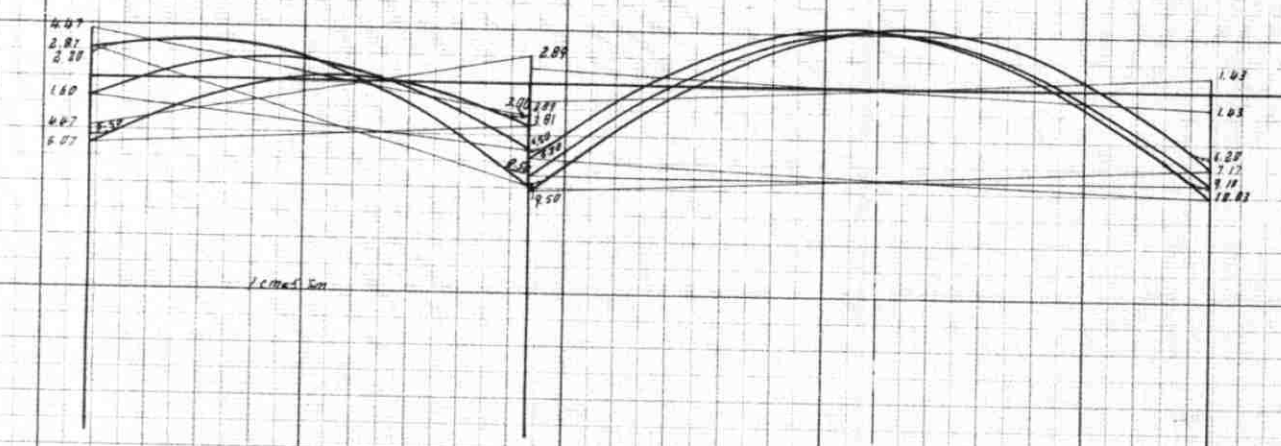
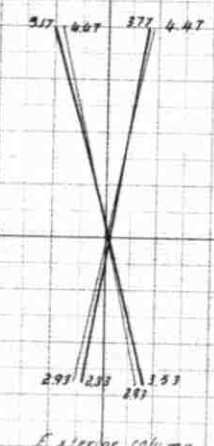
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| DRAWN BY : RIAD SHAHIN | | ENVELOPE DIAGRAMS | |
| CHK'D BY : RIAD SHAHIN | | REINFORCEMENT IN BEAMS | |
| APP'D BY : DR. JACK NASSER | | DATE : DECEMBER 1964 | SHEET NO 103 / |



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| CHK'D BY : RIAD SHAHIN | REINFORCEMENT IN BEAMS | |
| APP'D BY : DR. JACK NASSER | DATE : DECEMBER 1964 | SHEET N° 104 |



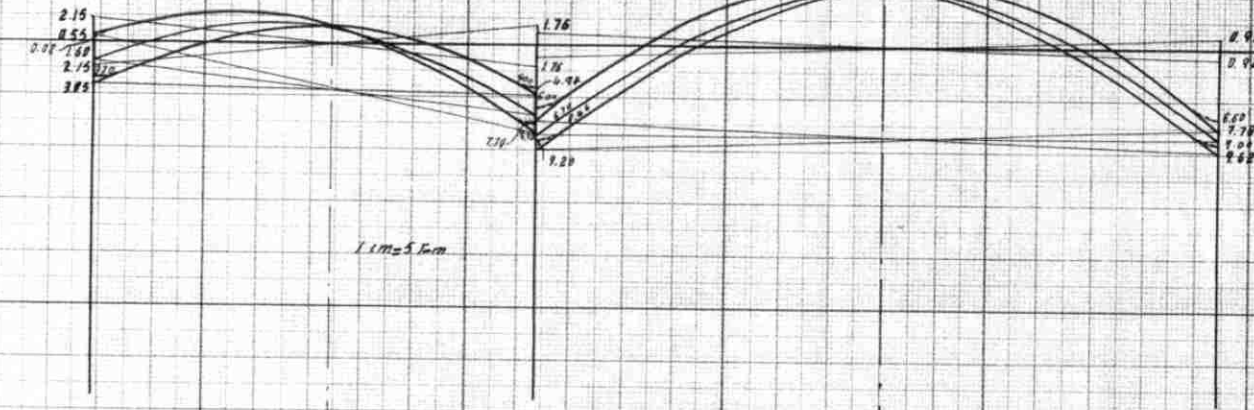
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| DRAWN BY: RIAD SHAHIN | ENVELOPE DIAGRAMS |
| CHK'D BY: RIAD SHAHIN | REINFORCEMENT IN BEAMS |
| APP'D BY: DR. JACK NASSER | DATE: DECEMBER 1964 SHEET NO 105 / |



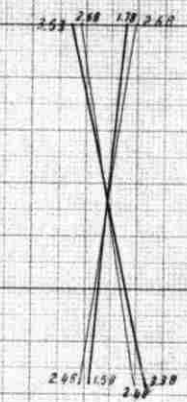
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| DRAWN BY : RIAD SHAHIN | ENVELOPE DIAGRAMS |
| CHECKED BY : RIAD SHAHIN | REINFORCEMENT IN BEAMS |
| APPROVED BY : DR. JACK NASSER | DATE : DECEMBER 1964 SHEET NO. 106/ |



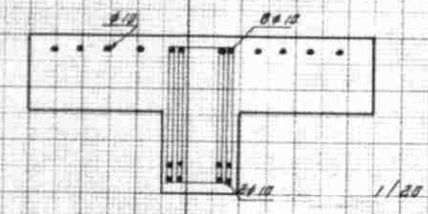
Exterior column



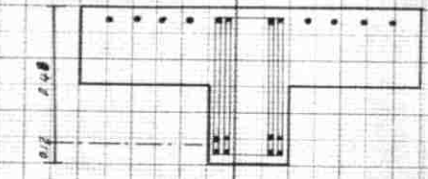
$1.1m = 5.6m$



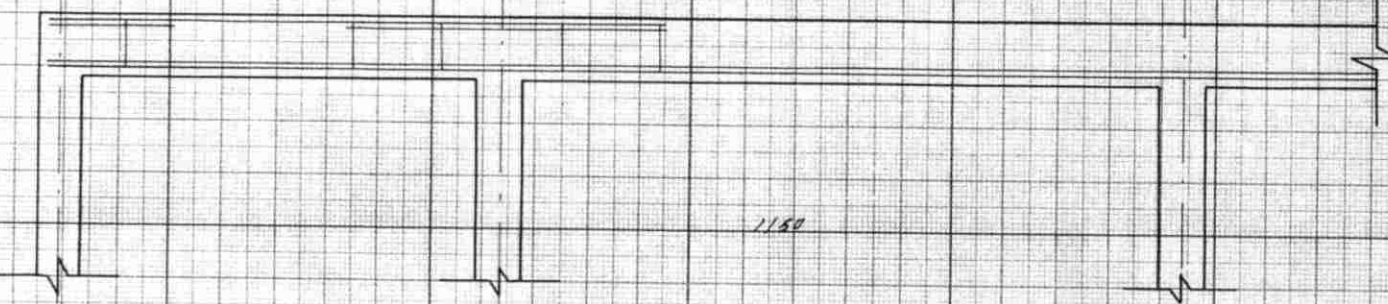
Interior column



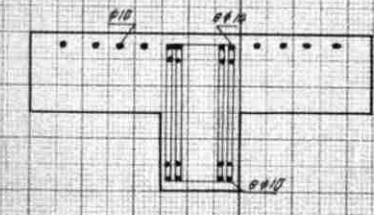
Exterior support



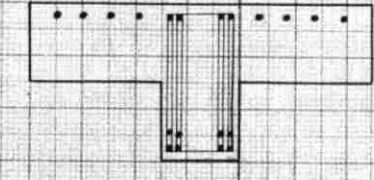
First midspan



1/20

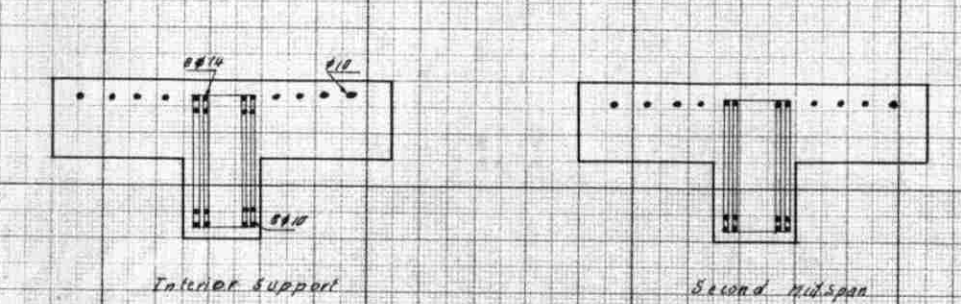
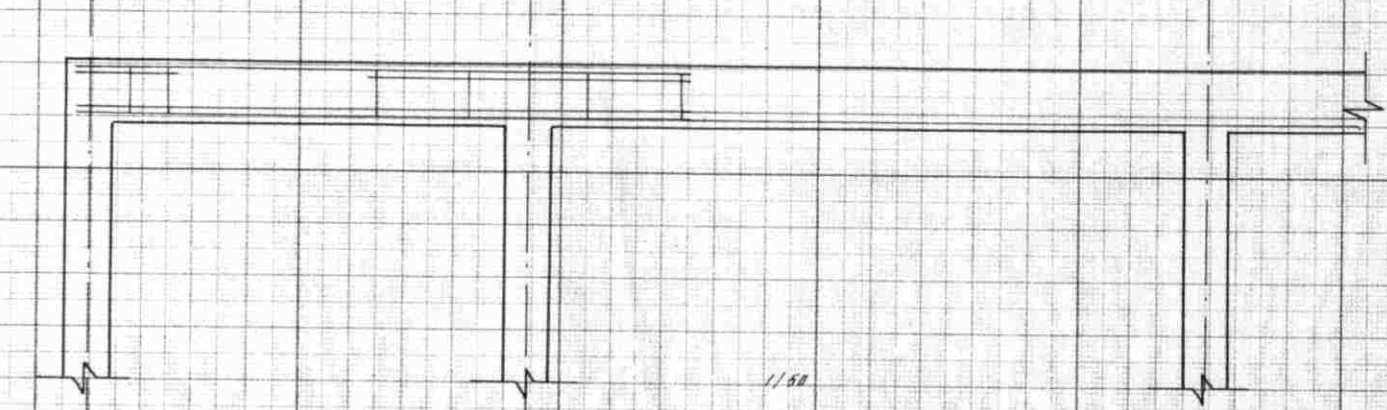
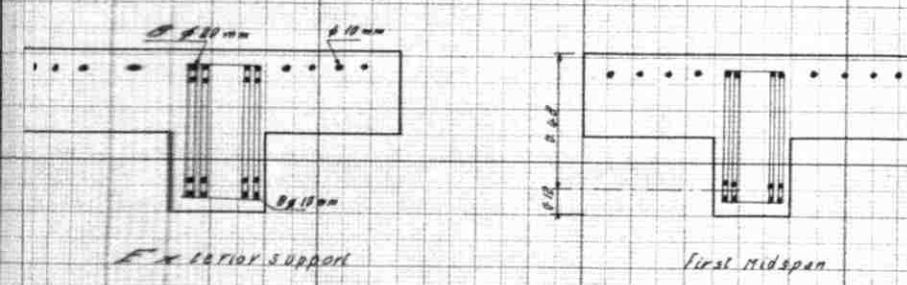
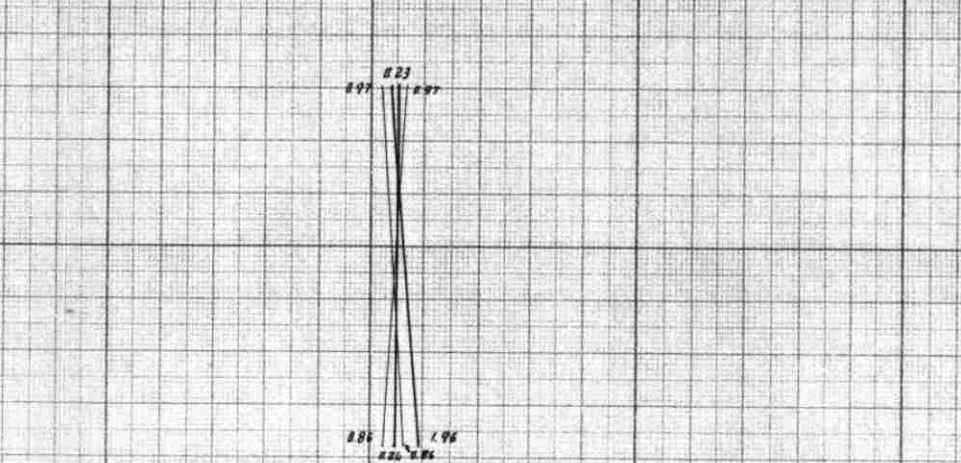
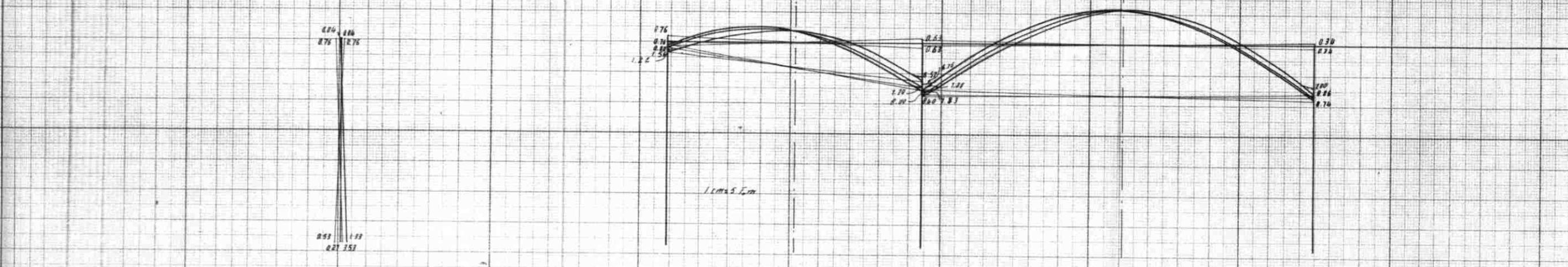


Interior support



Second midspan

| ANALYSIS OF THE EFFECT OF WIND ON A HIGH REINFORCED CONCRETE BUILDING | | | |
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| Comparison of Approximate and Exact Methods | | | |
| DRAWN BY | RIAD SHAHIN | ENVELOPE DIAGRAMS | |
| CHK'D BY | RIAD SHAHIN | REINFORCEMENT IN BEAMS | |
| APP'D BY | DR JACK HASSER | DATE: DECEMBER 1964 | SHEET N° 107 |



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| CHK'D BY : RIAD SHAHIN | REINFORCEMENT IN BEAMS |
| APP'D BY : DR. JACK HASSER | DATE: DECEMBER 1964 SHEET N° 108 / |

CHAPTER
REINFORCED CONCRETE DESIGN

General:

Although this chapter appears as a unity, the method adopted consists in designing the slabs and long direction beams of a typical floor before making the wind analysis. The design of the slabs at an earlier stage is considered necessary because it serves as a guide with respect to the depth of the beams.

This section has no intention of being detailed.

The design of the most critical frame members was conducted for Case "C" only, whereby the structure proved to stand.

Basis of Design:

1. Working stress theory is used.
2. A.C.I. Code (1959 edition) is used. This edition was violated in designing the columns whereby 6% of steel was required for one of the members. However, the 1963 edition allows up to 8%. Furthermore, when designing the footings, reference is made to "Foundation Engineering, Peck, Hanson and Thornburn". This implies one deviation from the A.C.I. Code in the magnitude of moment and shear for flexure and bond. The A.C.I. Code recommends the use of 85 per cent of the static moment and shear for the determination of the area of the steel and for the computation of the bond stress. This procedure cannot be

justified either by statics or by experiment. With the present growing practice of using bars that develop high bond stresses without hooks, it becomes increasingly important that the full static moment and shear be used for investigating stresses at the face of the column.

3. Metric units are used.

4. A good quality concrete with a crushing strength of $f'c = 3750 \text{ psi} = 263 \text{ Kg/cm}^2$.

5. Working stresses of concrete due to bending flexure will be $fc = 0.45 \times 263 = 118 \text{ Kg/cm}^2$.

6. Working stress of concrete due to compression will be $fc = 0.25 \times 263 = 66 \text{ Kg/cm}^2$.

7. Working stress of steel under tension is taken as:

a. Mild steel, $fs = 20,000 \text{ psi} = 1400 \text{ Kg/cm}^2$,

b. High strength steel, $fs = 30,000 \text{ psi} = 2100 \text{ Kg/cm}^2$.

8. Ratio of equivalence is $n = 8$.

9. Due to such working stresses, the resisting moment of a rectangular section under bending will be

a. Mild Steel

$$Mc = \frac{1}{2} fc.k.j.bd^2$$

$$= \frac{1}{2} \times 1180 \times 0.405 \times 0.865 bd^2 = 207 bd^2 \text{ (T-m)}$$

if b and d are in meters and $f'c$ is in T/m^2

b. High Strength Steel

$$Mc = \frac{1}{2} \times 1180 \times 0.312 \times 0.896 bd^2$$

$$= 165 bd^2 \text{ (T-m)}$$

if b and d are in meters and $f'c$ is in T/m^2 .

10. Reinforcement equations will be

a. Mild Steel

$$\begin{aligned} \Delta s_1 &= \frac{M_1}{f_s j d} = \frac{M_1}{14,000 \times 0.865 d} \text{ m}^2 \\ &= \frac{10^4 M_1}{14,000 \times 0.865 d} \text{ cm}^2 = 0.825 \frac{M_1}{d} \text{ cm}^2 \\ &\text{if } M_1 \text{ is in T-m and } d \text{ in meters} \end{aligned}$$

$$\begin{aligned} \Delta s_2 &= \frac{M_2}{f_s (d - d')} = \frac{M_2}{1.40 (d - d')} \text{ cm}^2 \\ &\text{if } M_2 \text{ is in T-m} \\ &\text{and } d \text{ in meters} \end{aligned}$$

$$\Delta s = \Delta s_1 + \Delta s_2$$

$$\begin{aligned} \Delta s &= \frac{\Delta s_2}{2} \left(\frac{1 - k}{k - \frac{d'}{d}} \right) = \frac{\Delta s_2}{2} \left(\frac{1 - 0.405}{0.405 - \frac{d'}{d}} \right) \\ &= \frac{\Delta s_2}{2} \left(\frac{0.595}{0.405 - \frac{d'}{d}} \right) \text{ cm}^2 \end{aligned}$$

b. High Strength Steel

$$\begin{aligned} \Delta s_1 &= \frac{M_1}{2.10 \times 0.896 d} = 0.535 \frac{M_1}{d} \text{ cm}^2 \\ &\text{if } M_1 \text{ is in T-m and } d \text{ in meters} \end{aligned}$$

$$\begin{aligned} \Delta s_2 &= \frac{M_2}{2.10 (d - d')} = 0.476 \frac{M_2}{(d - d')} \text{ cm}^2 \\ &\text{if } M_2 \text{ is in T-m and } d \text{ in meters} \end{aligned}$$

$$\Delta s = \frac{\Delta s_2}{2} \cdot \frac{(1 - 0.312)}{(0.312 - \frac{d'}{d})} = \frac{\Delta s_2}{2} \times \frac{0.688}{(0.312 - \frac{d'}{d})} \text{ cm}^2$$

if M_1 is T-m and d in meters.

11. Bond Coefficients

a. Mild and High Strength Steel

$$\sum o = \frac{V}{ujd} = \frac{V \times 100}{(0.10 \times 2630) \times 7/8 d}$$

$$= 0.435 \frac{V}{d} \text{ cms}$$

if V is in T and d in meters

12. Examples

This item aims in calculating the coefficients for the slabs and beams.

a. Slabs

$$d = 27 \text{ cm} = 0.27 \text{ m.}$$

using mild steel

$$As_1 = 0.825 \frac{M_1}{0.27} = 3.05 M_1 \text{ cm}^2$$

$$As_2 = \frac{M_2}{1.40 (0.27 - 0.03)} = 2.97 M_2 \text{ cm}^2$$

$$As' = \frac{As_2}{2} \left(\frac{0.595}{0.405 - \frac{0.03}{0.27}} \right) = 1.01 As_2 \text{ cm}^2$$

$$\sum o = 0.435 \frac{V}{0.27} = 1.61 V \text{ cms.}$$

b. Frame Beams

Using high strength steel

The various coefficients are calculated below for the five cases available with $d' = 8$ cms in the case of one row and $d' = 12$ cms in the case of two rows of reinforcement.

| Floor | $\Delta s_1 = CM$ | | | | $\Delta s_2 = CM$ | |
|-------|-------------------|-------|----------|-------|-------------------|-------|
| | One Row | | Two Rows | | One Row | |
| | d(m) | C | d(m) | C | (d-d')(M) | C |
| 20-17 | 0.52 | 1.03 | 0.48 | 1.11 | 0.44 | 1.08 |
| 16-13 | 0.62 | 0.862 | 0.58 | 0.925 | 0.54 | 0.88 |
| 12-9 | 0.72 | 0.742 | 0.68 | 0.790 | 0.64 | 0.744 |
| 8-5 | 0.82 | 0.652 | 0.78 | 0.688 | 0.74 | 0.644 |
| 4-1 | 0.92 | 0.582 | 0.88 | 0.610 | 0.84 | 0.566 |

The values of the resisting moments at supports will be

| Floor | Negative Moment | | | | | Positive Moment | | | | |
|-------|-----------------|-------|----------------------------------|-------------------------|----------|-----------------|-------|----------------------------------|------------------------|----------|
| | b' (m) | d (m) | d ² (m ²) | Kb' (T/m ²) | MR (T-m) | b' (m) | d (m) | d ² (m ²) | Kb (T/m ²) | MR (T-m) |
| 20-17 | 0.30 | 0.48 | 0.232 | 49.50 | 13.50 | 1.30 | 0.48 | 0.232 | 214 | 49.50 |
| 16-13 | " | 0.58 | 0.340 | " | 19.20 | " | 0.58 | 0.340 | " | 72.50 |
| 12-9 | " | 0.68 | 0.465 | " | 25.80 | " | 0.68 | 0.465 | " | 99.20 |
| 8-5 | " | 0.78 | 0.610 | " | 33.60 | " | 0.78 | 0.610 | " | 130.00 |
| 4-1 | " | 0.88 | 0.780 | " | 42.00 | " | 0.88 | 0.780 | " | 167.00 |

PART A

DESIGN OF A TYPICAL FLOOR

General:

Although it is the regular practice (i.e. more economical) to design slabs with the ribs parallel to the short direction if the slab is one way, and to have slabs as two ways when square, in the present case all slabs will be designed as one way and with ribs parallel to the long direction in order to load the short direction beams with the vertical load, and hence to relieve the long direction beams to take care of the wind loading which is supposed to have a high intensity.

The approximate coefficients provided by the A.C.I. Code cannot be used for two reasons:

1. The longer span is exceeding the shorter spans by more than 20%.
2. The presence of the two cantilevers.

However, two methods of analysis are considered satisfactory, namely:

1. Three Moments Equations.
2. Moment Distribution.

The three moment equations will be used, assuming simple supports.

Moments and Shears:

In order to eliminate some calculations, a general equation is derived with a uniform load w .

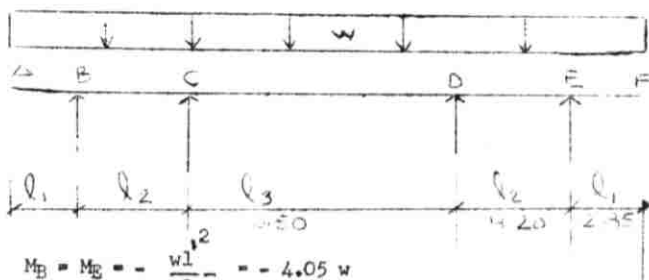


Fig 1

$$M_B = M_E = - \frac{w l_1^2}{2} = - 4.05 w$$

$$M_C = M_D$$

$$M_B \cdot l_2 + 2M_C (l_2 + l_3) + M_C \cdot l_3 = - \frac{w}{4} (l_2^3 + l_3^3)$$

$$(-4.05 w) 4.20 + 2M_C(10.70) + 6.50 M_C = - \frac{w}{4} (74 + 274)$$

$$- 17w + 21.40 M_C + 6.50 M_C = \frac{w}{4} \times 348 = 87 w$$

$$- 17w + 27.90 M_C = 87 w$$

$$27.90 M_C = 104 w$$

$$M_C = \frac{104}{27.90} w = 3.73 w$$

$$M_C = 4.20 R_B - w \times \frac{7.05^2}{2} = - 2.50 w$$

$$4.20 R_B - 25 w = - 2.50 w$$

$$4.20 R_B = 22.50 w$$

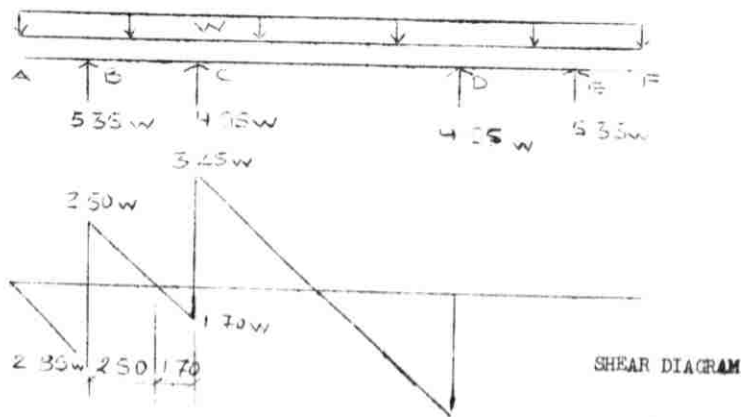
$$R_B = \frac{22.50}{4.20} w = 5.35 w$$

$$M_D = 10.70 (5.35 w) + 6.50 R_C - w \times \frac{13.55^2}{2} = - 2.50 w$$

$$57.20 w + 6.50 R_C - 92 w = - 2.50 w$$

$$6.50 R_C = (-2.50 + 92 - 57.20)w$$

$$R_C = \frac{32.30 w}{6.50} = 4.95 w$$



SHEAR DIAGRAM

MOMENT DIAGRAM

Fig 2

Loading:

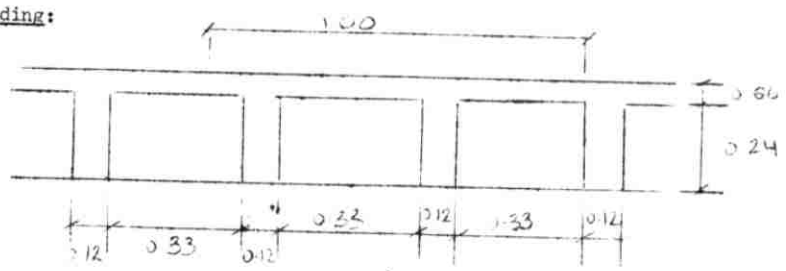


Fig 3.

| | |
|------------------------|------------------------------------|
| Live Load | 250 Kg/m ² |
| D.L. of 6 cms. Slab | 150 Kg/m ² |
| Tiles and mortar 3 cms | |
| 0.03 x 2400 | 72 Kg/m ² |
| Sand 4 cms | |
| 0.04 x 1800 | 72 Kg/m ² |
| 2 cms Plaster | 48 Kg/m ² |
| Blocks (12 x 13) | 156 Kg/m ² |
| Joists | |
| (0.12x0.24x2500)2 | 144 Kg/m ² |
| Partitions: | 100 Kg/m ² |
| | <hr/> |
| | 992 Kg/m ² |
| | Say 1 ^T /m ² |

$$\text{Load / Rib} = 0.50 \text{ T/m}^2$$

From the shear diagram

$$V_{\max} = 3.25 w = 3.25 \times 500 = 1625 \text{ Kg.}$$

$$b'(r_{qd}) = \frac{1625}{8 \times 7/8 \times 27} = \frac{1625}{168} = 9.70 \text{ cms.}$$

. . . O.K.

$$M_C (\text{Support}) = 207 \times 0.12 \times 0.27^2 = 1.43 \text{ T-m}$$

$$M_C (\text{Center}) = 207 \times 0.45 \times 0.27^2 = 5.35 \text{ T-m}$$

Reinforcement:

1. First Mid-Span

$$M_1 = 0.92 \times 0.50 = 0.46 \text{ T-m}$$

$$M_C > M_1 \text{ i.e. } 5.35 > 0.46$$

$$A_s = 3.05 \times 0.46 = 1.40 \text{ cm}^2$$

Use $2\phi 10$ mm.

$$A_s (\text{fur.}) = 1.56 \text{ cm}^2$$

2. Second Mid-Span

$$M_1 = 2.93 \times 0.50 = 1.47 \text{ T-m}$$

$$M_C > M_1$$

$$A_s = 3.05 \times 1.47 = 4.50 \text{ cm}^2$$

Use $2\phi 18$ mm.

$$A_s (\text{fur.}) = 5.00 \text{ cm}^2$$

3. Interior Supports

$$M_1 = 2.37 \times 0.50 = 1.19 \text{ T-m}$$

$$M_C > M_1 \text{ i.e. } 1.43 > 1.19$$

$$A_s = 3.05 \times 1.19 = 3.62 \text{ cm}^2$$

Use $1\phi 22$ mm.

$$A_s (\text{fur.}) = 3.83 \text{ cm}^2$$

$$\Sigma o = 1.61 \times 1.625 = 2.62 \text{ cms.}$$

. . . O.K.

4. Exterior Supports

$$M = 4.05 w = 4.05 \times 0.50 = 2.03 \text{ T-m}$$

$$M_c = 1.43 \text{ T-m}$$

$$A_{s1} = 3.05 M_c = 3.05 \times 1.43 = 4.35 \text{ cm}^2$$

$$A_{s2} = 2.97 (2.03 - 1.43)$$

$$= 2.97 \times 0.60 = 1.80$$

$$A's = 1.01 \times 1.80 = 1.82 \quad A_{s2}$$

$$A_s = 4.35 + 1.80 = 6.15 \text{ cm}^2$$

Use 1 ϕ 30 mm.

$$A_s (\text{fur.}) = 7.00 \text{ cm}^2$$

$$\Sigma o = 1.61 (2.85 \times 0.50) = 2.30 \text{ cms.}$$

. . O.K.

PART B

B E A M S

BEAM B₁

1. Loads:

$$\text{Load from slab : } \frac{wl}{2}$$

$$1000 \times \frac{4.20}{2} = 2100 \text{ Kg/M.R.}$$

Load from balcony: wl

$$1000 \times 2.85 = 2850 \text{ Kg/M.R.}$$

$$4950 \text{ Kg/M.R.}$$

$$4.95 \text{ T/M.R.}$$

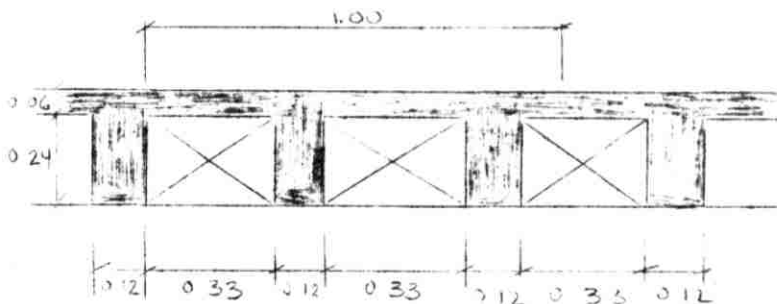


Fig. 1.

Find the equivalent thickness of the slab:

$$t' = \frac{1 \times 0.06 + 2 (0.24 \times 0.12)}{1} = 0.1176 \text{ m} \approx 12 \text{ cms.}$$

2. Section:

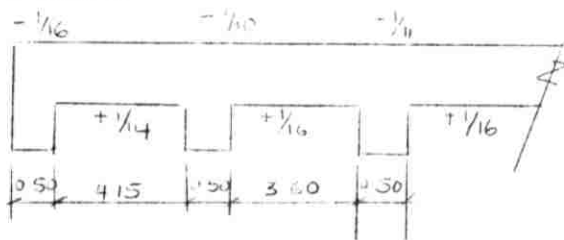


Fig 2

The effective overhang width of an L beam will be the smallest of the following:

- $1/12$ of the beam span = $1/12 \times 4.65 \times 100 = 39$ cms.
 - 6 times slab thickness = $6 \times 12 = 72$ cms.
 - $\frac{1}{2}$ clear distance to next beam
 $\frac{1}{2} (4.20 - 0.50) = 185$ cms.
- $\therefore b'' = 39$ cms Say 40 cms.

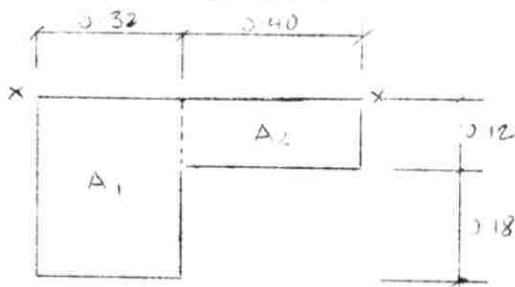


Fig 2

Let the width of the beam be 32 cms.

$$\begin{aligned} \therefore \text{D.L.} &= (0.32 \times 0.30 + 0.40 \times 0.12) 2500 \\ &= (0.096 + 0.048) 2500 = 360 \text{ Kg/m} \end{aligned}$$

$$\therefore w_T = 4950 + 360 = 5310 \text{ Kg/m}$$

$$\begin{aligned} V_{\max} &= 1.15 \frac{w l^1}{2} = 1.15 \times \frac{w}{2} \left(\frac{4.15 + 3.60}{2} \right) \\ &= 1.15 \times \frac{w}{2} \times 3.88 \\ &= 1.15 \times w \times 1.94 = 223w = 11900 \text{ Kg} \end{aligned}$$

$$b'd = \frac{11,900}{7/8 \times 16} = \frac{11,900}{14} = 850$$

$$d = 27 \text{ cm} \quad \therefore b' = \frac{850}{27} = 31.50 \text{ cms.}$$

\therefore O.K.

Find the neutral axis by summing moments at x-x

$$\sum M_{xx} = 0$$

$$A_1 \bar{y}_1 + A_2 \bar{y}_2$$

$$(32 \times 30 + 40 \times 12) \bar{y} = (32 \times 30 \times 15) + (40 \times 12 \times 6)$$

$$(960 + 480) \bar{y} = 14,400 + 2880$$

$$1440 \bar{y} = 17,280$$

$$\bar{y} = \frac{17,280}{1440} = 12 \text{ cms}$$

$$\text{i.e. } k_d = 12 \text{ cms.}$$

Hence the beam could act as a rectangular or T-Beam. For simplicity use the rectangular beam equations.

$$M_C (\text{Center}) = 207 \times 0.72 \times \overline{0.27}^2 = 12.40 \text{ T-m}$$

$$M_C (\text{Support}) = 207 \times 0.32 \times \overline{0.27}^2 = 5.95 \text{ T-m}$$

3. Reinforcement:

a. First Mid-Span

$$M = 1/14 \times w \times \overline{4.15}^2 = 1.23 w = 1.23 \times 5.31 = 6.92 \text{ T-m}$$

$$\therefore M < M_R \quad \text{i.e. } 7.90 < 13.40$$

$$A_s = 3.05 M_1 = 3.05 \times 6.92 = 20 \text{ cm}^2$$

Use $4\phi 28$ mm

$$A_s (\text{fur.}) = 24.40 \text{ cm}^2$$

Bend up two bars

b. Other Mid-Spans

$$M = 1/16 \times w \times \overline{3.60}^2 = 0.81 w = 0.81 \times 5.31 = 4.30 \text{ T-m}$$

$$M_R > M \quad \text{i.e. } 13.40 > 4.30$$

$$A_s = 3.05 \times 4.30 = 13.10 \text{ cm}^2$$

Use $4\phi 20$ mm

$$A_s (\text{fur.}) = 12.56 \text{ cm}^2$$

Bend up two bars

c. First Interior Support

$$M = 1/10 w l^2$$

$$= 1/10 \times w \times \overline{3.88}^2 = 1.50 w = 1.50 \times 5.31 = 7.96 \text{ T-m}$$

$$M > M_C \quad \text{i.e. } 7.96 > 5.95$$

$$A_{s1} = 3.05 \times 5.95 = 18.20 \text{ cm}^2$$

$$A_{s2} = 2.97 (7.96 - 5.95)$$

$$= 2.97 \times 2.01 = 5.94 \text{ cm}^2$$

$$A_s = 18.20 + 5.94 = 24.14 \text{ cm}^2$$

$$A'_s = 1.01 A_{s2} = 6 \text{ cm}^2$$

$$A_s (\text{fur.}) = 12.20 + 6.55 = 18.75 \text{ cm}^2$$

Add $2\phi 20$ mm

$$\Sigma o = 1.61 \times 11.90 = 19.10 \text{ cms}$$

$$\Sigma o (\text{fur.}) = 25.52 + 17.60 = 43.12 \text{ cms.}$$

d. Other Interior Support

$$M = 1/11 w l^2 = 1/11 \times w \times \frac{3.60^2}{2} = 1.18 w$$

$$= 1.18 \times 5.31 = 6.25 \text{ T-m}$$

$$M > M_c \quad \text{i.e.} \quad 6.25 > 5.95 \text{ T-m}$$

$$A_{s1} = 3.05 \times 5.95 = 18.20 \text{ cm}^2$$

$$A_{s2} = 2.97 (6.25 - 5.95) = 0.89 \text{ cm}^2$$

$$A_s = 18.20 + 0.89 = 19.09 \text{ cm}^2$$

$$A'_s = 1.01 \times 0.89 = 0.90 \text{ cm}^2$$

$$A_s (\text{fur.}) = 12.56 \text{ cm}^2$$

Add $2\phi 22$ mm

$$V = \frac{w l'}{2} = 5.310 \times \frac{3.60}{2} = 9.55 \text{ T}$$

$$\Sigma o = 1.61 \times 9.55 = 15.40 \text{ cms}$$

$$\Sigma o (\text{fur.}) = 38.92 \text{ cms}$$

e. Exterior Support

$$M = 1/16 \times w \times \frac{4.15^2}{2} = 1.03 w$$

$$= 1.03 \times 5.31 = 5.50 \text{ T-m}$$

$$M < M_c \quad \text{i.e. } 5.50 < 5.95$$

$$A_s = 5.95 \times 3.05 = 16.80 \text{ cm}^2$$

$$A_s (\text{fur.}) = 12.20 \text{ cm}^2$$

Add 2 ϕ 18 mm

$\Sigma \phi$ (fur.) is ample

BEAM B₂

1. Loads:

$$\text{Load from Slab: } 1000 \left(\frac{4.20}{2} + \frac{6.50}{2} \right) = 5360 \text{ Kg/M.R.}$$

The width of the T-Beam will be the smallest of the following:

a) 1/4 of Beam Span = $1/4 \times 4.65 \times 100 = 114 \text{ cms.}$

b) 16 times slab thickness + b'

i.e. $16 \times 10 + 60 = 220 \text{ cms.}$

c) Beam Spacing = $\frac{4.20 + 6.50}{2} = 535 \text{ cms.}$

\therefore 114 cms. governs

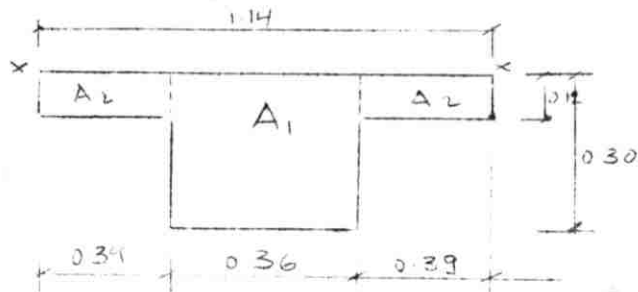


Fig 3

$$D.L. = (0.36 \times 0.30 + 0.39 \times 0.12 \times 2) 2500$$

$$= (0.108 + 0.094) \times 2500 = 0.202 \times 2500 = 505 \text{ Kg/M}$$

$$W_T = 5350 + 505 = 5855 \text{ Kg/ m}^2$$

$$V_{\max} = 5855 \times 2.23 = 13100 \text{ Kg.}$$

$$b'd = \frac{13,100}{7/8 \times 16} = 935 \text{ cm}^2$$

$$d = 27 \text{ cms.} \quad b' = \frac{935}{27} = 35 \text{ cms.}$$

. . . O.K.

Find the neutral axis by summing moment at x-x.

$$(36 \times 30 + 39 \times 12 \times 2) k_d = 1080 \times 15 + 940 \times 6$$

$$(1080 + 940) k_d = 16,200 + 5640$$

$$2020 k_d = 21,840$$

$$k_d = \frac{21,840}{2020} = 1090 \text{ cms.}$$

. . . It acts as a rectangular beam

$$M_C (\text{Center}) = 207 \times 1.14 \times 0.27^2 = 21.20 \text{ T-m}$$

$$M_S (\text{Support}) = 207 \times 0.36 \times 0.27^2 = 6.70 \text{ T-m}$$

2. Reinforcement:

a. First Mid-Span

$$M = 1.23 w = 1.23 \times 5.855 = 7.20 \text{ T-m}$$

$$M < M_C \quad \text{i.e.} \quad 7.20 < 21.20$$

$$A_s = 3.05 \times 720 = 22 \text{ cm}^2$$

$$\text{Use } 4\phi 28 \text{ mm} \quad A_s (\text{fur.}) = 24.40 \text{ cm}^2$$

Bend up two bars.

$$D.L. = (0.36 \times 0.30 + 0.39 \times 0.12 \times 2) 2500$$

$$= (0.108 + 0.094) \times 2500 = 0.202 \times 2500 = 505 \text{ Kg/M}$$

$$W_T = 5350 + 505 = 5855 \text{ Kg/M}^2$$

$$V_{max} = 5855 \times 2.23 = 13100 \text{ Kg.}$$

$$b'd = \frac{13,100}{7/8 \times 16} = 935 \text{ cm}^2$$

$$d = 27 \text{ cms.}$$

$$b' = \frac{935}{27} = 35 \text{ cms.}$$

∴ O.K.

Find the neutral axis by summing moment at x-x.

$$(36 \times 30 + 39 \times 12 \times 2) k_d = 1080 \times 15 + 940 \times 6$$

$$(1080 + 940) k_d = 16,200 + 5640$$

$$2020 k_d = 21,840$$

$$k_d = \frac{21,840}{2020} = 1090 \text{ cms.}$$

∴ It acts as a rectangular beam

$$M_C (\text{Center}) = 207 \times 1.14 \times 0.27^2 = 21.20 \text{ T-m}$$

$$M_B (\text{Support}) = 207 \times 0.36 \times 0.27^2 = 6.70 \text{ T-m}$$

2. Reinforcement:

a. First Mid-Span

$$M = 1.23 \text{ w} = 1.23 \times 5.855 = 7.20 \text{ T-m}$$

$$M < M_C \quad \text{i.e.} \quad 7.20 < 21.20$$

$$A_s = 3.05 \times 720 = 22 \text{ cm}^2$$

$$\text{Use } 4\phi 28 \text{ mm} \quad A_s (\text{fur.}) = 24.40 \text{ cm}^2$$

Bend up two bars.

b. Other Mid-Spans

$$M = 0.81 w = 0.81 \times 5.855 = 4.75 \text{ T-m}$$

$$M < M_c \quad \text{i.e. } 4.75 < 21.20$$

$$A_s = 3.05 \times 4.75 = 14.50 \text{ cm}^2$$

$$\text{Use } 4\phi 22 \text{ mm} \quad A_s (\text{fur.}) = 15.32 \text{ cm}^2$$

Bend up two bars.

c. First Interior Support

$$M = 1.50 w = 1.50 \times 5.855 = 8.80 \text{ T-m}$$

$$M > M_c \quad \text{i.e. } 8.80 > 6.70$$

$$A_{s1} = 3.05 \times 6.70 = 20.50 \text{ cm}^2$$

$$A_{s2} = 2.97 (8.80 - 6.70) = 6.22 \text{ cm}^2$$

$$A_s = 20.50 + 6.22 = 26.72 \text{ cm}^2$$

$$A'_s = 1.01 \times 6.22 = 6.30 \text{ cm}^2$$

$$A_s (\text{fur.}) = 19.88 \text{ cm}^2$$

Add $2\phi 22$ mm

$$\bar{\Sigma} o = 13.10 \times 1.61 = 25.80 \text{ cm.}$$

$$\bar{\Sigma} o (\text{fur.}) = 45.20 \text{ cms.}$$

d. Other Interior Supports

$$M = 1.18 w = 1.18 \times 5.855 = 6.90 \text{ T-m}$$

$$\therefore M > M_c \quad \text{i.e. } 6.90 > 6.70$$

$$A_{s1} = 20.50 \text{ cm}^2$$

$$A_{s2} = 2.97 \times 0.20 = 0.59 \text{ cm}^2$$

$$A_g = 20.50 + 0.59 = 21.09 \text{ cm}^2$$

$$A'_g = 1.01 \times 0.59 = 0.60 \text{ cm}^2$$

$$A_g \text{ (fur.)} = 15.32 \text{ cm}^2$$

Add $\phi 18$ mm

$$V = 5.85 \times 1.80 = 10.50 \text{ T}$$

$$\Sigma o = 10.50 \times 1.61 = 16.90 \text{ cms}$$

$$\Sigma o \text{ (fur.)} = 38.90 \text{ cms.}$$

e. Exterior Support

$$M = 1.03 \times 5.85 = 6.02 \text{ T-m} < 6.90 \text{ T-m}$$

$$A_g = 3.05 \times 6.02 = 18.40 \text{ cm}^2$$

$$A_g \text{ (fur.)} = 12.20 \text{ cm}^2$$

Add $\phi 20$ mm

Σo (fur.) is ample

Critical Frame Beams:

1. Loads Acting:

The loads are:

- a. D.L. of Beams.
- b. Partitions.
- c. Plaster, sand, tiles, etc.
- d. Load from slab.
- e. Live loads.

The first four items are existing at any time and constitute the major part of the vertical loading .Hence two separate analyses are not rendered necessary.

The basis of the calculation is run below for the four top beams.

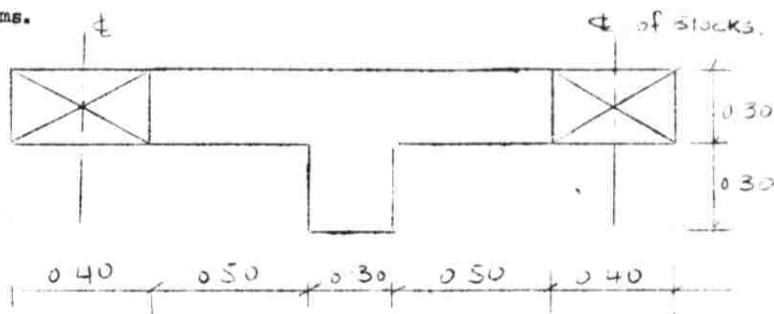


Fig 4

D.L. = 0.48×2.50 = 1.20 T/m
 Partitions = 0.50 T/m
 Load from slab = 0.40 T/m
 Plaster, sand, tiles, etc. = 0.20×1.20 = 0.24 T/m
 Live Load = 0.25×1.20 = 0.30 T/m

$w_T = 2.64 \text{ T/m}$

| Floors | Area m ² | D.L. 2.50 T/m ² (T/m) | Partitions (T/m) | Load from Slab (T/m) | Plaster, Tiles Sand, etc. (T/m) | Live Load T/m | Total Load T/m | F.E.M. | | | |
|--------|------------------------|--|---------------------|----------------------------|---------------------------------------|---------------------|----------------------|---------------------------------|--|--------------------|---------------------------------|
| | | | | | | | | Ext. Span 1 ² /12 | Mid. Span w ¹ ² /12 | 1 ² /12 | w ¹ ² /12 |
| 20-17 | 0.48 | 1.20 | 0.50 | 0.40 | 0.24 | 0.30 | 2.64 | 1.47 | 3.90 | 3.52 | 9.30 |
| 16-13 | 0.51 | 1.27 | 0.50 | 0.40 | 0.24 | 0.30 | 2.71 | 1.47 | 4.00 | 3.52 | 9.50 |
| 12-9 | 0.54 | 1.35 | 0.50 | 0.40 | 0.24 | 0.30 | 2.79 | 1.47 | 4.10 | 3.52 | 9.80 |
| 8-5 | 0.57 | 1.42 | 0.50 | 0.40 | 0.24 | 0.30 | 2.86 | 1.47 | 4.20 | 3.52 | 10.10 |
| 4-1 | 0.60 | 1.50 | 0.50 | 0.40 | 0.24 | 0.30 | 2.94 | 1.47 | 4.30 | 3.52 | 10.30 |

2. Distribution Factors:

| Joint | Kc S | Kg1 L | Kg2(Mod) R | Kc I | K | Distribution Factors | | | |
|----------|---------|----------|---------------|---------|--------|----------------------|------|------|------|
| | | | | | | S | L | R | I |
| 2Ca | 0 | 24.00 | 7.70 | 7.70 | 39.40 | 0 | 0.60 | 0.20 | 0.20 |
| 19,18,17 | 7.70 | 24.00 | 7.70 | 7.70 | 47.10 | 0.17 | 0.51 | 0.16 | 0.16 |
| 16 | 7.70 | 37.30 | 12.10 | 26.40 | 83.50 | 0.09 | 0.45 | 0.14 | 0.32 |
| 15,14,13 | 26.40 | 37.30 | 12.10 | 26.40 | 102.20 | 0.26 | 0.36 | 0.12 | 0.26 |
| 12 | 26.40 | 55.80 | 18.00 | 62.50 | 162.70 | 0.16 | 0.34 | 0.11 | 0.39 |
| 11,10,9 | 62.50 | 55.80 | 18.00 | 62.50 | 198.80 | 0.31 | 0.28 | 0.09 | 0.32 |
| 8 | 62.50 | 79.00 | 25.50 | 122.00 | 289.00 | 0.22 | 0.27 | 0.09 | 0.42 |
| 7,6,5 | 122.00 | 79.00 | 25.50 | 122.00 | 348.50 | 0.35 | 0.23 | 0.07 | 0.35 |
| 4 | 122.00 | 108.00 | 35.00 | 211.00 | 476.00 | 0.26 | 0.23 | 0.07 | 0.44 |
| 3 | 211.00 | 108.00 | 35.00 | 211.00 | 565.00 | 0.37 | 0.19 | 0.07 | 0.37 |
| 2 | 211.00 | 108.00 | 35.00 | 147.00 | 501.00 | 0.42 | 0.22 | 0.07 | 0.29 |
| 1 | 147.00 | 108.00 | 4 | 160.00 | 450.00 | 0.33 | 0.24 | 0.08 | 0.35 |

3. Maximum Positive Moment:

| Joint | w T/m | Exterior Span | | | | | Middle Span | | | | Max. Positive Moment $(wl^2/8 - \frac{a+b}{2} = (wl^2/8 - a))$ |
|-------|----------|---------------|----------|------------|------|------|-------------|----------|------------|-------|---|
| | | $l^2/8$ | $wl^2/8$ | $2xwl^2/8$ | a | b | $l^2/8$ | $wl^2/8$ | $2xwl^2/8$ | a=b | |
| 20 | 2.64 | 2.21 | 5.82 | 11.64 | 0.80 | 7.20 | 5.30 | 14.00 | 28.00 | 8.40 | 14-8.40=5.60 |
| 19 | " | " | " | " | 1.60 | 6.70 | " | " | " | 8.70 | 14-8.70=5.30 |
| 18 | " | " | " | " | 1.60 | 6.70 | " | " | " | 8.60 | 14-8.60=5.40 |
| 17 | " | " | " | " | 1.50 | 6.90 | " | " | " | 8.70 | 14-8.70=5.30 |
| 16 | 2.71 | " | 6.00 | 12.00 | 1.80 | 6.60 | " | 14.30 | 28.60 | 8.90 | 14.30-8.90=5.40 |
| 15 | " | " | " | " | 2.30 | 6.00 | " | " | " | 9.10 | 14.30-9.10=5.20 |
| 14 | " | " | " | " | 2.30 | 6.00 | " | " | " | 9.00 | 14.30-9.00=5.30 |
| 13 | " | " | " | " | 2.20 | 6.20 | " | " | " | 9.10 | 14.30-9.10=5.20 |
| 12 | 2.79 | " | 6.18 | 12.36 | 2.50 | 6.10 | " | 14.80 | 29.60 | 9.40 | 14.80-9.40=5.40 |
| 11 | " | " | " | " | 2.80 | 5.60 | " | " | " | 9.50 | 14.80-9.50=5.30 |
| 10 | " | " | " | " | 2.80 | 5.70 | " | " | " | 9.50 | 14.80-9.50=5.30 |
| 9 | " | " | " | " | 2.70 | 5.70 | " | " | " | 9.40 | 14.80-9.40=5.40 |
| 8 | 2.86 | " | 6.32 | 12.64 | 2.90 | 5.80 | " | 15.10 | 30.20 | 9.70 | 15.10-9.70=5.40 |
| 7 | " | " | " | " | 3.10 | 5.50 | " | " | " | 9.80 | 15.10-9.80=5.30 |
| 6 | " | " | " | " | 3.00 | 5.60 | " | " | " | 9.80 | 15.10-9.80=5.30 |
| 5 | " | " | " | " | 3.10 | 5.60 | " | " | " | 9.80 | 15.10-9.80=5.30 |
| 4 | 2.94 | " | 6.52 | 13.04 | 3.20 | 5.70 | " | 15.60 | 31.20 | 10.00 | 15.60-10.00=5.60 |
| 3 | " | " | " | " | 3.40 | 5.40 | " | " | " | 10.00 | 15.60-10.00=5.60 |
| 2 | " | " | " | " | 3.20 | 5.60 | " | " | " | 10.00 | 15.60-10.00=5.60 |
| 1 | " | " | " | " | 3.00 | 5.90 | " | " | " | 9.90 | 15.60-9.90=5.70 |

N.B.- All moments are in T-m.

- a and b are end moments.

4. Moment in Columns Due to Vertical Loading:

| Story | Exterior Columns | | Interior Side | |
|-------|-------------------|-------------------|-------------------|-------------------|
| | Upper Side T-m | Lower Side T-m | Upper Side T-m | Lower Side T-m |
| 20 | 0.80 | 0.80 | 1.20 | 1.10 |
| 19 | 0.80 | 0.80 | 0.90 | 0.90 |
| 18 | 0.80 | 0.80 | 1.00 | 1.00 |
| 17 | 0.70 | 0.60 | 0.80 | 0.60 |
| 16 | 1.20 | 1.20 | 1.70 | 1.70 |
| 15 | 1.10 | 1.20 | 1.40 | 1.50 |
| 14 | 1.10 | 1.20 | 1.50 | 1.60 |
| 13 | 1.00 | 0.90 | 1.30 | 1.10 |
| 12 | 1.60 | 1.50 | 2.20 | 2.00 |
| 11 | 1.30 | 1.40 | 1.90 | 1.90 |
| 10 | 1.40 | 1.40 | 1.90 | 1.90 |
| 9 | 1.30 | 1.20 | 1.80 | 1.50 |
| 8 | 1.70 | 1.70 | 2.40 | 2.20 |
| 7 | 1.40 | 1.60 | 2.10 | 2.00 |
| 6 | 1.40 | 1.60 | 2.20 | 2.20 |
| 5 | 1.50 | 1.40 | 2.00 | 1.80 |
| 4 | 1.80 | 1.80 | 2.50 | 2.30 |
| 3 | 1.60 | 1.70 | 2.30 | 2.40 |
| 2 | 1.50 | 1.70 | 2.00 | 2.20 |
| 1 | 1.30 | 1.70 | 1.80 | 0.90 |

5. Shear Equations

a. Vertical Loading

$$R_1 = \frac{wl}{2} + \frac{(M_1 + M_2)}{l}$$

$$R_2 = \frac{wl}{2} - \frac{(M_1 + M_2)}{l}$$

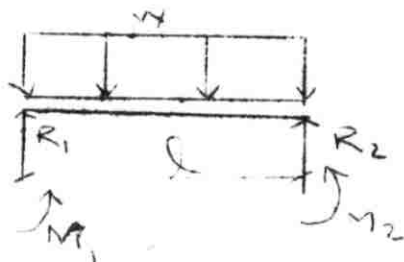


Fig 5

The signs of moments are already taken care of.

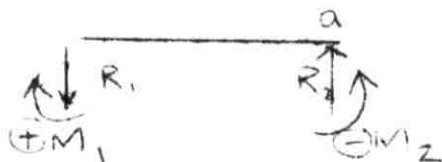
b. Wind From Left

$$M_a = 0$$

$$(M_1 - M_2) - R_1 l = 0$$

$$R_1 = \frac{+(M_1 - M_2)}{l}$$

$$R_2 = \frac{-(M_1 - M_2)}{l}$$



$$M_1 > M_2$$

Fig. 6

c. Wind From Right

$$R_1 = \frac{-(M_1 - M_2)}{l}$$

$$R_2 = \frac{+(M_1 - M_2)}{l}$$

Again signs are taken care of.

6. Shears Due to Vertical Loading:

a. Exterior Support

| Floor | M_1 (T-m) | M_2 (T-m) | (M_1+M_2) (T-M) | $\frac{M_1+M_2}{1}$ (T-m) | $\frac{wl}{2}$ (T-m) | R_1 (T) | R_2 (T) |
|-------|----------------|----------------|----------------------|------------------------------|-------------------------|--------------|--------------|
| 20 | 0.80 | 7.20 | 8.00 | 1.90 | 5.55 | 7.45 | 3.65 |
| 19 | 1.60 | 6.70 | 8.30 | 2.00 | 5.55 | 7.55 | 3.55 |
| 18 | 1.60 | 6.70 | 8.30 | 2.00 | 5.55 | 7.55 | 3.55 |
| 17 | 1.50 | 6.90 | 8.40 | 2.00 | 5.55 | 7.55 | 3.55 |
| 16 | 1.80 | 6.60 | 8.40 | 2.00 | 5.70 | 7.70 | 3.70 |
| 15 | 2.30 | 6.00 | 8.30 | 2.00 | 5.70 | 7.70 | 3.70 |
| 14 | 2.30 | 6.00 | 8.30 | 2.00 | 5.70 | 7.70 | 3.70 |
| 13 | 2.20 | 6.20 | 8.40 | 2.00 | 5.70 | 7.70 | 3.70 |
| 12 | 2.50 | 6.10 | 8.60 | 2.05 | 5.85 | 7.90 | 3.80 |
| 11 | 2.80 | 5.60 | 8.40 | 2.00 | 5.85 | 7.85 | 3.85 |
| 10 | 2.80 | 5.70 | 8.50 | 2.05 | 5.85 | 7.90 | 3.80 |
| 9 | 2.70 | 5.70 | 8.40 | 2.00 | 5.85 | 7.85 | 3.85 |
| 8 | 2.90 | 5.80 | 8.70 | 2.08 | 6.00 | 8.08 | 3.92 |
| 7 | 3.10 | 5.50 | 8.60 | 2.05 | 6.00 | 8.05 | 3.95 |
| 6 | 3.00 | 5.60 | 8.60 | 2.05 | 6.00 | 8.05 | 3.95 |
| 5 | 3.10 | 5.60 | 8.70 | 2.08 | 6.00 | 8.08 | 3.92 |
| 4 | 3.20 | 5.70 | 8.90 | 2.10 | 6.15 | 8.25 | 4.05 |
| 3 | 3.40 | 5.40 | 8.80 | 2.10 | 6.15 | 8.25 | 4.05 |
| 2 | 3.20 | 5.60 | 8.80 | 2.10 | 6.15 | 8.25 | 4.05 |
| 1 | 3.00 | 5.90 | 8.90 | 2.10 | 6.15 | 8.25 | 4.05 |

b. Interior Support

| Floor | M_1 (T-m) | $2M_1$ (T-m) | $\frac{2M_1}{l}$ (T-m) | $\frac{wl}{2}$ (T-m) | R'_2 (T) |
|-------|----------------|-----------------|---------------------------|-------------------------|---------------|
| 20 | 8.40 | 16.80 | 2.60 | 8.60 | 11.20 |
| 19 | 8.70 | 17.40 | 2.70 | 8.60 | 11.30 |
| 18 | 8.60 | 17.20 | 2.65 | 8.60 | 11.25 |
| 17 | 8.70 | 17.40 | 2.70 | 8.60 | 11.30 |
| 16 | 8.90 | 17.80 | 2.75 | 8.80 | 11.55 |
| 15 | 9.10 | 18.20 | 2.80 | 8.80 | 11.60 |
| 14 | 9.00 | 18.00 | 2.77 | 8.80 | 11.57 |
| 13 | 9.10 | 18.20 | 2.80 | 8.80 | 11.60 |
| 12 | 9.40 | 18.80 | 2.88 | 9.05 | 11.93 |
| 11 | 9.50 | 19.00 | 2.90 | 9.05 | 11.95 |
| 10 | 9.50 | 19.00 | 2.90 | 9.05 | 11.95 |
| 9 | 9.40 | 18.80 | 2.88 | 9.05 | 11.93 |
| 8 | 9.70 | 19.40 | 2.98 | 9.25 | 12.23 |
| 7 | 9.80 | 19.60 | 3.00 | 9.25 | 12.25 |
| 6 | 9.80 | 19.60 | 3.00 | 9.25 | 12.25 |
| 5 | 9.80 | 19.60 | 3.00 | 9.25 | 12.25 |
| 4 | 10.00 | 20.00 | 3.05 | 9.55 | 12.60 |
| 3 | 10.00 | 20.00 | 3.05 | 9.55 | 12.60 |
| 2 | 10.00 | 20.00 | 3.05 | 9.25 | 12.60 |
| 1 | 9.90 | 19.80 | 3.02 | 9.25 | 11.57 |

7. Shears due to Wind From Left

a. Exterior Supports

| Floor | M_1 (T-m) | M_2 (T-m) | $M_1 - M_2$ (T-m) | R_1 (T) | R_2 (T) |
|-------|----------------|----------------|----------------------|--------------|--------------|
| 20 | 0.76 | 0.63 | 0.13 | -0.03 | +0.03 |
| 19 | 2.15 | 1.76 | 0.39 | -0.09 | +0.09 |
| 18 | 4.47 | 2.89 | 1.58 | -0.38 | +0.38 |
| 17 | 4.76 | 3.74 | 1.02 | -0.24 | +0.24 |
| 16 | 5.75 | 4.99 | 0.74 | -0.18 | +0.18 |
| 15 | 7.03 | 6.10 | 0.93 | -0.22 | +0.22 |
| 14 | 8.18 | 7.03 | 1.15 | -0.27 | +0.27 |
| 13 | 8.85 | 7.50 | 1.35 | -0.32 | +0.32 |
| 12 | 9.65 | 8.59 | 1.06 | -0.25 | +0.25 |
| 11 | 11.25 | 9.89 | 1.36 | -0.32 | +0.32 |
| 10 | 11.80 | 10.92 | 0.88 | -0.21 | +0.21 |
| 9 | 12.44 | 10.43 | 2.01 | -0.50 | +0.50 |
| 8 | 13.98 | 12.80 | 1.18 | -0.28 | +0.28 |
| 7 | 15.60 | 14.43 | 1.17 | -0.28 | +0.28 |
| 6 | 16.00 | 14.72 | 1.38 | -0.33 | +0.33 |
| 5 | 16.00 | 14.48 | 1.52 | -0.36 | +0.36 |
| 4 | 17.67 | 16.18 | 1.49 | -0.35 | +0.35 |
| 3 | 22.20 | 19.43 | 2.77 | -0.66 | +0.66 |
| 2 | 41.00 | 39.27 | 1.73 | -0.41 | +0.41 |
| 1 | 43.75 | 40.53 | 2.22 | -0.52 | +0.52 |

8. Final Shears:

a. Exterior Supports

| Floor | Pos. Moment at Exterior Support | | | Neg. Moment at Exterior Support | |
|-------|---------------------------------|------------------|--------------------|---------------------------------|--------------------|
| | D.L. (T) | Wind Load (T) | Total Shear (T) | Wind Load (T) | Total Shear (T) |
| 20 | +7.45 | -0.03 | +7.45 | +0.03 | +7.48 |
| 19 | +7.55 | -0.09 | +7.55 | +0.09 | +7.64 |
| 18 | +7.55 | -0.038 | +7.55 | +0.38 | 7.93 |
| 17 | +7.55 | -0.24 | +7.55 | +0.24 | 7.79 |
| 16 | +7.70 | -0.18 | +7.70 | +0.18 | 7.88 |
| 15 | +7.70 | -0.22 | +7.70 | +0.22 | 7.92 |
| 14 | +7.70 | -0.27 | +7.70 | +0.27 | 7.92 |
| 13 | +7.70 | -0.32 | +7.70 | +0.32 | 8.02 |
| 12 | +7.90 | -0.25 | +7.90 | +0.25 | 8.15 |
| 11 | +7.85 | -0.32 | +7.85 | +0.32 | 8.17 |
| 10 | +7.90 | -0.21 | +7.90 | +0.21 | 8.11 |
| 9 | +7.85 | -0.50 | +7.85 | +0.50 | 8.35 |
| 8 | +8.08 | -0.28 | +8.08 | +0.28 | 8.36 |
| 7 | +8.05 | -0.28 | +8.05 | +0.28 | 8.33 |
| 6 | +8.05 | -0.33 | +8.05 | +0.33 | 8.38 |
| 5 | +8.08 | -0.36 | +8.08 | +0.36 | 8.44 |
| 4 | +8.25 | -0.35 | +8.25 | +0.35 | 5.60 |
| 3 | +8.25 | -0.66 | +8.25 | +0.66 | 8.91 |
| 2 | +8.25 | -0.41 | +8.25 | +0.41 | 8.66 |
| 1 | +8.25 | -0.52 | +8.25 | +0.52 | 8.77 |

b. Interior Supports

| Floor | Neg. Moment at Interior Support | | | Pos. Moment at Interior Support | |
|-------|---------------------------------|------------------|-------------------|---------------------------------|-------------------|
| | D.L. (T) | Wind Load (T) | Total Load (T) | Wind Load (T) | Total Load (T) |
| 20 | +3.65 | +0.03 | 3.68 | -0.03 | 3.65 |
| 19 | +3.55 | +0.09 | 3.64 | -0.09 | 3.55 |
| 18 | +3.55 | +0.38 | 3.93 | -0.38 | 3.55 |
| 17 | +3.55 | +0.24 | 3.79 | -0.24 | 3.55 |
| 16 | +3.70 | +0.18 | 3.88 | -0.18 | 3.70 |
| 15 | +3.70 | +0.22 | 3.92 | -0.22 | 3.70 |
| 14 | +3.70 | +0.27 | 3.97 | -0.27 | 3.70 |
| 13 | +3.70 | +0.32 | 4.02 | -0.32 | 3.70 |
| 12 | +3.80 | +0.25 | 4.05 | -0.25 | 3.80 |
| 11 | +3.85 | +0.32 | 4.17 | -0.32 | 3.85 |
| 10 | +3.80 | +0.21 | 4.01 | -0.21 | 3.80 |
| 9 | +3.85 | +0.50 | 4.35 | -0.50 | 3.85 |
| 8 | +3.92 | +0.28 | 4.20 | -0.28 | 3.92 |
| 7 | +3.95 | +0.28 | 4.23 | -0.28 | 3.95 |
| 6 | +3.95 | +0.33 | 4.28 | -0.33 | 3.95 |
| 5 | +3.92 | +0.36 | 4.28 | -0.36 | 3.92 |
| 4 | +4.05 | +0.35 | 4.40 | -0.35 | 4.05 |
| 3 | +4.05 | +0.66 | 4.71 | -0.66 | 4.05 |
| 2 | +4.05 | +0.41 | 4.46 | -0.41 | 4.05 |
| 1 | +4.05 | +0.52 | 4.57 | -0.52 | 4.05 |

| FLOOR | MR | 1st Mid span M < MR | | | | 2nd Mid span M < MR | | | | Exterior Support | | | | | | | | | | | | | | Interior Support | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
|-------|-------|------------------------|---------------------------|---------------|--------------------|--|---------------------------|---------------|--------------------|--|---|---------------|--------------------|--------------------------------|-------|-----|--------|---|---------|------------|-----------|------------|---------------------------------|--------------------------------|-------------------------|----------|-------------------|----------|-------------------|------------|---------------------------------|--------------------------------|-------|------|------------|------------|---------------------------------|--------------------------------|--|-------------------|----------|------------|------|--------------------|---------------|--|------|--------------------|---------------|--------------------|---|--------------------|---------------------|--------------------|---|--------------------|---------------|--------------------|---|---------------------|---------------|--------------------|---|--------------------|---------------|--------------------|
| | | Support 165 bd 2 | Rft (High strength steel) | | | | Rft (High strength steel) | | | | Positive Moment (M < MR) Rft (High strength steel) | | | | | | | Neg. Moment (M < MR) Rft (High strength steel) | | | | | | | Positive Moment Bond | | | | | | | Neg. Moment Bond | | | | | | | Positive Moment (M < Mc) Rft. (High strength steel) | | | | | | | Negative Moment (M < Mc) Rft. (High strength steel) | | | | | | | Pos. Moment Bond | | | | | | | Neg. Moment Bond | | | | | | |
| | | | M (T-m) | As (Reqd) | | As (Fur) from Support (cm ²) | M (T-m) | As (Reqd) | | As (Fur) from Support (cm ²) | M (T-m) | As (Reqd) | | As (Fur) (cm ²) | b | d | bd | P. As bd | K | Kd (cm) | e (cm) | M (T-m) | As (Reqd) (cm ²) | Af (Fur) (cm ²) | 0.435 d | V (T) | Σd (Reqd) (cm) | V (T) | Σd (Reqd) (cm) | M (T-m) | As (Reqd) (cm ²) | As (Fur) (cm ²) | P | K | Kd (cm) | M (T-m) | As (Reqd) (cm ²) | As (Fur) (cm ²) | V (T) | Σd (Reqd) (cm) | V (T) | Σd (cm) | | | | | | | | | | | | | | | | | | | | | | | | |
| | | | | Coef. of M | (cm ²) | | | Coef. of M | (cm ²) | | | Coef. of M | (cm ²) | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | Φ | (cm ²) | Coef. of M | (cm ²) | Φ | (cm ²) | Coef. of M | (cm ²) | Φ | (cm ²) | Coef. of M | (cm ²) | Φ | (cm ²) | Coef. of M | (cm ²) | Φ | (cm ²) | Coef. of M | (cm ²) | Φ | (cm ²) | Coef. of M | (cm ²) |
| 1 | 42.00 | 167.00 | 2.50 | 0.512 | 1.46 | Ample | 5.50 | 0.512 | 320 | Ample | 36.50 | 0.60 | 22.20 | 8Φ20 | 25.12 | 130 | 88 | 11,900 | 0.0022 | 0.164 | 19.50 | 10 | 37.30 | 22.70 | 8Φ20 | 25.12 | 0.483 | 8.25 | 4.00 | 8.77 | 4.20 | 31.60 | 19.30 | 8Φ20 | 25.12 | 0.0022 | 0.164 | 19.50 | 34.50 | 21.00 | 8Φ20 | 25.12 | 4.05 | 2.00 | 4.57 | 2.20 | | | | | | | | | | | | | | | | | | | | |
| 2 | " | " | " | " | " | " | " | " | " | " | 34.80 | " | 21.20 | 8Φ20 | 25.12 | " | " | " | 0.0022 | 0.164 | 19.50 | " | 34.00 | 20.70 | 8Φ20 | 25.12 | " | " | " | 8.60 | 4.17 | 31.10 | 18.90 | 8Φ20 | 25.12 | " | " | " | 35.60 | 21.10 | " | 25.12 | " | " | 4.46 | 2.15 | | | | | | | | | | | | | | | | | | | | |
| 3 | " | " | " | " | " | " | " | " | " | " | 17.00 | " | 0.00 | 8Φ14 | 12.00 | " | " | " | 0.00195 | 0.119 | 10.50 | " | 20.10 | 12.20 | 8Φ16 | 16.24 | " | " | " | 8.01 | 4.30 | 12.40 | 7.60 | 8Φ14 | 12.00 | 0.00160 | 0.119 | 10.50 | 19.15 | 11.10 | 8Φ14 | 12.00 | " | " | 4.71 | 2.27 | | | | | | | | | | | | | | | | | | | | |
| 4 | " | " | " | " | " | " | " | " | " | " | 12.60 | " | 7.70 | 8Φ12 | 9.04 | " | " | " | 0.0008 | Kdct | " | " | 14.50 | 8.85 | 8Φ14 | 12.00 | " | " | " | 8.60 | 8.70 | 9.50 | 5.80 | 8Φ10 | 6.14 | " | " | Kdct | 15.75 | 9.60 | " | " | " | 4.40 | 2.12 | | | | | | | | | | | | | | | | | | | | | |
| 5 | 33.60 | 130.00 | " | 0.652 | 1.63 | " | " | 0.652 | 3.58 | " | 0.50 | 0.688 | 7.90 | 8Φ12 | 9.04 | 78 | 10,100 | 0.0008 | " | " | " | 15.00 | 10.30 | 8Φ14 | 12.00 | 0.545 | 8.08 | 4.40 | 8.44 | 4.60 | 7.65 | 5.25 | 8Φ10 | " | " | " | 15.80 | 10.40 | " | " | 3.92 | 2.13 | 4.29 | 2.33 | | | | | | | | | | | | | | | | | | | | | | |
| 6 | " | " | " | " | " | " | " | " | " | " | 0.60 | " | 7.95 | 8Φ12 | 9.04 | " | " | " | 0.0008 | " | " | " | 15.00 | 10.30 | 8Φ14 | 12.00 | " | " | " | 8.39 | 4.55 | 7.90 | 5.02 | 8Φ10 | " | " | " | 17.20 | 11.20 | " | " | 3.95 | 2.15 | 4.29 | 2.53 | | | | | | | | | | | | | | | | | | | | | |
| 7 | " | " | " | " | " | " | " | " | " | " | 0.00 | " | 7.55 | 8Φ12 | 9.04 | " | " | " | 0.0019 | " | " | " | 14.50 | 9.95 | 8Φ14 | " | " | " | 8.37 | 4.50 | 7.55 | 5.20 | 8Φ10 | " | " | " | 15.50 | 10.60 | " | " | 3.95 | " | 4.23 | 2.20 | | | | | | | | | | | | | | | | | | | | | | |
| 8 | " | " | " | " | " | " | " | " | " | " | 10.10 | " | 7.00 | 8Φ12 | 9.04 | " | " | " | 0.0008 | " | " | " | 13.99 | 9.60 | 8Φ14 | " | " | " | 8.36 | 4.50 | 5.45 | 3.75 | 8Φ10 | " | " | " | 15.15 | 10.40 | " | " | 3.92 | 2.13 | 4.20 | 2.28 | | | | | | | | | | | | | | | | | | | | | | |
| 9 | 25.80 | 99.20 | " | 0.782 | 1.86 | " | " | 0.782 | 4.07 | " | 9.00 | 0.790 | 7.10 | 8Φ12 | 9.04 | 68 | 9,800 | 0.001 | " | " | " | 12.40 | 9.90 | 8Φ14 | " | 0.625 | 7.85 | 4.90 | 8.35 | 5.20 | 4.72 | 3.95 | 8Φ10 | " | " | " | 13.50 | 10.70 | " | " | 3.85 | 2.40 | 4.35 | 2.72 | | | | | | | | | | | | | | | | | | | | | | |
| 10 | " | " | " | " | " | " | " | " | " | " | 8.20 | " | 6.45 | 8Φ12 | 9.04 | " | " | " | 0.001 | " | " | " | 4.00 | 8.70 | 8Φ14 | " | " | " | 7.90 | 4.93 | 8.11 | 5.08 | 4.10 | 3.25 | 8Φ10 | " | " | " | 14.50 | 11.50 | " | " | 3.90 | 2.39 | 4.01 | 2.50 | | | | | | | | | | | | | | | | | | | | |
| 11 | " | " | " | " | " | " | " | " | " | " | 7.80 | " | 6.15 | 8Φ12 | 9.04 | " | " | " | 0.001 | " | " | " | 8.50 | 9.05 | 8Φ14 | " | " | " | 7.85 | 4.90 | 8.17 | 5.10 | 3.50 | 2.76 | 8Φ10 | " | " | " | 13.00 | 11.30 | " | " | 3.85 | 2.40 | 4.17 | 2.60 | | | | | | | | | | | | | | | | | | | | |
| 12 | " | " | " | " | " | " | " | " | " | " | 6.60 | " | 5.20 | 8Φ10 | 6.04 | " | " | " | 0.0007 | " | " | " | 10.00 | 7.90 | 8Φ12 | 9.04 | " | " | " | 7.90 | 4.98 | 8.15 | " | 1.50 | 1.19 | 8Φ10 | " | " | " | 12.00 | 9.50 | " | " | 3.80 | 2.34 | 4.05 | 2.53 | | | | | | | | | | | | | | | | | | | |
| 13 | 19.20 | 72.30 | " | 0.862 | 2.16 | " | " | 0.862 | 4.73 | " | 6.20 | 0.925 | 5.77 | 8Φ10 | 6.04 | 58 | 7,500 | 0.0008 | " | " | " | 9.50 | 8.80 | 8Φ12 | " | 0.732 | 7.70 | 5.65 | 8.02 | 5.90 | 0.75 | 0.69 | 8Φ10 | " | " | " | 12.00 | 11.10 | " | " | 3.70 | 2.72 | 4.02 | 2.93 | | | | | | | | | | | | | | | | | | | | | | |
| 14 | " | " | " | " | " | " | " | " | " | " | 5.10 | " | 4.73 | 8Φ10 | 6.04 | " | " | " | 0.0009 | " | " | " | 9.00 | 8.30 | 8Φ12 | " | " | " | 7.92 | 5.80 | 0.50 | 0.46 | 8Φ10 | " | " | " | 11.60 | 11.70 | " | " | " | " | 2.97 | 2.00 | | | | | | | | | | | | | | | | | | | | | | |
| 15 | " | " | " | " | " | " | " | " | " | " | 4.20 | " | 3.80 | 8Φ10 | 6.04 | " | " | " | 0.0008 | " | " | " | 8.00 | 7.40 | 8Φ12 | " | " | " | 7.92 | " | 0 | " | " | " | 10.50 | 9.70 | " | " | " | " | 3.92 | 2.85 | | | | | | | | | | | | | | | | | | | | | | | | |
| 16 | " | " | " | " | " | " | " | " | " | " | 3.35 | " | 3.10 | 8Φ10 | 6.04 | " | " | " | 0.0008 | " | " | " | 6.00 | 5.55 | 8Φ12 | 6.04 | " | " | " | 7.88 | 5.75 | 0 | " | " | " | 9.60 | 8.90 | " | " | " | " | 3.88 | 2.80 | | | | | | | | | | | | | | | | | | | | | | | |
| 17 | 13.50 | 49.50 | " | 1.030 | 2.57 | " | " | 1.030 | 5.63 | " | 2.89 | 1.110 | 3.20 | 8Φ10 | 6.04 | 47 | 6,230 | 0.0008 | " | " | " | 5.50 | 6.10 | 8Φ12 | " | 0.885 | 7.55 | 6.70 | 7.79 | 6.90 | 0 | " | " | " | 9.30 | 10.30 | " | " | 3.55 | 3.14 | 3.79 | 3.35 | | | | | | | | | | | | | | | | | | | | | | | | |
| 18 | " | " | " | " | " | " | " | " | " | " | 2.10 | " | 2.33 | 8Φ10 | 6.04 | " | " | " | " | " | " | " | 5.50 | 6.10 | 8Φ12 | " | " | " | 7.93 | 7.00 | 0 | " | " | " | 8.50 | 8.40 | " | " | " | " | 3.93 | 3.47 | | | | | | | | | | | | | | | | | | | | | | | | |
| 19 | " | " | " | " | " | " | " | " | " | " | 0 | " | 0 | " | " | " | " | " | " | " | " | " | 3.30 | 3.65 | 8Φ12 | " | " | " | 7.64 | 6.75 | 0 | " | " | " | 7.30 | 8.10 | " | " | " | " | 3.64 | 3.22 | | | | | | | | | | | | | | | | | | | | | | | | |
| 20 | " | " | " | " | " | " | " | " | " | " | 0 | " | 0 | " | " | " | " | " | " | " | " | " | 1.22 | 1.33 | 8Φ12 | " | " | " | 7.45 | 6.60 | 7.49 | 6.60 | 0 | " | " | 8.00 | 8.85 | " | " | " | " | 3.68 | 3.25 | | | | | | | | | | | | | | | | | | | | | | | |

N.B. Stirrups are not required.

ANALYSIS OF THE EFFECT OF WIND ON A HIGH REINFORCED CONCRETE BUILDING

Comparison of Approximate and Exact Methods

| | | |
|----------|----------------|------------------------|
| COMPUTER | RIAD SHAHIN | REINFORCEMENT IN BEAMS |
| CHK'D BY | RIAD SHAHIN | |
| APP'D BY | DR JACK NASSER | |

DATE: DECEMBER 1964 SHEET NO 142/

| FLOOR | MR | 1st Mid span M < MR | | | | | | 2nd Mid span M < MR | | | | | | Exterior Support | | | | | | | | | | | | Interior Support | | | | | | | | | | | | | | | | | | | | | | |
|-------|-------|---------------------|--------------------|---------------------------|-------|---------------------------|--------------------|---------------------------|--------------------|--------------------------|-------|-------|--------------------|----------------------|-------|------|--------|-----------------|--------------------|--------------------|-------|-------------|--------------------|-------|-------|--------------------------|-------|-------|--------------------|--------------------------|------|-------|--------------------|-------|-------|---------|-------|-------|--------------------|--------------------|-------|-------|--------------------|-------|------|------|------|------|
| | | Support | | Rft (High strength steel) | | Rft (High strength steel) | | Rft (High strength steel) | | Positive Moment (M < MR) | | | | Neg. Moment (M > MR) | | | | Positive Moment | | | | Neg. Moment | | | | Positive Moment (M < Mc) | | | | Negative Moment (M > Mc) | | | | | | | | | | | | | | | | | | |
| | | M | As (Reqd) | As (Fon) | M | As (Reqd) | As (Fon) | M | As (Reqd) | As (Fon) | b | d | bd | P.A.S | K | Kd | E | M | As (Reqd) | As (Fon) | b | d | bd | P.A.S | K | Kd | E | M | As (Reqd) | As (Fon) | b | d | bd | P.A.S | K | Kd | E | M | As (Reqd) | As (Fon) | b | d | bd | P.A.S | K | Kd | E | |
| | | (T-m) | (cm ²) | (cm ²) | (T-m) | (cm ²) | (cm ²) | (T-m) | (cm ²) | (cm ²) | (cm) | (cm) | (cm ²) | (cm) | (cm) | (cm) | (cm) | (T-m) | (cm ²) | (cm ²) | (cm) | (cm) | (cm ²) | (cm) | (cm) | (cm) | (cm) | (T-m) | (cm ²) | (cm ²) | (cm) | (cm) | (cm ²) | (cm) | (cm) | (cm) | (cm) | (T-m) | (cm ²) | (cm ²) | (cm) | (cm) | (cm ²) | (cm) | (cm) | (cm) | (cm) | |
| 1 | 42.80 | 167.10 | 2.50 | 0.552 | 1.46 | Ample | 5.50 | 0.582 | 3.20 | Ample | 36.50 | 0.60 | 22.20 | 8Φ20 | 25.12 | 130 | 88 | 11,900 | 0.0022 | 0.164 | 10.50 | 30 | 37.30 | 22.70 | 8Φ20 | 25.12 | 0.483 | 8.25 | 4.00 | 8.77 | 4.20 | 31.60 | 19.30 | 8Φ20 | 25.12 | 0.0022 | 0.164 | 10.50 | 34.50 | 21.00 | 8Φ20 | 25.12 | 4.05 | 2.00 | 4.57 | 2.20 | | |
| 2 | " | " | " | " | " | " | " | " | " | " | 34.80 | " | 21.20 | 8Φ20 | 25.12 | " | " | " | 0.0022 | 0.164 | 10.50 | " | 34.00 | 20.70 | 8Φ20 | 25.12 | " | " | " | 8.60 | 4.17 | 31.10 | 18.90 | 8Φ20 | 25.12 | " | " | " | 35.60 | 8.10 | " | 25.12 | " | " | 4.46 | 2.15 | | |
| 3 | " | " | " | " | " | " | " | " | " | " | 17.00 | " | 0.00 | 8Φ14 | 12.00 | " | " | " | 0.00105 | 0.119 | 10.50 | " | 20.10 | 12.20 | 8Φ16 | 16.24 | " | " | " | 8.01 | 4.30 | 12.40 | 7.60 | 8Φ19 | 12.00 | 0.00105 | 0.119 | 10.50 | 18.15 | 11.10 | 8Φ19 | 12.00 | " | " | 4.71 | 2.27 | | |
| 4 | " | " | " | " | " | " | " | " | " | " | 12.60 | " | 7.70 | 8Φ12 | 9.04 | " | " | " | 0.0008 | | | | | 10.50 | 3.85 | 8Φ14 | 12.00 | " | " | " | 5.60 | 2.70 | 9.50 | 5.80 | 8Φ10 | 6.69 | | | | | | | | 4.90 | 2.12 | | | |
| 5 | 33.60 | 110.00 | " | 0.652 | 1.63 | " | " | 0.652 | 3.51 | " | 1.50 | 0.688 | 7.90 | 8Φ12 | 9.04 | 78 | 10,100 | 0.0008 | | | | | 15.00 | 10.30 | 8Φ14 | 12.00 | 0.545 | 8.08 | 4.40 | 8.44 | 4.60 | 7.65 | 5.25 | 8Φ10 | " | " | " | 15.80 | 10.90 | " | " | 3.92 | 2.13 | 4.28 | 2.33 | | | |
| 6 | " | " | " | " | " | " | " | " | " | " | 1.60 | " | 7.95 | 8Φ12 | 9.04 | " | " | " | 0.0008 | | | | | 15.00 | 10.30 | 8Φ14 | 12.00 | " | " | " | 8.05 | " | 8.38 | 4.55 | 7.90 | 5.42 | 8Φ10 | " | " | " | 17.20 | 11.80 | " | " | 3.95 | 2.15 | 4.28 | 2.53 |
| 7 | " | " | " | " | " | " | " | " | " | " | 4.00 | " | 7.55 | 8Φ12 | 9.04 | " | " | " | 0.0008 | | | | | 14.50 | 9.95 | 8Φ14 | " | " | " | 8.33 | 4.50 | 7.55 | 5.20 | 8Φ10 | " | " | " | 15.50 | 10.60 | " | " | 3.95 | " | 4.23 | 2.30 | | | |
| 8 | " | " | " | " | " | " | " | " | " | " | 10.10 | " | 7.00 | 8Φ12 | 9.04 | " | " | " | 0.0008 | | | | | 13.99 | 9.60 | 8Φ14 | " | " | " | 8.08 | " | 8.36 | 4.50 | 5.45 | 3.75 | 8Φ10 | " | " | " | 15.15 | 10.40 | " | " | 3.92 | 2.13 | 4.20 | 2.28 | |
| 9 | 25.80 | 99.20 | " | 0.742 | 1.86 | " | " | 0.742 | 4.07 | " | 9.00 | 0.790 | 7.10 | 8Φ12 | 9.04 | 68 | 9,800 | 0.001 | | | | | 12.40 | 9.80 | 8Φ14 | " | 0.625 | 7.75 | 4.90 | 8.35 | 5.20 | 4.73 | 3.23 | 8Φ10 | " | " | " | 13.50 | 10.70 | " | " | 3.85 | 2.40 | 4.35 | 2.72 | | | |
| 10 | " | " | " | " | " | " | " | " | " | " | 8.20 | " | 6.45 | 8Φ12 | 9.04 | " | " | " | 0.001 | | | | | 11.00 | 9.70 | 8Φ14 | " | " | " | 7.90 | 4.93 | 8.11 | 5.08 | 4.10 | 3.25 | 8Φ10 | " | " | " | 14.50 | 11.50 | " | " | 3.80 | 2.38 | 4.01 | 2.50 | |
| 11 | " | " | " | " | " | " | " | " | " | " | 7.80 | " | 6.15 | 8Φ12 | 9.04 | " | " | " | 0.001 | | | | | 8.50 | 9.05 | 8Φ14 | " | " | " | 7.85 | 4.90 | 8.17 | 5.10 | 3.50 | 2.76 | 8Φ10 | " | " | " | 13.00 | 11.30 | " | " | 3.85 | 2.40 | 4.17 | 2.60 | |
| 12 | " | " | " | " | " | " | " | " | " | " | 6.60 | " | 5.20 | 8Φ10 | 6.04 | " | " | " | 0.0007 | | | | | 10.00 | 7.90 | 8Φ12 | 9.04 | " | " | 7.90 | 4.93 | 8.15 | " | 1.50 | 1.19 | 8Φ10 | " | " | " | 12.00 | 9.50 | " | " | 3.80 | 2.34 | 4.05 | 2.53 | |
| 13 | 19.20 | 72.30 | " | 0.862 | 2.16 | " | " | 0.862 | 4.73 | " | 6.20 | 0.925 | 5.72 | 8Φ10 | 6.04 | 58 | 7,500 | 0.0008 | | | | | 9.50 | 8.80 | 8Φ12 | " | 0.732 | 7.70 | 5.65 | 8.02 | 5.90 | 0.75 | 0.69 | 8Φ10 | " | " | " | 12.00 | 11.10 | " | " | 3.70 | 2.73 | 4.02 | 2.93 | | | |
| 14 | " | " | " | " | " | " | " | " | " | " | 5.10 | " | 4.73 | 8Φ10 | 6.04 | " | " | " | 0.0009 | | | | | 9.00 | 8.30 | 8Φ12 | " | " | " | 7.92 | 5.80 | 0.50 | 0.46 | 8Φ10 | " | " | " | 11.60 | 11.70 | " | " | " | " | 3.97 | 2.00 | | | |
| 15 | " | " | " | " | " | " | " | " | " | " | 4.20 | " | 3.90 | 8Φ10 | 6.04 | " | " | " | 0.0008 | | | | | 8.00 | 7.40 | 8Φ12 | " | " | " | 7.92 | " | 0 | " | " | " | 10.50 | 9.70 | " | " | " | " | 3.92 | 2.85 | | | | | |
| 16 | " | " | " | " | " | " | " | " | " | " | 3.35 | " | 3.10 | 8Φ10 | 6.04 | " | " | " | 0.0008 | | | | | 6.00 | 5.55 | 8Φ12 | 6.04 | " | " | 7.98 | 5.75 | 0 | " | " | " | 9.60 | 8.90 | " | " | " | " | 3.88 | 2.70 | | | | | |
| 17 | 13.50 | 49.50 | " | 1.030 | 2.57 | " | " | 1.030 | 5.63 | " | 2.89 | 1.110 | 3.20 | 8Φ10 | 6.04 | 49 | 6,230 | 0.0008 | | | | | 5.50 | 6.10 | 8Φ12 | " | 0.885 | 7.55 | 6.70 | 7.79 | 6.90 | 0 | " | " | " | 9.30 | 10.30 | " | " | 3.55 | 3.14 | 3.79 | 3.35 | | | | | |
| 18 | " | " | " | " | " | " | " | " | " | " | 2.10 | " | 2.33 | 8Φ10 | 6.04 | " | " | " | | | | | 5.50 | 6.10 | 8Φ12 | " | " | " | 7.93 | 7.00 | 0 | " | " | " | 8.50 | 9.40 | " | " | " | " | 3.93 | 3.47 | | | | | | |
| 19 | " | " | " | " | " | " | " | " | " | " | 0 | " | 0 | " | " | " | " | " | | | | | 3.30 | 3.65 | 8Φ12 | " | " | " | 7.64 | 6.75 | 0 | " | " | " | 7.30 | 9.10 | " | " | " | " | 3.64 | 3.22 | | | | | | |
| 20 | " | " | " | " | " | " | " | " | " | " | 0 | " | 0 | " | " | " | " | " | | | | | 1.22 | 1.33 | 8Φ12 | " | " | " | 7.45 | 6.60 | 7.49 | 6.60 | 0 | " | " | " | 8.00 | 8.85 | " | " | " | " | 3.68 | 3.25 | | | | |

N.B. Stirrups are not required.

ANALYSIS OF THE EFFECT OF WIND ON A HIGH REINFORCED CONCRETE BUILDING

Comparison of Approximate and Exact Methods

COMPUTER : RIAD SHAHIN

CHK'D BY : RIAD SHAHIN

APP'D BY : DR. JACK NASSER

REINFORCEMENT IN BEAMS

DATE: DECEMBER 1964 SHEET NO 142/

PART C
CRITICAL FRAME COLUMNS

General:

The sizes of columns have been changed once. In the first case, special effort was made to use the minimum allowable percentage of steel which did not work out properly. In the second case the sections were reduced almost to half which implied the use of high percentages of steel. The basis of the design are:

1. Load from slab = 1 T/m^2
2. Working stresses
 - a. Interior Columns : 600 T/m^2
 - b. Exterior Columns : 520 T/m^2
 - c. Angle Columns : 450 T/m^2

The calculations for the second case are enclosed hereinafter.

Dead Load Analysis:

| Story | Section mxm | Area m^2 | Height m | Volume m^3 | w T/m^3 | Weight T |
|-------|----------------|----------------------|-------------|------------------------|---------------------|-------------|
| 20-17 | 0.50 x 0.40 | 0.20 | 3.40 | 0.68 | 2.50 | 1.70 |
| 16-13 | 0.50 x 0.60 | 0.30 | 3.40 | 1.02 | 2.50 | 2.55 |
| 12-8 | 0.50 x 0.80 | 0.40 | 3.40 | 1.36 | 2.50 | 3.40 |
| 8-4 | 0.50 x 1.00 | 0.50 | 3.40 | 1.70 | 2.50 | 4.25 |
| 4-2 | 0.50 x 1.20 | 0.60 | 3.40 | 2.04 | 2.50 | 5.10 |
| 2-1 | 0.50 x 1.20 | 0.60 | 4.90 | 2.94 | 2.50 | 7.25 |
| 1-0 | 0.50 x 1.20 | 0.60 | 4.50 | 2.70 | 2.50 | 6.75 |

Load From Slab:

| Column | Area m x m | Load T |
|----------------|--|-----------|
| C ₂ | $(2.85+4.20) \times \frac{4.10}{2} = 7.05 \times 2.05 = 14.40$ | 14.40 |
| C ₄ | $(4.20+6.50) \times \frac{4.10}{2} = 10.70 \times 2.05 = 22$ | 22 |

Load From Tank:

$$C_4 = 71 \text{ T (1)}$$

$$C_2 = 0$$

Total Loads / Floor:

| Story | Column C ₄ | | | Column C ₂ | | |
|-------|--------------------------|-------------|--------------|--------------------------|-------------|--------------|
| | Load from slab (T) | D.L. (T) | Total (T) | Load from slab (T) | D.L. (T) | Total (T) |
| 20-17 | 22 | 1.70 | 23.70 | 14.40 | 1.70 | 16.10 |
| 16-13 | 22 | 2.55 | 24.55 | 14.40 | 2.55 | 16.95 |
| 12-9 | 22 | 3.40 | 25.40 | 14.40 | 3.40 | 17.80 |
| 8-5 | 22 | 4.25 | 26.25 | 14.40 | 4.25 | 18.65 |
| 4-3 | 22 | 5.10 | 27.10 | 14.40 | 5.10 | 19.50 |
| 2 | 22 | 7.25 | 29.25 | 14.40 | 7.25 | 21.65 |
| 1 | 22 | 6.75 | 28.75 | 14.40 | 6.75 | 21.15 |

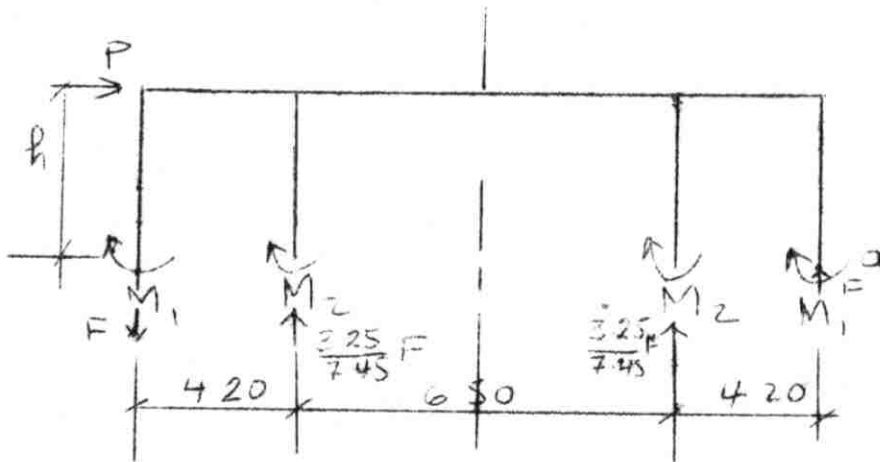
(1) The load from the tank was calculated on the basis of a detailed design of the tank.

Total Loads:

| Floor | Column C ₄ | | | Column C ₂ | |
|-------|-------------------------------|--------------------------|-----------------------|-----------------------------|----------------------|
| | D.L.+Load from slab (T) | Load from Tank (T) | Total (T) | Load From Slab (T) | Total Load (T) |
| 20 | 23.70 | 71 | $23.70+71.00=94.70$ | 16.10 | 16.10 |
| 19 | | | $94.70+23.70=118.40$ | | 32.20 |
| 18 | | | $118.40+23.70=142.10$ | | 48.30 |
| 17 | | | $142.10+23.70=165.80$ | | 64.40 |
| 16 | 24.55 | | $165.80+24.55=190.35$ | 16.95 | 81.35 |
| 15 | | | $190.35+24.55=214.90$ | | 98.30 |
| 14 | | | $214.90+24.55=239.45$ | | 115.25 |
| 13 | | | $239.45+24.55=264.00$ | | 132.20 |
| 12 | 25.40 | | $264.00+25.40=289.40$ | 17.80 | 150.00 |
| 11 | | | $289.40+25.40=314.80$ | | 167.80 |
| 10 | | | $314.80+25.40=340.20$ | | 185.60 |
| 9 | | | $340.20+25.40=365.60$ | | 203.40 |
| 8 | 26.25 | | $365.60+26.25=391.85$ | | 222.05 |
| 7 | | | $391.85+26.25=418.10$ | | 240.70 |
| 6 | | | $418.10+26.25=444.35$ | | 259.35 |
| 5 | | | $444.35+26.25=470.60$ | | 278.00 |
| 4 | 27.10 | | $470.60+27.10=497.70$ | 19.50 | 297.50 |
| 3 | | | $497.70+27.10=524.80$ | | 317.00 |
| 2 | 29.25 | | $524.80+29.25=554.05$ | 21.65 | 338.65 |
| 1 | 28.75 | | $554.05+28.75=582.80$ | 21.15 | 359.80 |

Axial Stresses Due to Wind Loading:

The method adopted assumes that the axial stresses are proportional to their distances from the center of gravity of the structure. Since, the structure is symmetrical, and all columns are of the same dimension the center of gravity coincides with the center of symmetry. The problem then boils down to one of statics.



$$\sum Ma = 0$$

$$Ph - (M_1 + M_2)2 + \frac{3.25}{7.45} \times 4.20F - \frac{3.25}{7.45} \times 10.70 F - 14.90 F = 0$$

$$Ph - 2(M_1 + M_2) + 1.83 F - 4.65F - 14.90 F = 0$$

$$Ph - 2(M_1 + M_2) - 17.72 F = 0$$

If we have more than one load then:

$$\sum Ph - 2(M_1 + M_2) - 17.72 F = 0$$

$$17.72 F = \sum Ph - 2(M_1 + M_2)$$

$$F = \frac{\sum Ph - 2(M_1 + M_2)}{17.72}$$

| JOINT | 20 | | | 19 | | | 18 | | | 17 | | | 16 | | | 15 | | | JOINT | 8 | | | 7 | | | 6 | | | 5 | | | 4 | | | 3 | | |
|-------|------|------|------|------|------|-------|------|-------|-------|------|-------|-------|------|-------|-------|------|-------|-------|-------|------|-------|--------|------|-------|--------|------|-------|--------|-------|-------|--------|-------|-------|--------|-------|-------|--------|
| | P | h | Ph | P | h | Ph | P | h | Ph | P | h | Ph | P | h | Ph | P | h | Ph | | P | h | Ph | P | h | Ph | P | h | Ph | P | h | Ph | P | h | Ph | P | h | Ph |
| 20 | 1.85 | 3.40 | 6.28 | 1.85 | 6.80 | 12.60 | 1.85 | 10.20 | 18.80 | 1.85 | 13.60 | 25.00 | 1.85 | 17.00 | 31.30 | 1.85 | 20.40 | 37.70 | 20 | 1.85 | 44.20 | 81.20 | 1.85 | 47.60 | 87.50 | 1.85 | 51.00 | 93.80 | 1.85 | 54.40 | 100.00 | 1.85 | 57.80 | 106.00 | 1.85 | 61.20 | 113.00 |
| 19 | | | | 3.70 | 3.40 | 12.60 | 3.70 | 6.80 | 25.20 | 3.70 | 10.20 | 37.70 | 3.70 | 13.60 | 50.20 | 3.70 | 17.00 | 62.50 | 18 | 3.70 | 40.80 | 151.00 | 3.70 | 44.20 | 163.00 | 3.70 | 47.60 | 176.00 | 3.70 | 51.00 | 188.00 | 3.70 | 54.80 | 200.00 | 3.70 | 57.80 | 213.00 |
| 18 | | | | | 3.40 | 12.40 | 3.65 | 6.70 | 24.80 | 3.65 | 10.20 | 37.20 | 3.65 | 13.60 | 49.50 | 3.65 | 17.00 | 62.50 | 17 | 3.65 | 37.40 | 136.00 | 3.65 | 40.80 | 149.00 | 3.65 | 44.20 | 161.00 | 3.65 | 47.60 | 172.00 | 3.65 | 51.00 | 186.00 | 3.65 | 54.80 | 198.00 |
| 17 | | | | | | | 3.60 | 6.80 | 24.40 | 3.60 | 10.20 | 36.60 | 3.60 | 13.60 | 49.20 | 3.60 | 17.00 | 61.60 | 16 | 3.60 | 36.00 | 122.00 | 3.60 | 39.40 | 134.00 | 3.60 | 42.20 | 147.00 | 3.60 | 45.00 | 159.00 | 3.60 | 47.80 | 171.00 | 3.60 | 51.00 | 183.00 |
| 16 | | | | | | | 3.60 | 3.40 | 12.20 | 3.60 | 6.80 | 24.40 | 3.60 | 10.20 | 36.60 | 3.60 | 13.60 | 49.20 | 15 | 3.60 | 30.60 | 110.00 | 3.60 | 34.00 | 122.00 | 3.60 | 37.40 | 134.00 | 3.60 | 40.80 | 147.00 | 3.60 | 44.20 | 159.00 | 3.60 | 47.60 | 171.00 |
| 15 | | | | | | | | | | 3.60 | 3.40 | 12.20 | 3.60 | 6.80 | 24.40 | 3.60 | 10.20 | 36.60 | 14 | 3.60 | 27.20 | 95.00 | 3.60 | 30.60 | 107.00 | 3.60 | 34.00 | 119.00 | 3.60 | 37.40 | 131.00 | 3.60 | 40.80 | 143.00 | 3.60 | 44.20 | 154.00 |
| 14 | | | | | | | | | | | | | | | | 3.50 | 3.40 | 11.90 | 13 | 3.50 | 23.80 | 80.50 | 3.50 | 27.20 | 92.00 | 3.50 | 30.60 | 103.00 | 3.50 | 34.00 | 115.00 | 3.50 | 37.40 | 127.00 | 3.50 | 40.80 | 139.00 |
| 13 | | | | | | | | | | | | | | | | 3.40 | | | 12 | 3.40 | 20.40 | 69.00 | 3.40 | 23.80 | 80.50 | 3.40 | 27.20 | 92.00 | 3.40 | 30.60 | 103.00 | 3.40 | 34.00 | 115.00 | 3.40 | 37.40 | 127.00 |
| 12 | | | | | | | | | | | | | | | | 3.30 | | | 11 | 3.30 | 17.00 | 56.00 | 3.30 | 20.40 | 67.20 | 3.30 | 23.80 | 78.40 | 3.30 | 27.20 | 89.60 | 3.30 | 30.60 | 100.80 | 3.30 | 34.00 | 112.00 |
| 11 | | | | | | | | | | | | | | | | 3.20 | | | 10 | 3.20 | 13.60 | 43.30 | 3.20 | 17.00 | 54.20 | 3.20 | 20.40 | 65.20 | 3.20 | 23.80 | 76.40 | 3.20 | 27.20 | 86.60 | 3.20 | 30.60 | 97.50 |
| 10 | | | | | | | | | | | | | | | | 3.20 | | | 9 | 3.20 | 10.20 | 33.50 | 3.20 | 13.60 | 43.30 | 3.20 | 17.00 | 54.20 | 3.20 | 20.40 | 65.20 | 3.20 | 23.80 | 76.40 | 3.20 | 27.20 | 86.60 |
| 9 | | | | | | | | | | | | | | | | 3.15 | | | 8 | 3.15 | 6.80 | 29.00 | 3.15 | 10.20 | 32.00 | 3.15 | 13.60 | 42.70 | 3.15 | 17.00 | 52.80 | 3.15 | 20.40 | 64.20 | 3.15 | 23.80 | 75.50 |
| 8 | | | | | | | | | | | | | | | | 2.90 | | | 7 | 2.90 | 3.40 | 9.80 | 2.90 | 6.80 | 19.70 | 2.90 | 10.20 | 29.50 | 2.90 | 13.60 | 39.30 | 2.90 | 17.00 | 49.20 | 2.90 | 20.40 | 59.00 |
| 7 | | | | | | | | | | | | | | | | | | | 6 | | | 2.90 | 3.40 | 9.80 | 2.90 | 6.80 | 19.70 | 2.90 | 10.20 | 29.50 | 2.90 | 13.60 | 39.30 | 2.90 | 17.00 | 49.20 | |
| 6 | | | | | | | | | | | | | | | | | | | 5 | | | | | | 2.75 | 3.40 | 9.80 | 2.75 | 6.80 | 18.70 | 2.75 | 10.20 | 28.00 | 2.75 | 13.60 | 37.30 | |
| 5 | | | | | | | | | | | | | | | | | | | 4 | | | | | | | | 2.60 | 3.40 | 8.80 | 2.60 | 6.80 | 17.70 | 2.60 | 10.20 | 26.50 | | |
| 4 | | | | | | | | | | | | | | | | | | | 3 | | | | | | | | | | | | | | | | | | |
| 3 | | | | | | | | | | | | | | | | | | | 2 | | | | | | | | | | | | | | | | | | |
| 2 | | | | | | | | | | | | | | | | | | | 1 | | | | | | | | | | | | | | | | | | |
| 1 | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |

| | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
|-----|------|--|--|------|--|--|-------|--|--|-------|--|--|------|--|--|--------|--|--|-----|---------|--|--|---------|--|--|---------|--|--|---------|--|--|---------|--|--|---------|--|--|
| ΣPh | 6.28 | | | 2520 | | | 56.40 | | | 99.70 | | | 5530 | | | 222.60 | | | ΣPh | 1108.30 | | | 1161.20 | | | 1324.80 | | | 1496.40 | | | 1678.20 | | | 1867.00 | | |
|-----|------|--|--|------|--|--|-------|--|--|-------|--|--|------|--|--|--------|--|--|-----|---------|--|--|---------|--|--|---------|--|--|---------|--|--|---------|--|--|---------|--|--|

| JOINT | 14 | | | 13 | | | 12 | | | 11 | | | 10 | | | 9 | | | JOINT | 2 | | | 1 | | | | |
|-------|------|-------|-------|------|-------|-------|------|-------|--------|------|-------|--------|------|-------|--------|------|-------|--------|-------|-------|-------|--------|-------|-------|--------|-------|--------|
| | P | h | Ph | P | h | Ph | P | h | Ph | P | h | Ph | P | h | Ph | P | h | Ph | | P | h | Ph | P | h | Ph | | |
| 20 | 1.85 | 23.80 | 44.00 | 1.85 | 27.20 | 50.00 | 1.85 | 30.60 | 56.20 | 1.85 | 34.00 | 62.50 | 1.85 | 37.40 | 69.00 | 1.85 | 40.80 | 75.20 | 20 | 1.85 | 66.10 | 121.80 | 1.85 | 70.60 | 130.00 | | |
| 19 | 3.70 | 20.40 | 75.50 | 3.70 | 23.80 | 88.50 | 3.70 | 27.20 | 100.00 | 3.70 | 30.60 | 112.00 | 3.70 | 34.00 | 125.00 | 3.70 | 37.40 | 138.00 | 19 | 3.70 | 61.20 | 226.00 | 3.70 | 66.10 | 244.00 | | |
| 18 | 3.65 | 17.00 | 62.00 | 3.65 | 20.40 | 74.80 | 3.65 | 23.80 | 86.60 | 3.65 | 27.20 | 99.00 | 3.65 | 30.60 | 111.00 | 3.65 | 34.00 | 123.00 | 18 | 3.65 | 57.80 | 210.00 | 3.65 | 61.20 | 223.00 | | |
| 17 | 3.60 | 13.60 | 48.80 | 3.60 | 17.00 | 61.00 | 3.60 | 20.40 | 73.50 | 3.60 | 23.80 | 85.60 | 3.60 | 27.20 | 97.50 | 3.60 | 30.60 | 110.00 | 17 | 3.60 | 54.40 | 195.00 | 3.60 | 57.80 | 207.00 | | |
| 16 | 3.60 | 10.20 | 36.60 | 3.60 | 13.60 | 48.90 | 3.60 | 17.00 | 61.00 | 3.60 | 20.40 | 73.50 | 3.60 | 23.80 | 85.60 | 3.60 | 27.20 | 97.50 | 16 | 3.60 | 51.00 | 183.00 | 3.60 | 54.40 | 195.00 | | |
| 15 | 3.50 | 6.80 | 23.80 | 3.50 | 10.20 | 35.60 | 3.50 | 13.60 | 47.50 | 3.50 | 17.00 | 59.20 | 3.50 | 20.40 | 70.20 | 3.50 | 23.80 | 83.80 | 15 | 3.50 | 47.60 | 166.00 | 3.50 | 51.00 | 178.00 | | |
| 14 | 3.40 | 3.40 | 11.50 | 3.40 | 6.80 | 23.00 | 3.40 | 10.20 | 34.50 | 3.40 | 13.60 | 46.50 | 3.40 | 17.00 | 57.50 | 3.40 | 20.40 | 69.00 | 14 | 3.40 | 44.20 | 150.00 | 3.40 | 47.60 | 161.00 | | |
| 13 | | | | 3.40 | 3.40 | 11.20 | 3.40 | 6.80 | 23.50 | 3.40 | 10.20 | 34.50 | 3.40 | 13.60 | 46.00 | 3.40 | 17.00 | 57.00 | 13 | 3.40 | 40.80 | 139.00 | 3.40 | 44.20 | 152.00 | | |
| 12 | | | | | | | 3.30 | 3.40 | 11.20 | 3.30 | 6.80 | 22.40 | 3.30 | 10.20 | 33.60 | 3.30 | 13.60 | 44.80 | 12 | 3.30 | 37.40 | 123.00 | 3.30 | 40.80 | 134.20 | | |
| 11 | | | | | | | | | | 3.20 | 3.40 | 10.80 | 3.20 | 6.80 | 21.70 | 3.20 | 10.20 | 33.50 | 11 | 3.20 | 34.00 | 108.00 | 3.20 | 37.40 | 120.00 | | |
| 10 | | | | | | | | | | | | | | | 3.20 | 3.40 | 10.80 | 3.20 | 6.80 | 21.70 | 10 | 3.20 | 30.60 | 97.50 | 3.20 | 34.00 | 108.00 |
| 9 | | | | | | | | | | | | | | | 3.15 | 3.40 | 10.70 | 3.15 | 6.80 | 21.70 | 9 | 3.15 | 27.20 | 85.20 | 3.15 | 30.60 | 96.00 |
| 8 | | | | | | | | | | | | | | | | | | | 8 | 2.90 | 23.80 | 69.00 | 2.90 | 27.20 | 78.50 | | |
| 7 | | | | | | | | | | | | | | | | | | | 7 | 2.90 | 20.40 | 59.00 | 2.90 | 23.80 | 69.00 | | |
| 6 | | | | | | | | | | | | | | | | | | | 6 | 2.75 | 17.00 | 46.60 | 2.75 | 20.40 | 56.20 | | |
| 5 | | | | | | | | | | | | | | | | | | | 5 | 2.60 | 13.60 | 35.20 | 2.60 | 17.00 | 46.00 | | |
| 4 | | | | | | | | | | | | | | | | | | | 4 | 2.60 | 10.20 | 26.50 | 2.60 | 13.60 | 35.20 | | |
| 3 | | | | | | | | | | | | | | | | | | | 3 | 2.40 | 6.80 | 16.30 | 2.40 | 10.20 | 24.40 | | |
| 2 | | | | | | | | | | | | | | | | | | | 2 | 2.70 | 3.40 | 9.80 | 2.70 | 6.80 | 18.30 | | |
| 1 | | | | | | | | | | | | | | | | | | | 1 | | | | 1.60 | 3.40 | 5.40 | | |

| | | | | | | | | | | | | | | | | | | | | | | | | | |
|-----|--------|--|--|--------|--|--|--------|--|--|--------|--|--|--------|--|--|--------|--|--|-----|---------|--|--|---------|--|--|
| ΣPh | 302.20 | | | 392.10 | | | 493.50 | | | 606.50 | | | 727.90 | | | 863.90 | | | ΣPh | 2065.50 | | | 2279.20 | | |
|-----|--------|--|--|--------|--|--|--------|--|--|--------|--|--|--------|--|--|--------|--|--|-----|---------|--|--|---------|--|--|

ANALYSIS OF THE EFFECT OF WIND ON A HIGH REINFORCED CONCRETE BUILDING

Comparison of Approximate and Exact Methods

COMPUTER : RIAD SHAHIN

CHK'D BY : RIAD SHAHIN

APP'D BY : DR. JACK NASSER

WIND ANALYSIS
COLUMN AXIAL STRESSES
DATE: DECEMBER 1964 SHEET #147/

| Floor | M_1 (T-m) | M_2 (T-m) | M_1+M_2 (T-m) | $2(M_1+M_2)$ (T-m) | ΣPh (T-m) | $\Sigma Ph-2(M_1+M_2)$ (T-m) | F_1 T | $0.435F$ T |
|-------|----------------|----------------|--------------------|-----------------------|----------------------|---------------------------------|------------|---------------|
| 20 | 0.53 | 0.86 | 1.39 | 2.78 | 6.28 | 3.50 | 0.20 | 0.10 |
| 19 | 1.80 | 2.48 | 4.28 | 8.56 | 25.20 | 16.64 | 0.94 | 0.41 |
| 18 | 2.93 | 4.00 | 6.93 | 13.86 | 56.40 | 42.54 | 2.40 | 1.04 |
| 17 | 4.55 | 5.41 | 9.96 | 19.92 | 99.70 | 79.78 | 4.50 | 1.95 |
| 16 | 4.30 | 6.52 | 10.82 | 21.64 | 155.30 | 133.66 | 7.50 | 3.25 |
| 15 | 5.36 | 8.02 | 13.38 | 26.76 | 222.60 | 195.84 | 11.00 | 4.78 |
| 14 | 6.31 | 9.27 | 15.58 | 31.16 | 302.20 | 271.04 | 15.30 | 6.62 |
| 13 | 8.10 | 10.80 | 18.90 | 37.80 | 392.10 | 364.30 | 20.60 | 8.90 |
| 12 | 6.46 | 9.83 | 16.29 | 32.58 | 493.50 | 460.93 | 26.00 | 11.30 |
| 11 | 7.80 | 11.50 | 19.30 | 38.60 | 606.50 | 567.90 | 32.00 | 13.90 |
| 10 | 8.35 | 15.78 | 24.13 | 48.26 | 727.90 | 679.64 | 38.30 | 16.80 |
| 9 | 10.35 | 16.10 | 26.45 | 52.90 | 863.90 | 811.00 | 45.80 | 19.90 |
| 8 | 7.90 | 14.47 | 22.37 | 44.74 | 1008.30 | 963.56 | 54.40 | 24.00 |
| 7 | 9.20 | 16.50 | 25.70 | 51.40 | 1161.20 | 1109.80 | 62.50 | 27.20 |
| 6 | 10.00 | 17.83 | 27.83 | 55.66 | 1324.80 | 1269.14 | 71.50 | 31.00 |
| 5 | 12.25 | 19.00 | 31.25 | 62.50 | 1496.40 | 1433.90 | 80.60 | 35.00 |
| 4 | 8.20 | 16.40 | 24.60 | 49.20 | 1678.20 | 1629.00 | 92.00 | 40.00 |
| 3 | 8.30 | 20.37 | 28.67 | 57.34 | 1867.00 | 1809.66 | 102.00 | 44.20 |
| 2 | 31.05 | 41.73 | 72.78 | 145.56 | 2065.50 | 1919.94 | 108.00 | 46.80 |
| 1 | 46.22 | 51.60 | 97.82 | 195.64 | 2279.20 | 2083.56 | 118.00 | 51.00 |

| Column Designation | Area m ² | P | | P _t (T) | M (T-m) | e (M/F) | Condition of Failure | Pg % | REINFORCEMENT | | | | | Moment of inertia of Concrete Section | | Moment of inertia of Steel Section | | Total moment of inertia | | F _a (T/m ²) | F _b (T/m ²) | F _a / F _b | F _a + F _b | Sections Showing Reinforcement | | | | |
|--------------------|---------------------|----------|--------------|--------------------|---------|---------|----------------------|------|----------------------|------------|--------------|-------|-------|---------------------------------------|-------|------------------------------------|-------------------------|----------------------------------|----------------------------------|------------------------------------|------------------------------------|---------------------------------|---------------------------------|--------------------------------|---|---------------------------------|------|--|
| | | D.L. (T) | Windload (T) | | | | | | As (m ²) | Revd / Row | As Furnished | Row | a (m) | b (m) | c (m) | d (m) | e (m) | I _c (m ⁴) | I _s (m ⁴) | | | | | | I _c + I _s (m ⁴) | I _c / I _s | | |
| 20a | 0.50x0.40=0.20 | 94.70 | 0.10 | 94.80 | 1.96 | < 1/3 | Compression | 1 | 20 | 10 | 4φ18 | 10 | 0.10 | | | 0.00262 | 0.01 x 10 = 0.0001 | 15 | 0.00015 | 0.00277 | 640 | 1180 | 472 | 181.20-144 2.40 0.0277 | 472 = 0.74 1180 = 0.12 | 0.86 | | |
| 14a | " | 118.40 | 0.41 | 118.81 | 3.53 | " | " | 2 | 40 | 20 | 2φ28 2φ25 | 24.41 | " | " | " | 0 | 0.01 x 24.40 = 0.000244 | " | 0.00036 | 0.00299 | 808 | " | 592 | 3.53x20=70.6 0.0036 | 592 = 0.74 798 = 0.21 | 0.95 | | |
| 18a | " | 142.10 | 1.04 | 143.14 | 5.32 | " | " | 4 | 80 | 40 | 2φ40 2φ32 | 40.41 | " | " | " | 0 | 0.01 x 40.40 = 0.000404 | " | 0.00605 | 0.00323 | 1144 | " | 713 | 5.32x40=212.8 0.00323 | 713 = 0.62 1144 = 0.28 | 0.90 | | |
| 17a | " | 165.80 | 1.95 | 167.75 | 6.38 | " | " | 5 | 100 | 50 | 4φ40 | 48.80 | " | " | " | 0 | 0.01 x 48.80 = 0.000488 | " | 0.00732 | 0.00352 | 1310 | " | 835 | 6.38x50=319 0.00352 | 835 = 0.64 1180 = 0.21 | 0.95 | | |
| 16a | 0.50x0.40=0.20 | 193.35 | 3.25 | 193.60 | 9.37 | " | " | 3 | 90 | 2250 | 4φ28 | 24.40 | 0.10 | 0.20 | | 0.00900 | 0.05 x 24.40 = 0.001220 | " | 0.00182 | 0.0108 | 976 | " | 640 | 9.37x90=843.3 0.0108 | 640 = 0.65 1180 = 0.22 | 0.87 | | |
| 15a | " | 214.90 | 4.78 | 219.68 | 10.76 | " | " | 4 | 120 | 30 | 4φ32 | 32 | " | " | " | 0 | 0.05 x 32 = 0.00160 | " | 0.0024 | 0.0114 | 1144 | " | 730 | 10.76x30=322.8 0.0114 | 730 = 0.64 1180 = 0.24 | 0.86 | | |
| 14a | " | 239.45 | 6.62 | 246.07 | 12.34 | " | " | 5 | 150 | 375 | 2φ40 2φ30 | 38.80 | " | " | " | 0 | 0.05 x 37.58 = 0.001879 | " | 0.0029 | 0.0119 | 1310 | " | 815 | 12.34x150=1851 0.0119 | 815 = 0.63 1180 = 0.26 | 0.89 | | |
| 13a | " | 264.00 | 8.90 | 272.90 | 12.97 | " | " | 5 | 150 | 375 | 2φ40 2φ30 | 38.80 | " | " | " | 0 | 0.05 x 38.80 = 0.00194 | " | 0.0029 | 0.0119 | 1310 | " | 903 | 12.97x150=1945.5 0.0119 | 903 = 0.69 1180 = 0.28 | 0.97 | | |
| 12a | 0.50x0.30=0.15 | 287.40 | 11.30 | 300.70 | 15.63 | " | " | 3 | 120 | 20 | 2φ28 2φ25 | 22.20 | 0.10 | 0.20 | 0.50 | 0.0213 | 0.14 x 22.20 = 0.003108 | " | 0.0047 | 0.0260 | 976 | " | 750 | 15.63x20=312.6 0.0260 | 750 = 0.77 1180 = 0.20 | 0.97 | | |
| 11a | " | 314.80 | 13.80 | 328.70 | 17.39 | " | " | 4 | 140 | 2660 | 2φ32 2φ30 | 30 | " | " | " | 0 | 0.14 x 30 = 0.0042 | " | 0.0063 | 0.0276 | 1144 | " | 820 | 17.39x40=705.6 0.0276 | 820 = 0.72 1180 = 0.23 | 0.93 | | |
| 10a | " | 340.20 | 16.80 | 357.00 | 18.98 | " | " | 5 | 200 | 3330 | 2φ40 2φ35 | 34.20 | " | " | " | 0 | 0.10 x 34.26 = 0.003426 | " | 0.0072 | 0.0285 | 1310 | " | 890 | 18.98x20=379.6 0.0285 | 890 = 0.68 1180 = 0.23 | 0.91 | | |
| 9a | " | 365.60 | 19.90 | 385.50 | 17.84 | " | " | 5 | 200 | 3330 | 2φ40 2φ35 | 34.20 | " | " | " | 0 | 0.14 x 34.26 = 0.004794 | " | 0.0072 | 0.0285 | 1310 | " | 960 | 17.84x20=356.8 0.0285 | 960 = 0.74 1180 = 0.21 | 0.95 | | |
| 8a | 0.50x0.40=0.20 | 391.85 | 24.00 | 414.85 | 22.66 | " | " | 4 | 200 | 25 | 4φ28 | 24.40 | 0.10 | 0.20 | 0.30 | 0.40 | 0.0416 | 0.30 x 24.40 = 0.00732 | " | 0.0110 | 0.0526 | 1144 | " | 828 | 22.66x25=566.5 0.0526 | 828 = 0.72 1180 = 0.18 | 0.90 | |
| 7a | " | 418.10 | 27.20 | 445.30 | 24.58 | " | " | 4 | 200 | 25 | 4φ28 | 24.40 | " | " | " | " | 0 | 0.30 x 24.40 = 0.00732 | " | 0.0110 | 0.0526 | 1144 | " | 890 | 24.58x25=614.5 0.0526 | 890 = 0.78 1180 = 0.20 | 0.98 | |
| 6a | " | 444.35 | 31.00 | 475.35 | 25.36 | " | " | 5 | 250 | 3125 | 4φ32 | 32 | " | " | " | " | 0 | 0.30 x 32 = 0.0096 | " | 0.0144 | 0.0560 | 1310 | " | 950 | 25.36x32=811.5 0.0560 | 950 = 0.73 1180 = 0.19 | 0.92 | |
| 5a | " | 470.60 | 35.00 | 505.60 | 24.72 | " | " | 5 | 250 | 3125 | 4φ32 | 32 | " | " | " | " | 0 | 0.30 x 32 = 0.0096 | " | 0.0144 | 0.0560 | 1310 | " | 1010 | 24.72x32=791.0 0.0560 | 1010 = 0.77 1180 = 0.18 | 0.95 | |
| 4a | 0.50x0.40=0.20 | 497.70 | 4.00 | 537.70 | 28.28 | " | " | 4 | 240 | 24 | 4φ28 | 24.40 | 0.10 | 0.20 | 0.30 | 0.50 | 0.0720 | 0.55 x 24.40 = 0.01342 | " | 0.0200 | 0.092 | 1144 | " | 890 | 28.28x24=678.7 0.092 | 890 = 0.78 1180 = 0.16 | 0.94 | |
| 3a | " | 520.80 | 44.20 | 569.00 | 33.24 | " | " | 5 | 300 | 30 | 4φ32 | 32 | " | " | " | " | 0 | 0.55 x 32 = 0.0176 | " | 0.0264 | 0.0984 | 1310 | " | 945 | 33.24x30=997.2 0.0984 | 945 = 0.78 1180 = 0.17 | 0.99 | |
| 2a | " | 550.05 | 46.80 | 600.85 | 44.70 | " | " | 5 | 300 | 30 | 4φ32 | 32 | " | " | " | " | 0 | 0.55 x 32 = 0.0176 | " | 0.0264 | 0.0984 | 1310 | " | 1000 | 44.70x30=1341 0.0984 | 1000 = 0.76 1180 = 0.23 | 0.99 | |
| 1a | " | 582.80 | 51.00 | 633.80 | 52.50 | " | " | 6 | 360 | 36 | 2φ40 2φ32 | 40.40 | " | " | " | " | 0 | 0.55 x 40.40 = 0.02222 | " | 0.0333 | 0.1053 | 1480 | " | 1050 | 52.50x36=1890 0.1053 | 1050 = 0.71 1180 = 0.25 | 0.96 | |

| ANALYSIS OF THE EFFECT OF WIND ON A HIGH REINFORCED CONCRETE BUILDING | |
|---|-----------------------------------|
| Comparison of Approximate and Exact Methods | |
| COMPUTER | REINFORCEMENT IN COLUMNS |
| CHKD BY: RIAO SHAHIN | DATE: DECEMBER 1984 SHEET NO. 149 |
| APP'D BY: DR. JACK NASSER | |

PART D

CRITICAL FRAME FOOTINGS

Interior Footing:

1. Concrete and Steel Data

$$f'_c = 263 \text{ Kg/cm}^2$$

$$f_c = 118 \text{ Kg/cm}^2$$

$$f_s = 2100 \text{ Kg/cm}^2$$

$$v = 0.03 \times 263 = 7.90 \text{ Kg/cm}^2$$

$$u = 0.08 \times 263 = 21.00 \text{ Kg/cm}^2$$

2. Proportioning

$$P = 633.80 \text{ T}$$

$$M = 52.50 \text{ T-m}$$

$$\text{Bearing Capacity} = 300 \text{ T/m}^2$$

$$D.L. = 0.06 \times 633.80 = 38.20 \text{ T}$$

$$P_{\text{total}} = 633.80 + 38.20 = 672.00 \text{ T}$$

$$A = \frac{672}{300} = 2.25 \text{ m}^2$$

Use $1 \times 2.25 \text{ m}$

$$q_n = \frac{633.80}{2.25} = 282 \text{ T/m}^2$$

$$s = \frac{2.25}{1} = 2.25$$

$$B' = B \sqrt{2s - 1} = 1.00 \sqrt{4.50 - 1} = 1 \sqrt{3.50} = 1.86 \text{ m}$$

$$\frac{a}{B'} = \frac{0.50}{1.86} = 0.27$$

Use Eq. 19.2⁽¹⁾

$$\frac{d}{B'} = \frac{\sqrt{2C + 4C^2 + \frac{K^2}{4}} - \frac{K}{2}(1+4C)}{2 + 4C}$$

The constant C is evaluated from the net soil pressure q_n (lb/sq.ft) and allowable diagonal tension v (lb/sq.in) by the expression

$$C = \frac{q_n}{500v}$$

$$q_n = 28.20 \text{ Kg/cm}^2 = \frac{28.20}{0.07} = 403 \text{ psi} = 403 \times 12^2 = 58,000 \text{ lb/ft}^2$$

$$v = \frac{7.90}{0.07} = 113 \text{ psi}$$

$$C = \frac{58,000}{500 \times 113} = 1.03$$

$$K = \frac{a}{B'} = 0.27$$

$$\begin{aligned} \frac{d}{B'} &= \frac{\sqrt{2.06 + 4 \times 1.07 + 0.073/4} - 0.135(1+4.12)}{2 + 4.12} \\ &= \frac{\sqrt{2.06 + 4.28 + 0.018} - 0.135(5.12)}{6.12} \\ &= \frac{\sqrt{6.36} - 0.69}{6.12} = \frac{2.52 - 0.69}{6.12} \\ &= \frac{1.83}{6.12} = 0.30 \end{aligned}$$

(1) Peck, Hanson and Thornburn, "Foundation Engineering", P. 315, John Wiley & Sons, Inc. New York, 1953.

$$d = 0.30 \times 1.86 = 56 \text{ cms} \quad \text{say } 60 \text{ cms.}$$

$$kd = 0.312 \times 0.80 = 0.25 \text{ m}$$

$$jd = 0.896 \times 0.80 = 0.72 \text{ m}$$

3. Net Soil Pressures

$$e = \frac{M}{P} = \frac{52.50}{672} = 0.078 < \frac{2.25}{6} \quad \text{so resultant in mid } 1/3$$

$$\begin{aligned} q &= \frac{\sum V}{BL} \left(1 \mp \frac{6e}{l} \right) \\ &= \frac{672}{2.25} \left(1 \mp 6 \times \frac{0.078}{2.25} \right) \\ &= 300 (1 \mp 0.21) = 365 \text{ T/m}^2 = q_{\text{max}} \\ &= 237 \text{ T/m}^2 = q_{\text{min}} \end{aligned}$$

4. Check Diagonal Tension at de

The critical sections for shear is commonly located at a distance d from the face of the column, which falls outside the footing. This means that ^{the} footing is quite safe for shear.

However, the 1963 edition of the A.C.I. Code permits the location of the critical section at a distance of $d/2$. Checking the shear at this section we have:

$$\begin{aligned} \text{Average pressure on efgh} &= \frac{360 + 365}{2} (1.00 \times 0.125) \\ &= 362.50 \times 0.125 = 40.20 \text{ T} = V \\ v = \frac{V}{bd} &= \frac{40.20}{1.00 \times 0.80} = \frac{40.20}{0.80} = 50.20 \text{ T/m}^2 \\ &< 79 \text{ T/m}^2 \end{aligned}$$

∴ O.K.

5. Check Concrete at ab

Use two triangular pressure variations for convenience.

$$\frac{365}{2} (0.40 \times 1.00) = 73 \text{ T}$$

$$\times \frac{2}{3} (0.40) = 19.50 \text{ T-m}$$

$$\frac{335}{2} (0.40 \times 1.00) = 67 \text{ T}$$

$$\times \frac{1}{3} \times 0.40 = \frac{8.90}{28.40} \text{ T-m}$$

$$V = \overline{140} \text{ T}$$

$$\text{Total Compression} = \frac{28.40}{0.72} = 39.50 \text{ T}$$

$$\therefore \div \left(\frac{1.00 \times 0.25}{2} \right) = 315 \text{ T/m}^2$$

$$< 1180 \text{ T/m}^2$$

6. Steel Required at ab

$$A_s = \frac{39.50}{2100} \text{ m}^2 = 188 \text{ m}^2$$

Use 24 ϕ 32

$$A_s \text{ (furnished)} = 192 \text{ cm}^2$$

$$\sum o \text{ (furnished)} = 240 \text{ cms}$$

$$v = \frac{140}{2.40 \times 0.72} = 81 \text{ T/m}^2$$

$$< 210 \text{ T/m}^2$$

7. Steel Required at jK

Since the moment may act in either direction, use average pressure from ϕ to K over entire area.

$$\text{Average pressure} = \frac{300 + 365}{2} = 332.50 \text{ T/m}^2$$

$$V = 332.50 (0.25 \times 2.25) = 187 \text{ T}$$

$$\times 0.125 = 24.30 \text{ T-m} = M$$

$$As = \frac{24.30}{2100 \times 0.72} \times 10^4 = 160 \text{ cm}^2$$

Use 20 ϕ 32 mm

$$As \text{ (furnished)} = 160 \text{ cm}^2$$

$$o \text{ (furnished)} = 200 \text{ cms}$$

$$U = \frac{187}{2.00 \times 0.72} = 130 \text{ T/m}^2 < 210 \text{ T/m}^2$$

Use 24 ϕ 32 long way)
 Use 20 ϕ 32 short way) Uniform spacing

N.B. Since the size of the most critical footing is relatively small, it is recommended to maintain the same size for other footings.